Time-Predictable Communication in Networks-on-Chip

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Real-Time Systems

Strict timing **guarantees**

- Critical tasks have to be completed in time

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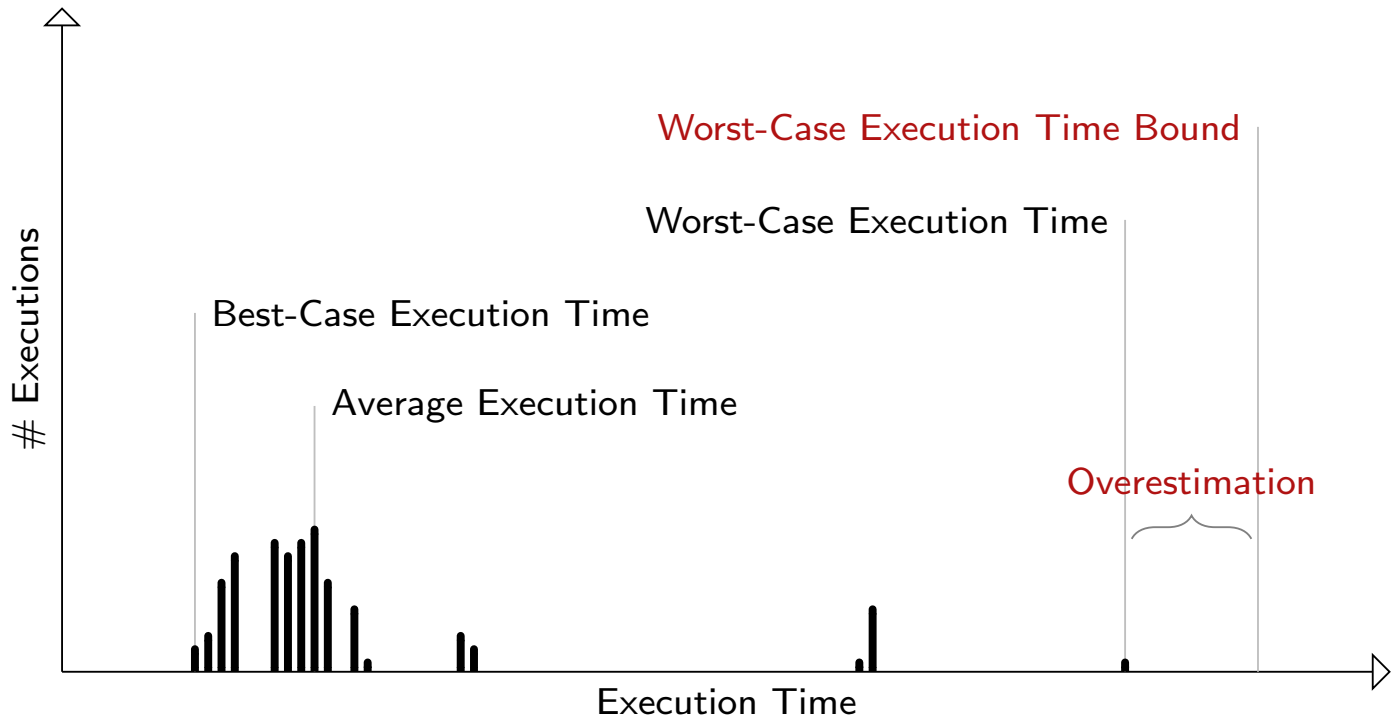

Networks-on-Chip

What is a Network-on-Chip (NoC)?

- Nodes: processors, specialized accelerators, memories, ...
- Nodes connected to routers
- Routers interconnected by links

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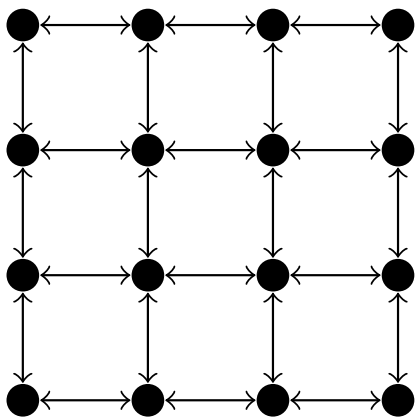
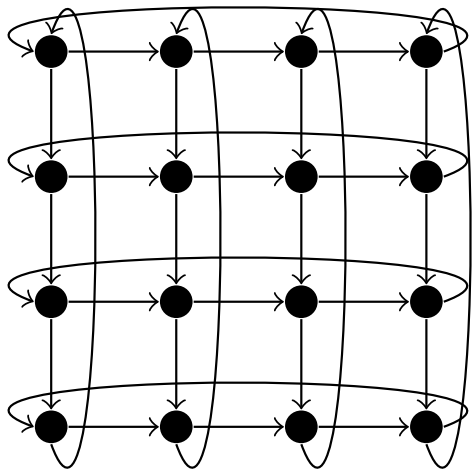
- Nodes connected to routers
- Routers interconnected by links
- Provide means to exchange messages between nodes

Network Topologies

Define structure and layout of nodes, routers, and links:



Mesh



Torus

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  - Nodes involved in the completion of the task
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Clear separation of independent tasks w.r.t. the NoC needed.

Make it time-predictable ...

