### Replicated State Machines and Paxos



#### SLR210, P4, 2019

# Quiz 1

- Argue that the GLA algorithm (prev. lecture) is live
- Show that a set in which updates return boolean responses (depending on the operation's success) cannot be wait-free implemented from GLA

# How to build a consistent and reliable system?

Service accepts requests from clients and returns responses

- Liveness: every persistent client receives a response
- Safety: responses constitute a total order w.r.t. the service's sequential specification

(recall universal construction)





#### How to build a fault-tolerant system?

#### **Replication:**

- Service = collection of servers
- Some servers may fail





### "CAP theorem" [Brewer 2000]

No system can combine:

- Consistency: all servers observe the same evolution of the system state
- Availability: every client's request is eventually served

 Partition-tolerance: the system operates despite a partial failure or loss of communication

# Strongly consistent replicated state machine

Universal construction in message-passing:

- Clients access the service via a standard interface
- Servers run replicas of the (sequential) service
- (A subset of) faulty servers do not affect consistency and availability

Leslie Lamport: The Part-Time Parliament. ACM Trans. Comput. Syst. 16(2): 133-169 (1998)

# Paxos: some history

- Late 80s: a three-phase consensus algorithm
  - ✓ A Greek parliament reaching agreement
- 1989: a Paxos-based faulttolerant distributed database
- 1990: rejected from TOCS

"All three referees said that the paper was mildly interesting, though not very important, but that all the Paxos stuff had to be removed."



This submission was recently discovered behind a filing cabinet in the TOCS editorial office. Despite its age, the editor-in-chief felt that it was worth publishing. Because the author is currently doing field work in the Greek isles and cannot be reached, I was asked to prepare it for publication.

The author appears to be an archeologist with only a passing interest in computer science. This is unfortunate; even though the obscure ancient Paxon civilization he describes is of little interest to most computer scientists, its legislative system is an excellent model for how to implement a distributed computer system in an asynchronous environment.

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Keith Marzullo

University of California, San Diego (preface for the TOCS 1998 paper)

# Paxos today

 Underlies a large number of practical system when strong consistency is needed

- ✓ Google Megastore, Google Spanner
- ✓Yahoo Zookeeper
- ✓ Microsoft Azure
- ✓ ....
- •ACM SIGOPS Hall of Fame Award in 2012
- Turing award 2019

#### Consensus: recall the definition

A process *proposes* an *input* value in V (IVI≥2) and tries to *decide* on an *output* value in V

- *Agreement:* No two process decide on different values
- Validity: Every decided value is a proposed value
- Termination: No process takes infinitely many steps without deciding

(Every correct process decides)

Cannot be solved in an asynchronous read-write sharedmemory system with at least one faulty process (extends to 1-resilient message-passing systems)

# Circumventing impossibility: commit-adopt

A variant of consensus with weaker safety (relaxed agreement)

Can be used for solving consensus with an oracle

A process p<sub>i</sub> *proposes* an *input* value in V (IVI≥2) and *decides* on a tuple (c,v) where c is a boolean and v is in V

✓We say p<sub>i</sub> adopts v

✓ If c=true, we say  $p_i$  *commits* on v

#### **Commit-adopt: properties**

- Validity: Every adopted value is an input value of some process
- Termination: Every correct process decides
- CA-Agreement:
  - ✓ If a process commits on a value v, then no process can adopt a value v' ≠v

✓ If all inputs are the same, then no process decides on (false,\*)

(every process that decides commits on a value)

#### Commit-adopt : protocol

#### Shared objects:

N atomic registers A[0,...,N-1], initially T N atomic registers B[0,...,N-1], initially T

#### Upon propose(v) by process p<sub>i</sub>:

```
\begin{array}{l} \mathsf{v}_i \coloneqq \mathsf{v} \\ \mathsf{A}[i] \coloneqq \mathsf{v}_i \\ \mathsf{V} \coloneqq \mathsf{read} \ \mathsf{A}[0, \ldots, \mathsf{N}\text{-}1] \\ \text{if all non-T values in V are v then} \\ & \mathsf{B}[i] \coloneqq (\mathsf{true}, \mathsf{vi}) \\ \text{else} \\ & \mathsf{B}[i] \coloneqq (\mathsf{false}, \mathsf{vi}) \\ \mathsf{V} \coloneqq \mathsf{read} \ \mathsf{B}[0, \ldots, \mathsf{N}\text{-}1] \\ \text{if all non-T values in V are } (\mathsf{true}, *) \text{ then} \\ & \mathsf{return} \ (\mathsf{true}, \mathsf{v}_i) \\ \text{else if V contains } (\mathsf{true}, \mathsf{v}) \text{ then} \\ & \mathsf{v}_i \coloneqq \mathsf{v} \\ & \mathsf{return} \ (\mathsf{false}, \mathsf{v}_i) \end{array}
```

#### Commit-adopt: proof

Validity and Termination: immediate

CA-Agreement:

Claim 1 B[0,...,N-1] never contains (true,v) and (true,v') where v≠v'

Suppose not: p<sub>i</sub> wrote (true,v) in B[i] and pj wrote (true,v') in B[j], v≠v' Previously, p<sub>i</sub> wrote v in A[i] and pj wrote v' in A[j] (let pi be the first to write) But p<sub>i</sub> should have seen A[i] ≠v' - a contradiction! Commit-adopt: proof (contd.)

