Comparison of optical feedback dynamics of InAs/GaAs quantum-dot lasers emitting solely on ground or excited states

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Received 9 November 2017; revised 5 December 2017; accepted 5 December 2017; posted 6 December 2017 (Doc. ID 312950); published 4 January 2018

We experimentally compare the dynamics of InAs/GaAs quantum dot lasers under optical feedback emitting exclusively on ground states (GSs) or excited states (ESs). By varying the feedback parameters and putting focus either on their short or long cavity regions, various P and chaotic oscillatory states are found. The GS laser is shown to be more resistant to feedback, benefiting from its strong relaxation oscillation damping. In contrast, the ES laser can easily be driven into complex dynamics. While the GS laser is of importance for the development of isolator-free transmitters, the ES laser is essential for applications taking advantages of chaos.

OCIS codes: (140.5960) Semiconductor lasers; (050.2230) Fabry-Perot; (160.4236) Nanomaterials; (190.0190) Nonlinear optics.

https://doi.org/10.1364/OL.43.000210

Nonlinear dynamics of quantum-well (QW) semiconductor lasers subject to optical feedback has been studied extensively. By controlling the feedback parameters, various dynamical states such as P, quasi-periodic, and chaotic oscillation states and their routes to chaos (C) have been investigated [1,2]. Self-pulsating dynamics, including RPP, chaotic-like pulsations, and low-frequency fluctuating states in transition from short cavity regions (SCRs) to long cavity regions (LCR) has been analyzed and reported [3–7].

Compared to QW lasers, quantum-dot (QD) lasers have many advantages such as small linewidth enhancement factor [8,9], temperature insensitivity [10], low transparency current [11], and low relative intensity noise [12] benefiting from the three-dimensional carrier confinement [13]. Although the modulation capabilities of QD lasers operating on the ground state (GS) are limited to a few gigahertz at room temperature, except for advanced tunneling structures, large signal operation at 20 Gbit/s was reported [14,15]. Not surprisingly, QD lasers operating on the excited state (ES) show higher differential gain, smaller nonlinear gain compression [13,16], and broader modulation bandwidths with smaller K-factors [17]. Modulation capabilities up to 25 Gbps on-off keying and 35 Gbps pulse-amplitude modulation for high-speed transmitters have been successfully demonstrated for a 1.3 μm InAs/GaAs QD laser emitting on the ES [13,14,16]. Moreover, near-zero linewidth enhancement factors in ES lasers for chirp-free transmitters have been reported [18].

To understand the nonlinear dynamics of QD lasers under the influence of optical feedback, the feedback sensitivity of QD lasers has been investigated [19,20]. The strong damping of relaxation oscillations in GS lasers is thought to be responsible for insensitivity to optical feedback, which has been demonstrated. Anti-phase dynamics in the GS and ES with π/2 phase shift has been reported [21]. Switching behavior corresponding to the variation of the modal gain when changing the feedback has been discussed [22]. For QD mode-locked lasers, significant stability deterioration at a certain critical level of optical feedback has been demonstrated [23], as well as a regime of extreme stability [24].

While feedback dynamics of QD lasers emitting on different lasing states has been discussed, most investigations were focused on the LCR [25]. To extend and complete the exploration of the feedback dynamics of QD lasers in the SCR, we study and compare here the dynamics of QD lasers in both the SCR and the LCR. For lasers emitting exclusively on the GS or ES, the feedback characteristics of each emission can be investigated independently. By varying the feedback strength and the external cavity length, various states such as periodic (P), regular pulse package (RPP), frequency-locking (FL), quasi-regular pulsing (QRP), quasi-chaos pulse package (QCPP), and C states are found. The GS laser is shown to be more resistant to the perturbation by feedback, benefiting from its large...
damping rate. In contrast, the ES laser can easily be driven into complex dynamics, including the $C$ states.

Figure 1 shows the schematic setup of the QD laser subject to optical feedback. The dynamical characteristics of two Fabry–Perot multimode QD lasers, one emitting exclusively on the GS and one on the ES, are investigated and compared under different operation and feedback conditions. The active regions of both lasers are composed of 10 InAs dot sheets grown in InGaAs QWs by molecular beam epitaxy (MBE) with a dot-in-well structure [26]. The dot densities are around $3 \times 5 \times 10^{10}$ cm$^{-2}$ per layer, and their lateral extensions approach 30 nm. Both laser types have internal cavities of 1 mm long and 2 μm waveguides etched through the active area. The output of the laser towards the left is fed back to the laser cavity through a partially reflecting mirror to form an external cavity with length $L_{\text{ext}}$ adjustable from 2 to 50 cm. The boundary separating the SCR and the LCR is defined by the ratio between the frequency of the external cavity $f_{\text{ext}}$ and the relaxation oscillation frequency $f_{\text{RO}}$, where $f_{\text{ext}}/f_{\text{RO}} > 1$ belongs to the SCR and $f_{\text{ext}}/f_{\text{RO}} < 1$ is the LCR. A variable optical attenuator is used to adjust the feedback strength $\xi_f$ defined as the ratio of the feedback field to the laser output field. The optical signals are analyzed by an optical spectrum analyzer (Advantest Q8384, 10 pm resolution), and the optical power is measured by a power meter. The electrical signals are detected by two identical high-speed photodetectors (Newport 1544-A, 12 GHz bandwidth) and analyzed by an electrical spectrum analyzer (RKS FSV30, 30 GHz bandwidth) and a real-time oscilloscope (Tektronix TDS 6604, 6 GHz bandwidth, 20 GS/s).

