Fast Lossy Compression of 3D Unit Vector Sets.

Sylvain Rousseau
LTCI, Telecom ParisTech,
Paris-Saclay University

Tamy Boubekeur
LTCI, Telecom ParisTech,
Paris-Saclay University

Figure 1: 1: Unit vectors are grouped according to their spherical coordinates. 2: For each group (window), we apply a \textit{uniform mapping} that relocates subparts to the whole surface of the unit sphere. 3: To compress the vectors, we apply any existing unit vector quantization with an improved precision.

ABSTRACT
We propose a new efficient ray compression method to be used prior to transmission in a distributed Monte Carlo rendering engine. In particular, we introduce a new compression scheme for unorganized unit vector sets (ray directions) which, combined with state-of-the-art positional compression (ray origin), provides a significant gain in precision compared to classical ray quantization techniques. Given a ray set which directions lie in a subset of the Gauss sphere, our key idea consists in mapping it to the surface of the whole unit sphere, for which collaborative compression achieves a high signal-over-noise ratio. As a result, the rendering engine can distribute efficiently massive ray waves over large heterogeneous networks, with potentially low bandwidth. This opens a way toward Monte Carlo rendering in cloud computing, without the need to access specialized hardware such as rendering farms, to harvest the latent horsepower present in public institutions or companies.

CCS CONCEPTS
• Computing methodologies → Ray tracing;

KEYWORDS
Direction field compression, Unorganized normal vector set compression, Ray wave compression

ACM Reference format:

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than the author(s) must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from permissions@acm.org.

SA ’17 Technical Briefs, November 27–30, 2017, Bangkok, Thailand © 2017 Copyright held by the owner/author(s). Publication rights licensed to Association for Computing Machinery.
ACM ISBN 978-1-4503-5406-6/17/11 ... $15.00
https://doi.org/10.1145/3145749.3149436

1 INTRODUCTION
Over the last decade, Monte Carlo rendering has become the de facto standard in high quality visual special effects and computer animation productions [Christensen and Jarosz 2016]. This is mostly due to its physical basis, its robustness and the large number of effects accounted for by the single primitive encompassed in such methods: path tracing. In the mean time, the resolution of the generated images and the typical complexity of the input 3D scene – including geometry, materials and lighting conditions – have continuously increased. To address this ever-growing demand on computational horsepower, distributed Monte Carlo rendering engines appear as a promising solution, in particular when, beyond tile-rendering on the final image sensor, the 3D scene itself is distributed among the nodes of a computing cluster. To do so, at rendering time, the collection of rays that compose the sensor-scene-light paths are sent to each compute node to determine whether intersections occur with each node-specific region of the scene [Kato and Saito 2002; Northam et al. 2013]. As Monte Carlo path tracing provides a reasonable approximation of the rendering equation only at the price of a high amount of such rays, data i.e., ray sets exchange quickly becomes the main bottleneck of the entire image synthesis process, even with high bandwidth. Similarly, others methods such as distributed Photon mapping need to send a high amount of rays (photons) between nodes and are penalized by available bandwidth [Günther and Grosch 2014].

To solve this problem, one can use on-the-fly compression algorithms such as LZ4 [Collet 2011], a popular on-the-fly compression method for general data. This algorithm is lossless and extremely fast, but provides only a low compression ratio (up to 2). Moreover, this dictionary-based algorithm does not work with floating point data e.g., ray position and direction in our scenario. To cope with this problem, Lindstrom [2014] introduced a specific compression scheme for general floating point data, which turns out to be efficient to compress the origins of the rays, but whose generality prevents high compression ratios on the ray directions, with their particular unit nature. Indeed, several quantization methods have been developed to efficiently compress such data. Cigolle et
we encode the unit vectors of each window by quantization, storing the input for our algorithm is a set of unit vectors i.e., the directions based on their Gauss sphere parametrization. More precisely, the step of our algorithm reorders the vector set by grouping them be partially exploited for our grouping step. Therefore, the first rendering, the order in which rays are sent is not relevant, which offers them based on their Gauss sphere parametrization to form win- maps to quantize ray directions in a constant time. In particular, our algorithm uses the coherence between groups of unit vectors to improve the precision of all unit vectors quantization techniques.