**Claim 2** If  $p_i$  returns (true,v) then no process pj returns (c,v') where  $v \neq v'$ 

Suppose not: let p<sub>j</sub> return (c,v') where v≠v'. By Claim 1, p<sub>j</sub> has previously written some (false,v'') in B[j]

- Since p<sub>j</sub> hasn't adopted v, it hasn't found (true,v) in B[1,...,N]
- But then p<sub>i</sub> should have read (false,v'') in B[j] a contradiction!

#### Commit-adopt: proof (contd.)

**Claim 3** If all inputs are the same then no process returns (false,\*)

Immediate: both "if" conditions are true, i.e., the non-T values in A and B are the same

### $\Omega$ : an oracle

- Eventual leader failure detector
- Produces (at every process) events:
  - $\checkmark < \Omega$ , leader, p>

✓We also write p=leader()

 Eventually, all correct processes output the same correct process as the leader

# Can be implemented in eventually synchronous system:

- There is a bound on communication delays and processing that holds only eventually
- ✓There is an a priori unknown bound in every run

#### Leader election Ω: example

There is a time after which the same correct process is considered leader by everyone.

(Sufficient to output a binary flag leader/not leader)



#### Consensus = $\Omega$ + CA

#### Shared:

D[1,..., $\infty$ ], regular registers, initially T CA<sub>1</sub>,CA<sub>2</sub>,... a series of commit-adopt instances

#### Upon propose(v) by process p<sub>i</sub>:

```
V_i := V
r := 0
repeat forever
    r++
    (C,V_i) := CA_r(V_i)
                                           // r-th instance of commit-adopt
    if c=true then
                 D[r]:=v<sub>i</sub>
                                           // let the others learn your value
                 return v<sub>i</sub>
    repeat
                 if \Omega outputs p_i then
                      D[r]:= vi // advertise your value if leader
    until D[r]=v' where v' \neq T
                                                      //wait until the leader writes its value
    V_i := V'
                                           //adopt the leader's value
```

#### Quiz 2: commit-adopt

- Would the CA algorithm is correct if regular registers were used?
- Show that Ω + CA indeed solve consensus
- Give an obstruction-free consensus algorithm using CA
  - ✓ Obstruction-freedom: every process that runs solo from some point on eventually decides

# Back to message-passing

- Asynchronous system
- Reliable communication channels
- Processes fail by crashing
- A majority of correct processes

But we proved that 1-resilient consensus is impossible even with shared memory! "CAP theorem" is violated! Where is the trick?

# Paxos/Synod algorithm

- Let's try to decouple liveness (termination) from safety (agreement)
- Synod made out of two components:
   ✓Ω the eventual leader oracle
   ✓(ofcons) obstruction-free consensus

#### **Obstruction-free Consensus (ofcons)**

- Similar to consensus
  - ✓ except for Termination

 $\checkmark$  ability to abort and propose again

Requests:

✓ <ofcons, propose, v> (propose v)

Responses:

✓ <ofcons,decide, v'> (decide v')

✓ <ofcons,abort > (aborts)

# **Obstruction-free Consensus**

• C1. Validity:

✓Any value decided is a value proposed

• C2. Agreement:

✓No two correct processes decide differently

- C3. Obstruction-Free Termination:
  - ✓ If a correct process p proposes, it eventually decides or aborts.
  - ✓ If a correct process decides, no correct process aborts infinitely often.
  - ✓ If there is a time after which a single correct process p proposes a value sufficiently many times, p eventually decides.