Two options

1. Guarantee throughput by buffering
2. Guarantee exclusive access by arbitration

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Buffers:

- Incur hardware overhead
- How determine buffer sizes?
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- Requirements are application-specific

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- Incur hardware overhead
- How determine buffer sizes?
- How determine bandwidth per router/link?
- Requirements are application-specific
- Not suited for a generic, cost-effective platform

The S4 Design

Minimalistic time-multiplexed NoC

- Fixed, static schedules
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- Guarantees
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  - Separation of independent tasks
  - Analyzability of worst-case behavior
- Minimal hardware requirements
  - Routers are simple multiplexers
  - Static schedule tables at routers

Schedule Construction

Some assumptions

- Every node sends one message to every other node
- Every node receives one message from every other node
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- Message = packet = flit = phit = 1 data word
- A hop from one router to the next takes one cycle
- Network given as a graph $G = (N \cup R, E)$
  N ... nodes, R ... router, E ... links

Schedule Construction (2)

Solve a multi-commodity flow problem over time:

- Commodities correspond to messages
- Minimize time to deliver all commodities/messages

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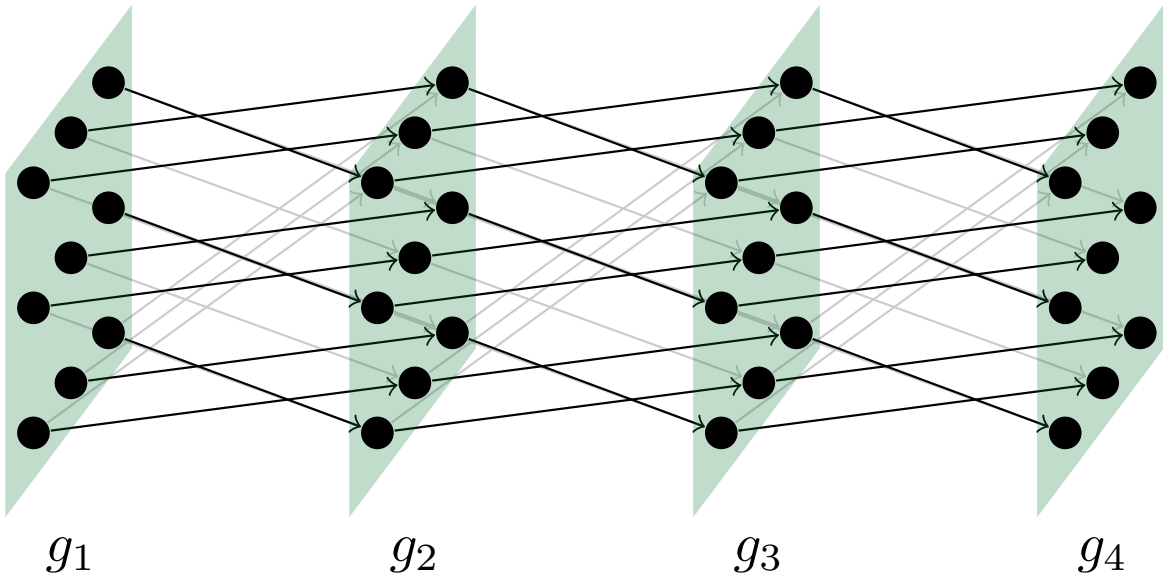
Solve a multi-commodity flow problem over time:

- Commodities correspond to messages
- Minimize time to deliver all commodities/messages
- Modeled as Integer Linear Program (ILP)
  - Given a network G construct a time-expanded network G^T
  - G^T consists of copies of G: $g_1, \ldots g_T$
  - Edges lead from some copy g_i to g_{i+1}
  - Solve a standard flow problem on G^T

Example: Time-Expanded 3×3 Torus



The time-expanded network represents the state of the NoC on all time instants during the schedule construction.

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Variables

- $\ell_{l,n}^{t}$: Use link l to send a message to node n at time instant t

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  All messages flowing into a router have to flow out again.

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  All messages flowing into a router have to flow out again.
- $\sum_{l \in In(n,t)} \ell^t_{l,n} = |N| - 1$
  Receive a message from every other node.
- $\sum_{l \in Out(s,t)} \ell^t_{l,d} = 1$
  Send once from source node s to destination node d.

Solving the Linear Program

Using a generic ILP solver

- CPLEX 12.3 academic
- DTU's `hms2` server
  8 Quad-Core AMD Opteron 8356 (32 cores), 256 GB RAM

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  (no initial solution, generous upper bound for schedule length)
  - Topologies: mesh, torus, bidir. torus (also: tree, fat-tree)
- Considerable improvements possible

Some results

Topology	Nodes	Routers	Links	Schedule Length
Mesh	4	4	8+8	5
	9	9	24+18	10
	16	16	48+32	18
	25	25	80+50	34
Torus	4	4	8+8	5
	9	9	18+18	11
	16	16	32+32	26
	25	25	50+50	54*
Bidir. Torus	4	4	16+8	4
	9	9	36+18	10
	16	16	64+32	18
	25	25	100+50	27

* DNF ... (lower bound from CPLEX: 52)

Dealing with Larger Networks

Observations from ILP solutions

- Paths taken for message routes
  - One straight horizontal or vertical segment, or
  - One horizontal and one vertical segment (X-Y, Y-X)
  - No detours, shortest routes only

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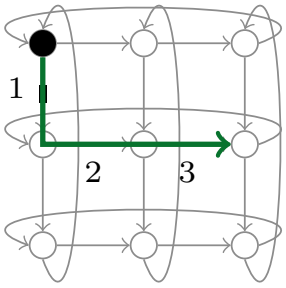
Observations from ILP solutions