2 ALGORITHM

2.1 Overview

The input for our algorithm is a set of unit vectors i.e., the directions of a set of rays. In the first step (Sec. 2.2), we start by reordering them based on their Gauss sphere parametrization to form windows (groups) of spatially coherent vectors. These windows delimit subparts of the unit sphere and are mapped to the whole surface of the unit sphere using the mapping introduced in Sec. 2.3, which preserves a uniform distribution to minimize the maximal error. Then, we encode the unit vectors of each window by quantization, storing the windows with the pattern defined in Sec. 2.5. The output of the algorithm is made of both the array of compressed windows and the array containing position indices of the vectors in the original unit vector array. Since, in our target application, the order of rays is not relevant during the interactions with the scene, this second array will be kept by the master node of the cluster and used to register the returned data in the correct path.

2.2 Grouping

Our compression algorithm for unit vector sets draws inspiration from methods exploiting small windows (groups) of data to encode samples as offsets w.r.t. the window average. In the context of rendering, the order in which rays are sent is not relevant, which offers us an opportunity to reorganize them in a spatially coherent way to maximize window sizes. Note that some rendering engines already sort the rays during rendering [Eisenacher et al. 2013], which can be partially exploited for our grouping step. Therefore, the first step of our algorithm reorders the vector set by grouping them based on their Gauss sphere parametrization. More precisely, the grouping is done by building windows of vectors sharing the same N most significant bits in the Morton code of their discretized spherical coordinates. Figure 2 shows a color coded representation of this grouping. Here, the induced linear complexity in the number of vectors motivates our choice against alternatives. In particular, the clustering quality could be improved using spherical Fibonacci point sets. However, this would significantly increase compression time, while we aim at providing on-the-fly data compaction. Moreover, this grouping gives us an easy way to compute the average vector from any vector contained inside of the window. All vectors in a window share the same N most significant bits that we call the key of the window. The Morton code of the average value of the window is equal to key + ((~ mask)/4) with mask being the value with its N most significant bits set to 1 and the others set to 0. With this grouping strategy, odd values of N give more uniform windows and should be favored because of step effect.

2.3 Uniform Mapping

Our on-the-fly compression scheme is entirely based on a specific quantization process. The best quantization to minimize the maximal error in the case of an unknown distribution is a uniformly distributed point set over the space in which the data is defined. The error is defined by the angle between the original and the decompressed unit vector. However, in practice, the range of directions associated with a local set of rays spans only a region of the Gauss sphere. Therefore, we propose to use a uniform mapping, from a region of the surface to the whole surface of the unit sphere.

In Fig. 3, we define the notations that we use. We also define $S_{cap}$, the surface of the spherical cap i.e., the region of the sphere defined by all the points that form an angle with a given vector which is smaller than a given threshold $\Theta$. In the following, we refer to the average unit vector as the vector at the center of the surface of the window.

$$
\frac{dS_1}{S_{sphere}} = \frac{dS_2}{S_{cap}}
$$

We want to find a mapping such as:

$$
\frac{dS_1}{S_{sphere}} = \frac{dS_2}{S_{cap}}
$$

Therefore, we propose to use a uniform mapping, from a region of the surface to the whole surface of the unit sphere.

In Fig. 3, we define the notations that we use. We also define $S_{cap}$, the surface of the spherical cap i.e., the region of the sphere defined by all the points that form an angle with a given vector which is smaller than a given threshold $\Theta$. In the following, we refer to the average unit vector as the vector at the center of the surface of the window.

$$
\frac{dS_1}{S_{sphere}} = \frac{dS_2}{S_{cap}}
$$

Therefore, we propose to use a uniform mapping, from a region of the surface to the whole surface of the unit sphere.

In Fig. 3, we define the notations that we use. We also define $S_{cap}$, the surface of the spherical cap i.e., the region of the sphere defined by all the points that form an angle with a given vector which is smaller than a given threshold $\Theta$. In the following, we refer to the average unit vector as the vector at the center of the surface of the window.

$$
\frac{dS_1}{S_{sphere}} = \frac{dS_2}{S_{cap}}
$$

Therefore, we propose to use a uniform mapping, from a region of the surface to the whole surface of the unit sphere.