### Consensus vs. OF-Consensus





#### 







# Consensus using $\Omega$ and ofcons

- Straightforward
  - ✓ Assume that in cons everybody proposes

```
upon (cons, propose, v)
while not(decided)
    if self=leader() then
    result = ofcons.propose(v)
    if result=(decide,v') then
        return v'
```

# Link to Paxos/Synod

 External cons.propose events come in a state machine replication algorithm as requests from clients

 $\checkmark As$  in universal construction

Focus now on implementing OFCons

# OFCons

- Not subject to FLP impossibility!
- Can be implemented in fully asynchronous system
  - ✓ Using the correct-majority assumption

✓Or read-write

Synod OFCons: a 2-phase algorithm

# Synod OFCons I

```
Code of every process pi:
```

```
Initially:
    ballot:=i-n; proposal:=nil; readballot:=0; imposeballot:=i-n;
    estimate:= nil; states:=[nil,0]<sup>n</sup>
```

```
upon (ofcons, propose, v)
proposal := v; ballot:=ballot + n; states:=[nil,0]<sup>n</sup>
send [READ, ballot] to all
```

```
upon receive [READ,ballot'] from p<sub>j</sub>
if readballot ≥ ballot' or imposeballot ≥ ballot' then
send [ABORT, ballot'] to pj
else
```

```
readballot:=ballot'
send [GATHER, ballot', imposeballot, estimate] to pj
```

```
upon receive [ABORT, ballot] from some process
```

```
return abort
```

# Synod OFCons II

upon receive [GATHER, ballot, estballot, est] from pj
states[pj]:=[est,estballot]

```
upon #states ≥ majority //collected a majority of responses
  if \exists states[pk]=[est,estballot] with estballot>0 then
      select states[pk]=(est,estballot) with highest
  estballot
     proposal:=est;
  states:=[nil,0]<sup>n</sup>
  send [IMPOSE, ballot, proposal] to all
upon receive [IMPOSE, ballot', v] from p<sub>i</sub>
   if readballot > ballot' or imposeballot > ballot' then
           send [ABORT, ballot'] to pi
  else
```

```
estimate := v; imposeballot:=ballot'
send [ACK, ballot'] to p<sub>i</sub>
```

# Synod OFCons III

upon received [ACK, ballot] from majority
send [DECIDE, proposal] to all

upon receive [DECIDE, v]

send [DECIDE, v] to all
return [decide, v]

### Correctness

- Validity
   ✓Immediate
- Agreement

 $\checkmark$  When is the decided value determined?

#### OF Termination

- ✓ Show that a correct process that proposes either decides or aborts
- ✓ If a single process keeps proposing?

### **Time Complexity**

- Fault-free time complexity: 4 message delays
  - + 1 communication step for decision relaible broadcast
- Optimizations

 $\checkmark$  Getting rid of the first READ phase

 Allow a single process (presumed leader, say p1) to skip the READ phase in its 1<sup>st</sup> ballot
 ✓ Reduces fault-free/sync time complexity to 2

#### From Synod to Paxos

- Paxos is a state-machine replication (SMR) protocol

   i.e., a universal construction given a sequential object
- Implemented as totally-ordered broadcast: exports one operation toBroadcast(m) and issues toDeliver(m') notifications

#### Paxos SMR

- Clients initiate requests
- Servers run consensus
  - ✓ Multiple instances of consensus (Synod)
  - ✓ Synod instance 25 used to agree on the 25<sup>th</sup> request to be ordered
- Both clients and servers have the (unreliable) estimate of the current leader (some server)
- Clients send requests to the leader
- The leader replies to the client

#### Paxos failure-free/sync message flow



## Observation

 READ phase involves no updates/new consensus proposals

✓ Makes the leader catch up with what happened before

Most of the time the leader will remain the same

+ nothing happened before (e.g., new requests)

# Optimization

- Run READ phase only when the leader changes
   ✓ and for multiple Synod instances simultaneously
- Use the same ballot number for all future Synod instances

✓run only IMPOSE phases in future instances

- ✓ Each message includes ballot number (from the last READ phase) and ReqNum, e.g., ReqNum = 11 when we're trying to agree what the 11<sup>th</sup> operation should be
- When a process increments a ballot number it also READs

 $\checkmark$ e.g., when leader changes

#### Paxos Failure-Free Message Flow



#### Paxos:

(universal) state machine replication

Replicated service:

- Collection of servers
- Some servers may fail
- Liveness: every persistent client receives a response
- Safety: responses constitute a total order w.r.t. the service's sequential specification

(linearizability)





# Atomic broadcast: Abstract ordering service

Interface:

- call broadcast(m)
- callback *deliver(m)*

Properties:

- Validity: if a correct process invokes broadcast(m), then eventually every correct process executes deliver(m)
- No duplication: for a given m, a process executes deliver(m) at most once
- No creation: if a process executes delivers(m), then some process previously executed broadcast(m)
- Total order: if a process delivers m and then m', then no process delivers m' before m

# Quiz 3

- Prove that Synod satisfies Agreement and OF-termination
- Show that Atomic Broadcast is equivalent to State Machine Replication (SMR):
  - Any SMR algorithm can be used to implement Atomic Broadcast
  - ✓Any Atomic Broadcast algorithm can be used to implement SMR