- Paths taken for message routes
  - One straight horizontal or vertical segment, or
  - One horizontal and one vertical segment (X-Y, Y-X)
  - No detours, shortest routes only
- We can exploit regularities of network topologies
  - Construct symmetric schedules
  - Synchronize all routers
  - Use the same schedule table everywhere

Example: Partial, Optimal Solution for the 3×3-Torus



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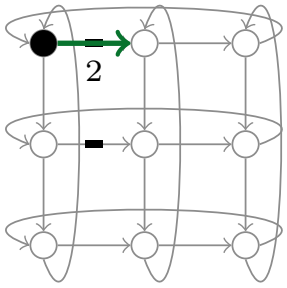

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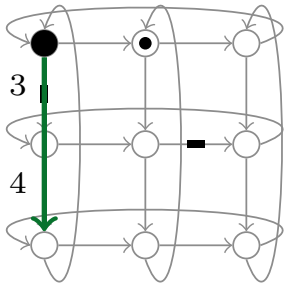

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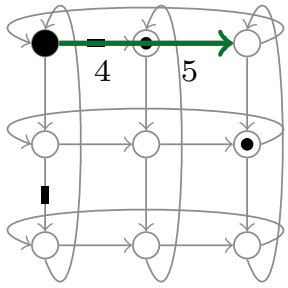

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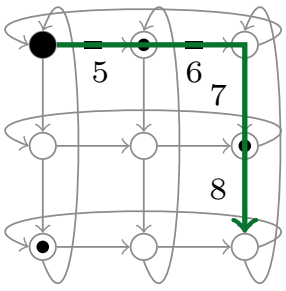

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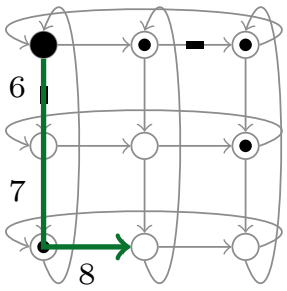

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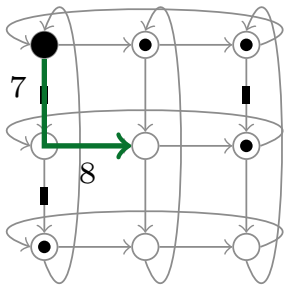

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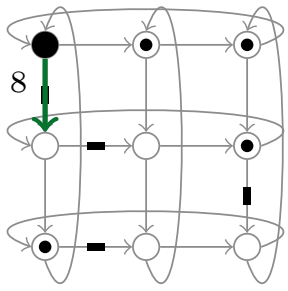

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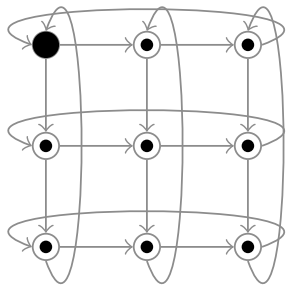
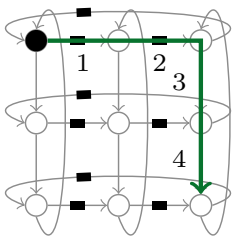

Step 9

This schedule cannot be replicated everywhere,
due to conflicts, e.g., at cycle 2.

Example: Symmetric Solution for the 3×3-Torus



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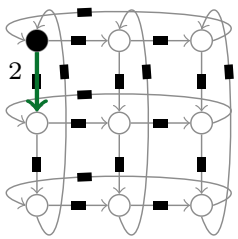

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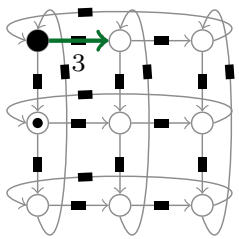

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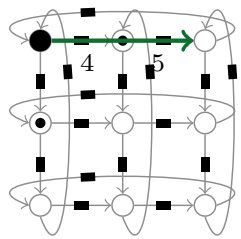

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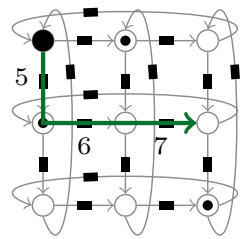

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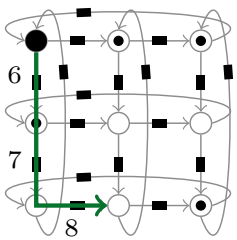

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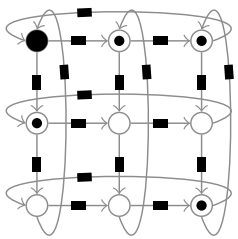
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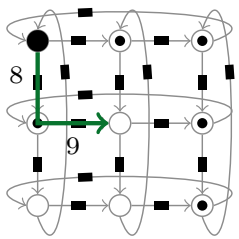

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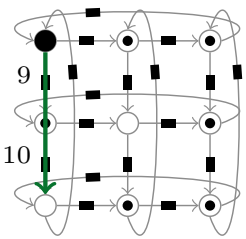

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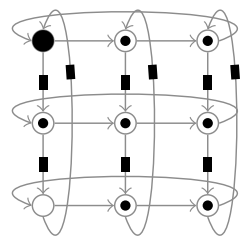
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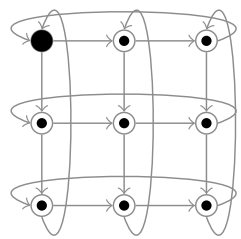
Step 11

This schedule can be replicated everywhere.