In Fig. 3, we define the notations that we use. We also define $S_{cap}$, the surface of the spherical cap i.e., the region of the sphere defined by all the points that form an angle with a given vector which is smaller than a given threshold $\Theta$. In the following, we refer to the average unit vector as the vector at the center of the surface of the window.
The density can be rewritten as:

\[
\frac{dS_1}{S_{sphere}} = \frac{2\pi r^2 \sin \theta_1 d\theta_1}{4\pi r^2} = \frac{\sin \theta_1 d\theta_1}{2} \quad (4)
\]

\[
\frac{dS_2}{S_{cap}} = \frac{2\pi r^2 \sin \theta_2 d\theta_2}{2\pi r^2 (1 - \cos \Theta)} = \frac{\sin \theta_2 d\theta_2}{1 - \cos \Theta} \quad (5)
\]

We seek \( h : \theta_1 \to \theta_2 \), a mapping function. Using Eq. 3:

\[
\sin \theta_2 d\theta_2 = \frac{1 - \cos \Theta}{2} \sin \theta_1 d\theta_1 \quad (6)
\]

\[
-d(\cos \theta_2) = \frac{1 - \cos \Theta}{2}(-d(\cos \theta_1)) \quad (7)
\]

\[
\cos \theta_2 = \frac{1 - \cos \Theta}{2} \cos \theta_1 + c \quad (8)
\]

We define \( h(0) = 0 \), a unit vector equal to the average that will be mapped to itself. We obtain:

\[
c = 1 - \frac{1 - \cos \Theta}{2} \quad (9)
\]

Then, we can compute \( \theta_2 \) with \( \theta_1 \):

\[
\cos \theta_2 = 1 + \frac{1 - \cos \Theta}{2} (\cos \theta_1 - 1) \quad (10)
\]

\[
\theta_2 = \arccos \left( 1 - \frac{1 - \cos \Theta}{2} (1 - \cos \theta_1) \right) \quad (11)
\]

Eq. 11 gives us the mapping from \( \theta_1 \) to \( \theta_2 \) as illustrated in Fig. 3. This can be written as:

\[
h(\theta_1) = \arccos \left( 1 - \frac{1 - \cos \Theta}{k} \right) \quad (12)
\]

The inverse function for decompression has the following form:

\[
h^{-1}(\theta_2) = \arccos(1 - k(1 - \cos \theta_2)) \quad (13)
\]

Interestingly, as we can see in Eq. 13, the exact same mapping function is used for compression and decompression, using \( k \) for compression and \( \frac{1}{k} \) for decompression.

With \( h \) providing a mapping from an angle to another angle, we can apply this mapping to the unit vector directly. Let \( x \) be the original unit vector, \( x' \) the mapped one and \( P_0 \) the normalized average vector. Let’s define:

\[
l_0 = \arccos < P_0, x > \quad (14)
\]

\[
l_1 = h(l_0) \quad (15)
\]

\[
= \arccos \left( 1 - \frac{1 - < P_0, x >}{k} \right) \quad (16)
\]

We define \( P_1 \), a vector orthogonal to \( P_0 \) in the same plane as \( x \):

\[
P_1 \equiv \frac{x - < x, P_0 > P_0}{\|x - < x, P_0 > P_0\|} \quad (17)
\]

Using \( P_0 \) and \( P_1 \) as axes, \( x' \) is defined as:

\[
x' = \cos(l_1)P_0 + \sin(l_1)P_1 \quad (18)
\]

which gives us the mapping from a point \( x \) to a point \( x' \):

\[
x' = cP_0 + \sqrt{1 - c^2P_1} \quad (19)
\]

This mapping can be easily implemented (List. 1). Its use on hemispherical Fibonacci point set is shown in Fig. 4.
Table 1: The grouping is done using 13 bits. Lin, oct and sf are respectively the method of Lindstrom [2014], the octahedral quantization [Meyer et al. 2010] and the Spherical Fibonacci point set quantization. The number after the name of the method corresponds to the number of bits used for quantization. With Lin, the per-scalar rate was set to 10 and the vectors were sorted according to the Morton code of their discretized spherical coordinates prior to compression.