A Heuristic Algorithm

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- Schedule relative to **one** reference node, then replicate
  - Restrict paths considered as routes
  - Only shortest routes from reference node
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  - So-so: 2D-mesh
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  - Yes: torus, bidirectional torus, ...
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  - No: tree, fat-tree, star, ...
- As before
  - all-to-all communication
  - single-cycle hops
  - Message = 1 flit = 1 word

A Heuristic Algorithm (2)

1. Compute set of candidate routes
   - Set of routes from the reference node to all other nodes
   - Example: shortest, X-Y and Y-X routes
2. Select a *good* candidate
   - Example: a longest remaining route
3. Schedule the candidate route
   - Avoid conflicts with already scheduled routes
   - Example: schedule as early as possible
4. Remove all *equivalent* candidate routes
5. Repeat step 2-4 until no candidate route remains

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  invalid: `eesss` / `wwss` valid: `eesss` / `wwss`
- Routes are equivalent when they lead to the same target node
  Example: `eesss` $\equiv$ `sssee`

Experiments

Several heuristic configurations

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  1 Dual-Core AMD Fusion E-350 (1 core), 2 GB RAM
- Network size up to 900 nodes
  - Network topologies: torus, bidirectional torus (also: mesh)
- Compare schedule lengths and execution times
  - Theoretical bounds: network capacity, bisection bandwidth
  - Optimal results (as far as available)

Configurations

Candidate selection

- Sht: Shortest routes first
- Rnd: Select random route
- Lng: Longest routes first
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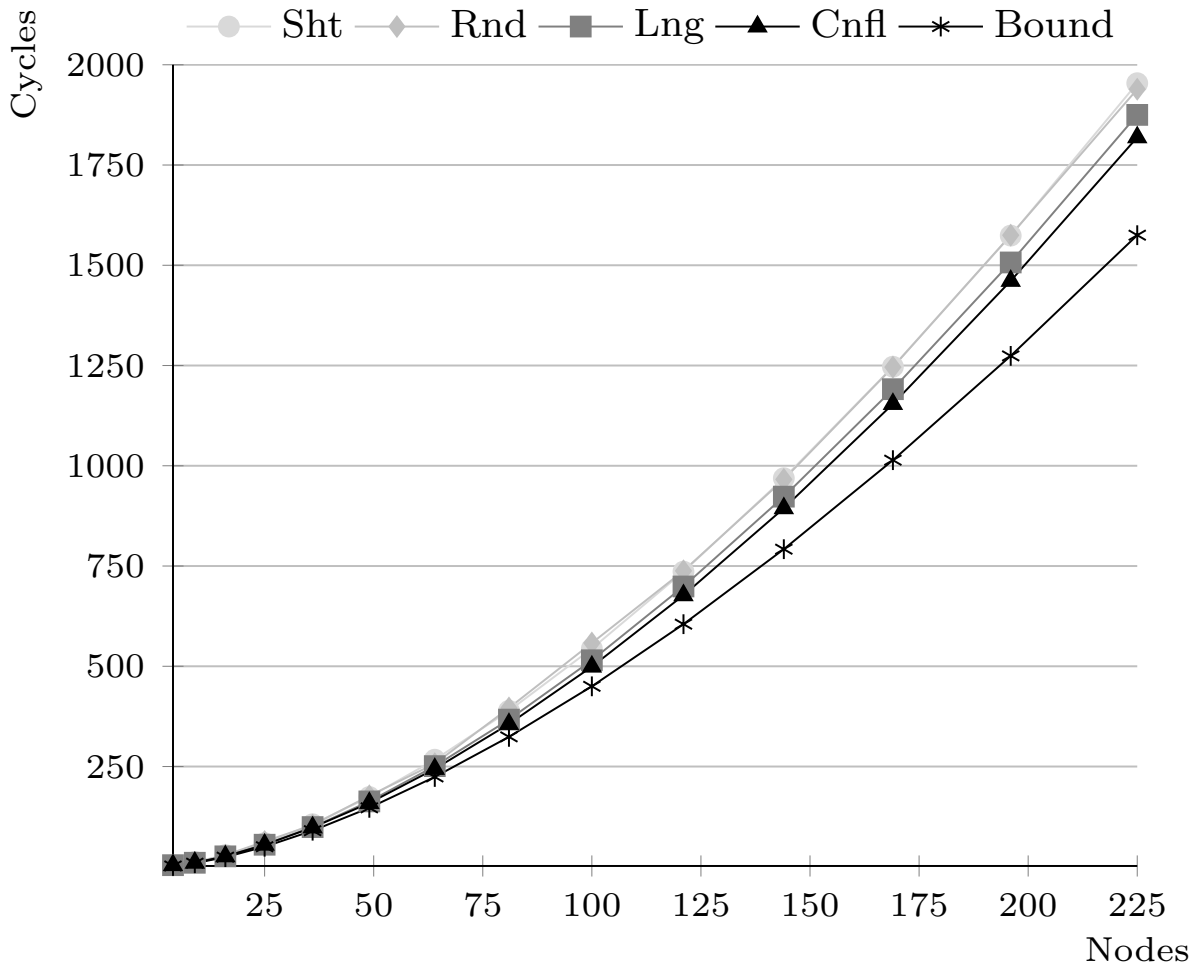
Scheduling

- Schedule as early as possible
- Naive checking for conflicts

Schedule Lengths – Torus



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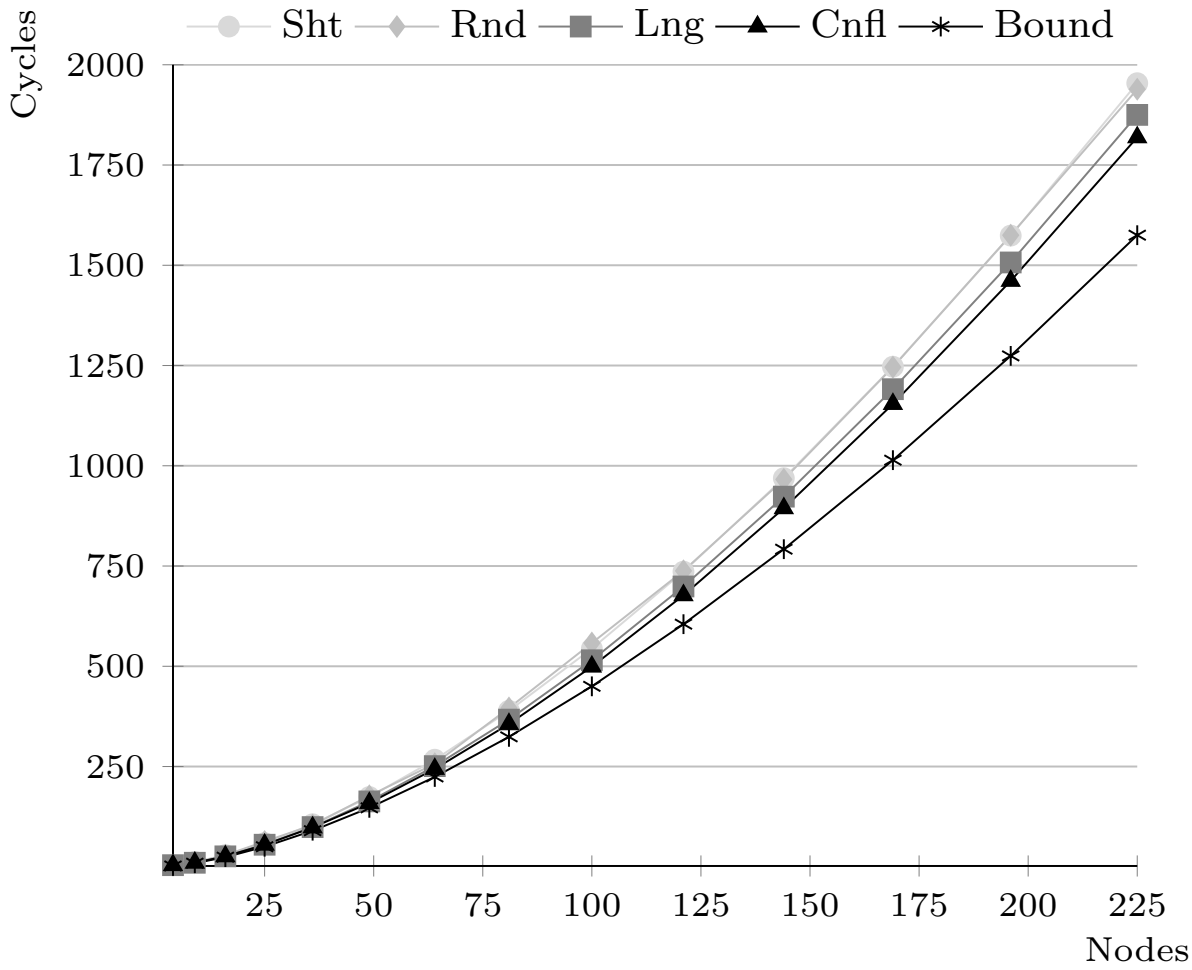
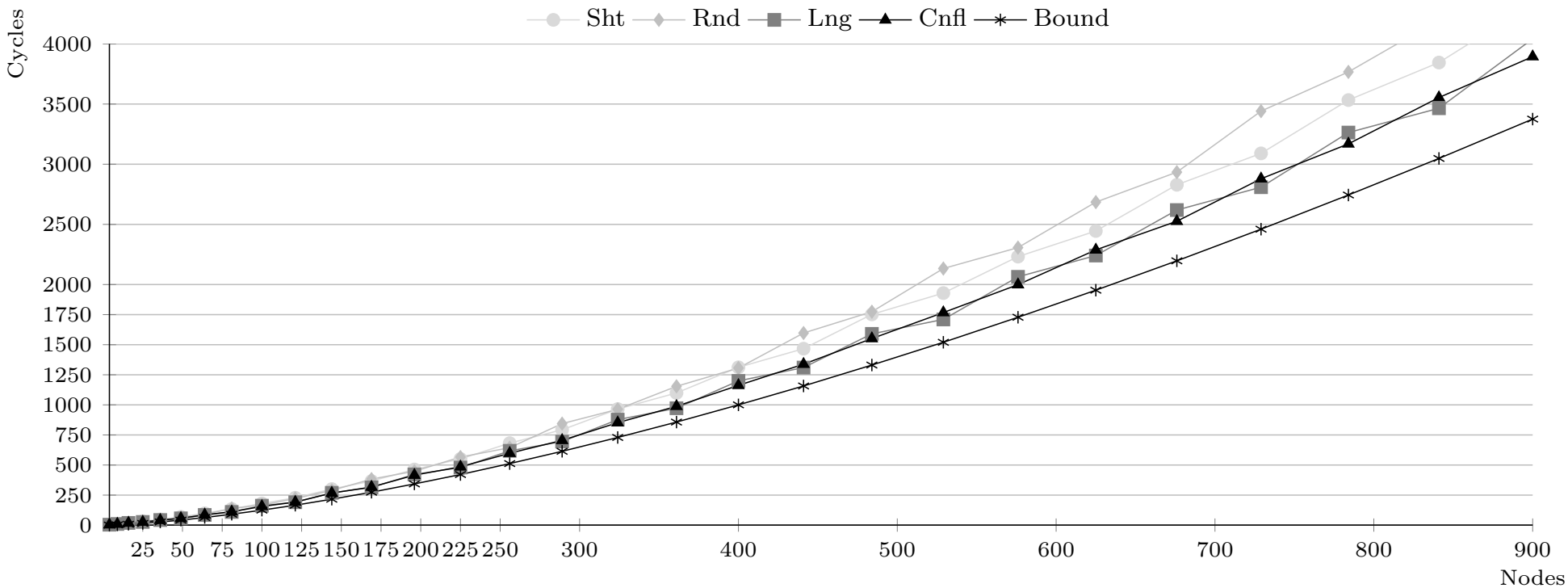