<table>
<thead>
<tr>
<th>Method</th>
<th>Compression with mapping (sec)</th>
<th>Decompression with mapping (sec)</th>
<th>Mean error (°)</th>
<th>Max error (°) with mapping</th>
<th>Mean error (°) with mapping</th>
<th>Max error (°) with mapping</th>
<th>Compression Ratio with mapping (except for Lin30)</th>
</tr>
</thead>
<tbody>
<tr>
<td>oct16</td>
<td>0.42</td>
<td>0.26</td>
<td>0.3370</td>
<td>0.9510</td>
<td>0.0029</td>
<td>0.0016</td>
<td>5.99019</td>
</tr>
<tr>
<td>sf16</td>
<td>1.39</td>
<td>0.48</td>
<td>0.3030</td>
<td>0.5895</td>
<td>0.0029</td>
<td>0.0016</td>
<td>5.99019</td>
</tr>
<tr>
<td>oct22</td>
<td>0.42</td>
<td>0.26</td>
<td>0.0418</td>
<td>0.1180</td>
<td>0.0031</td>
<td>0.0012</td>
<td>4.35893</td>
</tr>
<tr>
<td>sf22</td>
<td>1.39</td>
<td>0.48</td>
<td>0.0378</td>
<td>0.0700</td>
<td>0.0028</td>
<td>0.0012</td>
<td>4.35893</td>
</tr>
<tr>
<td>Lin30</td>
<td>5.249</td>
<td>4.83</td>
<td>0.0575</td>
<td>1.04</td>
<td>-</td>
<td>-</td>
<td>2.4</td>
</tr>
</tbody>
</table>

Figure 5: Windows compression pattern. \(N_i\) (resp. \(C_i\)) is the number of compressed unit vectors (resp. the compressed vectors) in the \(i^{th}\) window.

3 IMPLEMENTATION AND RESULTS

3.1 Speed and Error

Our error measure is the angle, in degrees, between the original vector and the compressed vector once decompressed. We evaluate the precision with the maximal and the mean error where the maximal is the largest error of the 10 million compressed vectors and the mean error is the average of these errors. As shown in Tab. 1, the method proposed by Lindstrom [2014] does not perform as well as classical quantization methods on unit vectors. This can be explained by the fact that this method was designed to handle a wide variety of floating point data, and does not use the properties of unit vectors. The lossless compression LZ4 applied to our data fails to compress as it was not designed to compress floating point data. In terms of performance, our uniform mapping (without quantization) can process 995 MB/s, and the grouping of the vectors takes 1.3 seconds. A smaller amount of windows reduces the grouping timing. Many different quantization methods exist and we choose to show the result of our mapping applied to two popular ones. The spherical Fibonacci point sets offer the best quantization with both the minimal mean and max error, while the octahedral quantization offers a good tradeoff between precision and encoding/decoding time. In terms of memory, the overhead for encoding a compressed window is 32 bits. Using a 13 bits grouping with 10 million vectors implies an overhead of 0.03 bits per encoded unit vector. If fewer vectors need to be compressed, the amount of bits used for division should be decreased. More results are provided as supplemental materials.

On shown results, our mapping reduce the mean error by a factor around 13 and the maximal error by a factor between 8.5 and 10.5. The highlighted cells show that using both Spherical Fibonacci point set or Octahedral quantization on 16 bits combined with our mapping function gives better mean and max error than the quantization without mapping using 22 bits. In this example, the use of our method increases the compression ratio from 4.36 to 5.99 with an improved accuracy.

4 CONCLUSION AND FUTURE WORK

We have presented a technique for on-the-fly compression of a set of unorganized unit vectors which, combined with state-of-the-art positional compression, can be used to compress rays in the pipeline of a distributed Monte Carlo renderer with lower compression error. The computational cost of the improved compression ratio is small in addition to classical quantization techniques and can be even reduced when used in a rendering engine that already sorts rays such as Hyperion [Eisenacher et al. 2013]. In the future, a better grouping could be designed to provide groups which shapes are close to spherical caps on the Gauss Sphere. Our algorithm could also be adapted to other kinds of data using unit vectors, e.g., compression of surfels or normal maps. We also plan to evaluate it in the context of a production renderer.

ACKNOWLEDGMENTS

This work was partially supported by the French National Research Agency (ANR) under grant ANR 16-LCV2-0009-01 ALLEGRO, by BPI France under grant PAPAYA and by the DGA We thank Ubisoft Motion Picture for their feedback.

REFERENCES