Heuristic is within 15-20% of theoretical lower bound.

Schedule Lengths – Bidirectional Torus



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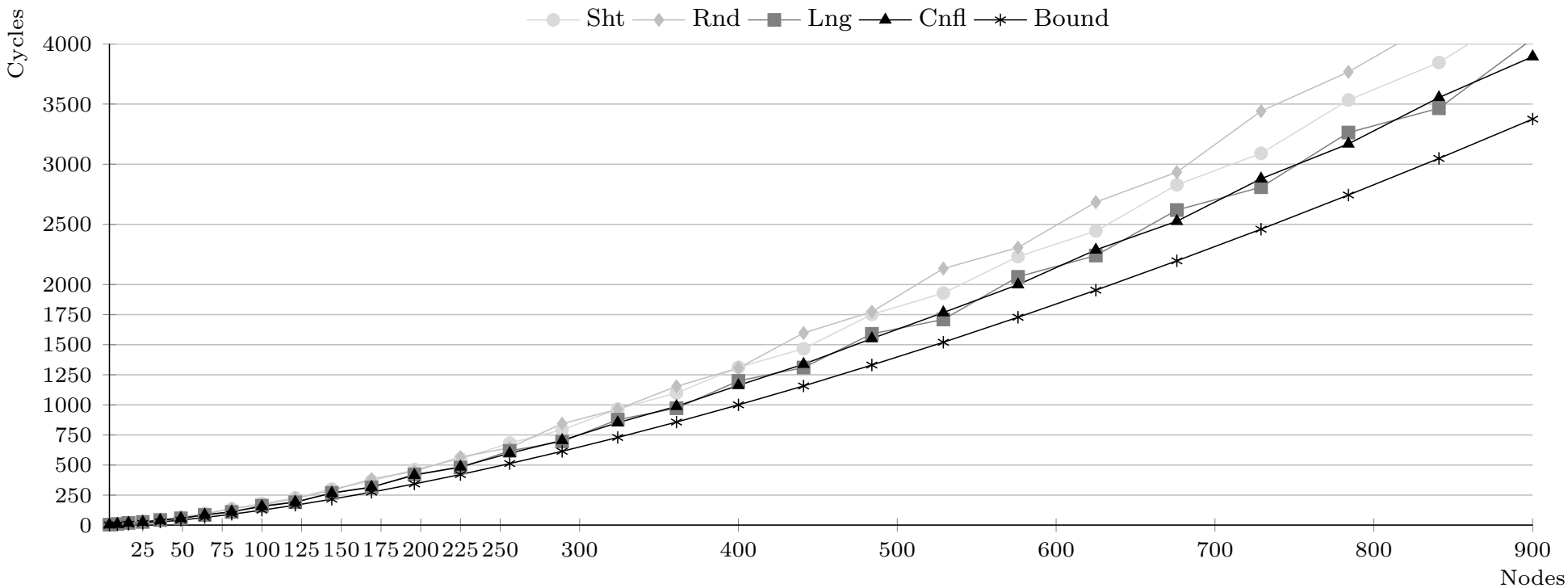


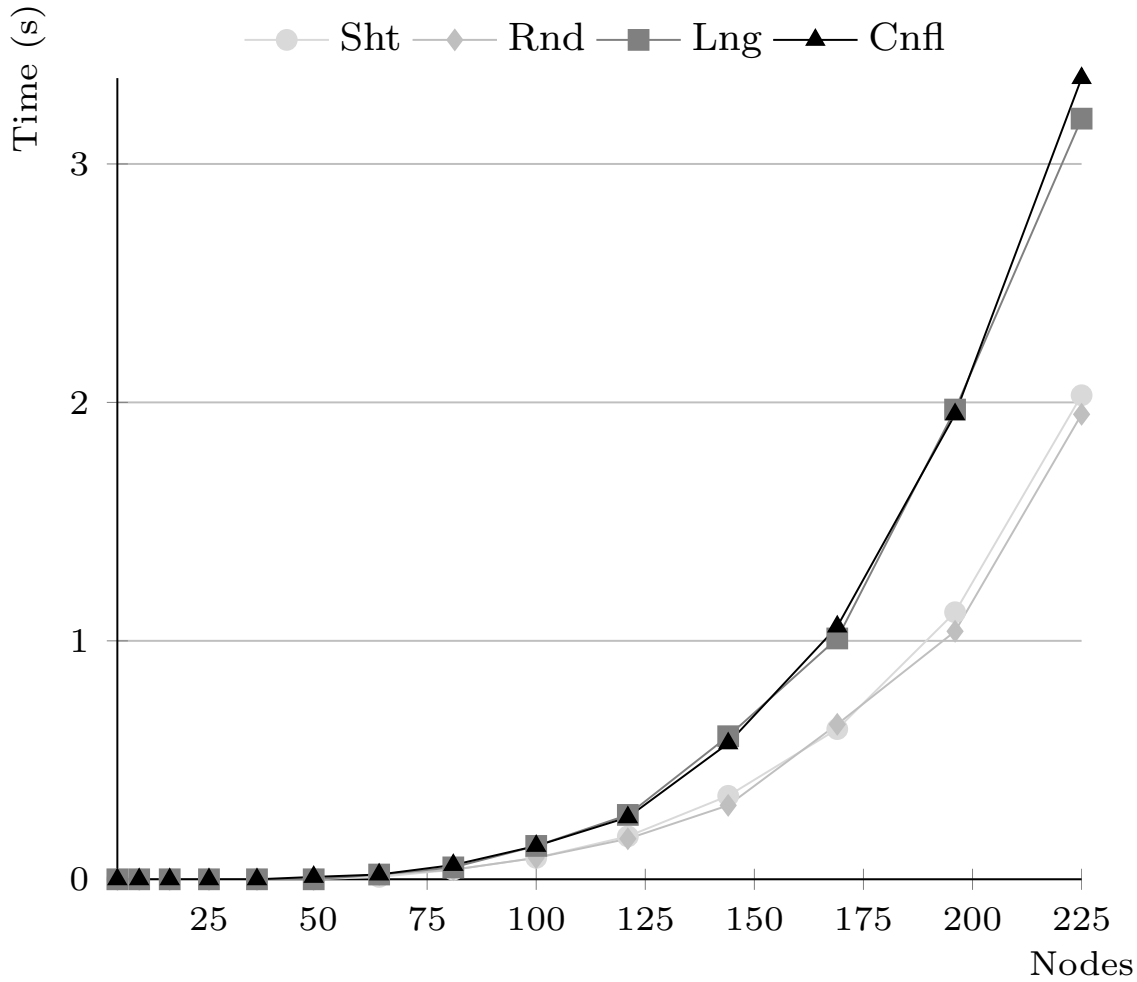
Again within 15-20% of theoretical lower bound.

Heuristic vs. Optimal Solutions

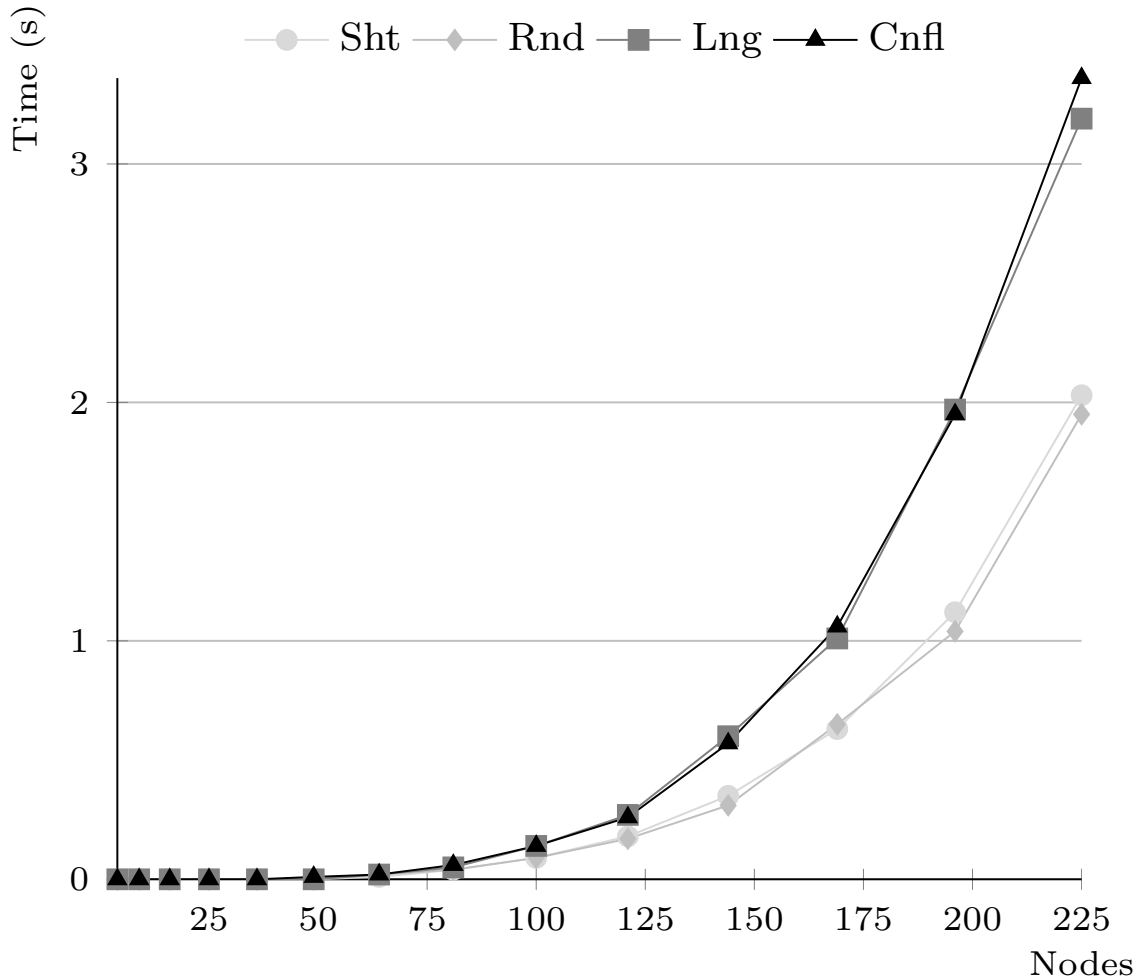
Topology	Nodes	Optimal	Heuristic	Ratio
Torus	4	5	5	1.00
	9	11	11	1.00
	16	26	27	1.04
	25	54*	56	1.04
Bidir. Torus	4	4	5	1.25
	9	10	10	1.00
	16	18	19	1.06
	25	27	28	1.04

* still: DNF ...

Execution Time – Bidirectional Torus



Execution Time – Bidirectional Torus



Polynomial curve, can clearly be improved by more efficient tracking of conflicts.

Conclusion

S4 network-on-chip

- Minimal hardware requirements NoC
- Static schedules at routers

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Heuristic scheduling

- Exploit regularity of NoC topology
- Simple, yet efficient
- 15-20% from lower bounds
- Even closer to optimal solutions

Future Work

Optimal scheduling

- Start from heuristic solution
- Prune search space
- Restrict freedom of routes

  Conjecture: Optimal symmetric schedules are globally optimal.

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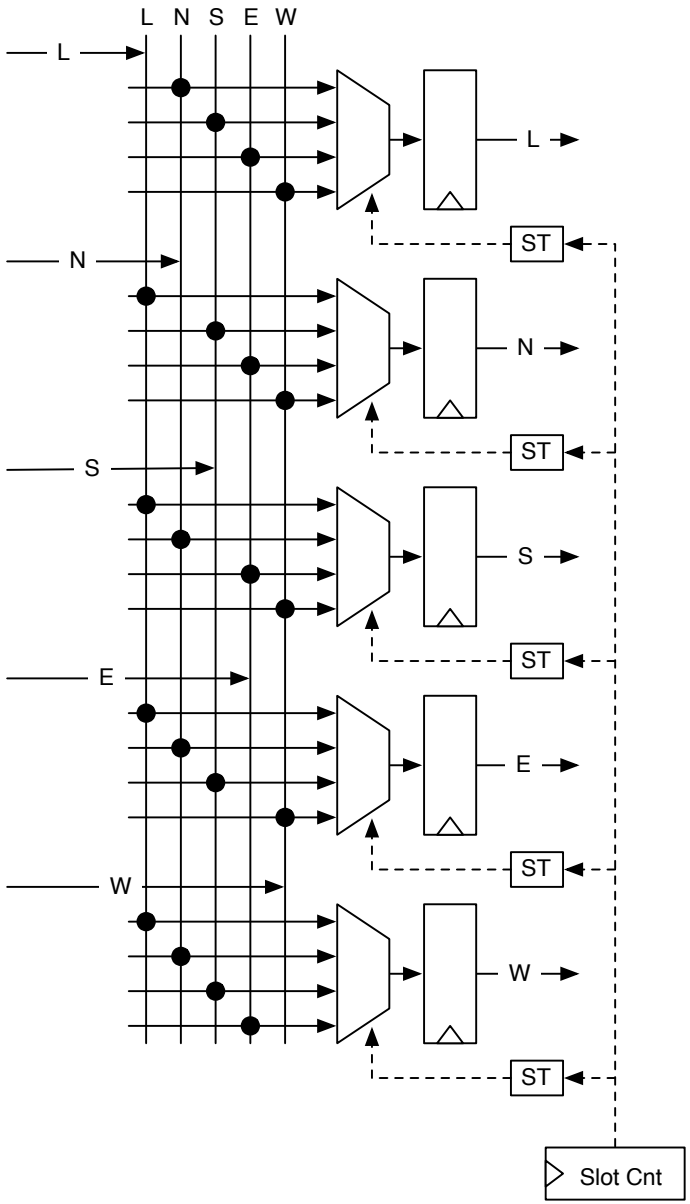
Heuristic scheduling

- Explore other network topologies
- Improve complexity of algorithm (tracking of conflicts)
- Relax some assumptions
  - worm-hole routing, ...

The S4 Router



- A a multiplexer and a register per out-going link
  - L connects the router to its node
  - N to the *north* neighbor
  - ...
- One in-coming/out-going link per direction
- Word-sized link width (e.g., 16 bits)
- Schedule table (ST) controls multiplexers