Figures 2(a) and 2(b) show the optical spectra of the GS and ES lasers on a semi-logarithmic scale in free-running conditions. For better comparison, both lasers are biased at 1.5 times their threshold currents ($I_{\text{th}} = 16$ mA for the GS and $I_{\text{th}} = 93$ mA for the ES lasers). The center wavelengths of the GS and ES lasers are 1301.5 and 1227.0 nm, and their $f_{\text{RO}}$ are 2.1 and 1.3 GHz, respectively. The corresponding boundaries of the SCR and the LCR for the GS and ES lasers are at $L_{\text{ext}}$ of 7.3 and 11.5 cm, respectively. As can be seen from the spectra, the GS laser emits exclusively on the GS without the presence of the ES, and the ES laser emits exclusively on the ES without the presence of the GS. By applying feedback to these lasers, the dynamical states associated with each emission line are individually investigated.

Figure 3 shows the time series and the corresponding power spectra of the dynamical states from the GS laser in the SCR and the LCR. In the SCR at $L_{\text{ext}} = 30$ mm, an RPP state is demonstrated in Figs. 3(a) and 3(b) for $\xi_f = 0.826$. Different from the RPP state described in [3] for QW lasers showing a fast oscillation frequency $f_{\text{SO}}$ coinciding with $f_{\text{ext}}$, the RPP state observed has $f_{\text{SO}}$ around $f_{\text{RO}} = 3$ GHz instead.

Moreover, the slow oscillation has a frequency $f_{\text{SO}} = 72$ MHz that is much lower than both $f_{\text{ext}}$ and $f_{\text{RO}}$. Compared to the RPP states reported in [3] with less than 10 oscillations in each package, more than 40 oscillations are packed in the RPP states reported in [3] with less than 10 oscillations in each package. When $\xi_f$ decreases to 0.731, the laser becomes more stable, and a $P$ state oscillating at $f_{\text{RO}}$, as shown in Figs. 3(c) and 3(d), is found. In the LCR at $L_{\text{ext}} = 100$ mm, an FL state [27] is obtained for $\xi_f = 0.634$. As shown in Figs. 3(e) and 3(f), $f_{\text{SO}}$ locks to $f_{\text{RO}}$ with a rotation number of 1:2. When $L_{\text{ext}}$ increases to 200 mm, an FL state with a rotation number of 1:4 is also found. Note that $f_{\text{RO}}$ here is increased to about 3 GHz from its free-running value due to the change of the threshold by the feedback [28]. The GS laser subject to feedback is relatively stable such that no $C$ state can be found, even with the strongest feedback attainable in this setup.

Figure 4 shows the time series and corresponding power spectra of the dynamical states from the ES laser in the SCR and the LCR. In the SCR, at $L_{\text{ext}} = 20$ mm and with a strong feedback of $\xi_f = 0.703$, a $C$ state with irregular intensity modulation and a spectrum broader from the noise floor is shown in Figs. 4(a) and 4(b). When $\xi_f$ decreases to 0.686, a QCPS state is found and shown in Figs. 4(c) and 4(d). Different from an RPP state that has a fast oscillation at $f_{\text{ext}}$ [3],
the fast oscillation of this QCPP oscillates at $f_{\text{RO}}$. The $f_{\text{SO}}$ is not coincident with either $f_{\text{RO}}$ or $f_{\text{ext}}$, but occurs with a frequency of 340 MHz. Moreover, unlike the spectra of typical RPP states that have frequency components of only fast or slow oscillations and their corresponding harmonics and beats, the spectrum of the QCPP state preserves the broadband characteristics as present in the $C$ state. When $\xi_f$ further decreases to 0.48, as shown in Figs. 4(e) and 4(f), a $P$ state stably oscillating at $f_{\text{FO}} = 4$ GHz is obtained. Increasing $L_{\text{ext}}$ to 200 mm into the LCR, a $C$ state with a time delay signature corresponding to $f_{\text{ext}}$ is obtained at $\xi_f = 0.703$, as shown in Figs. 4(g) and 4(h). When $\xi_f$ decreases to 0.267, a QRP state with periodic drops in intensity, as shown in Figs. 4(i) and 4(j), is found. Unlike typical regular pulsing states that oscillate at a frequency corresponding to $f_{\text{RO}}$, the QRP states oscillate at frequencies coincident with $f_{\text{ext}}$.

Compared to the GS laser which, in general, is stable and insensitive to feedback, the ES laser is more easily moving to complex dynamics. While a GS laser is of large importance for the development of isolator-free transmitters in short-reach networks, an ES laser on the other hand can be essential for applications taking advantages of $C$ such as $C$ lidars, $C$ radars, and high-speed random number generations [29–31].

Figures 5(a) shows $f_{\text{SO}}$ extracted from the RPP states of the GS laser and the QCPP states of the ES laser in their SCRs under different $f_{\text{ext}}$. As can be seen, while $f_{\text{SO}}$ does not coincide exactly with either $f_{\text{RO}}$ or $f_{\text{ext}}$, $f_{\text{SO}}$ in both states increases linearly as $f_{\text{ext}}$ increases. Figure 5(b) shows the $f_{\text{SO}}$ extracted from the QRP states under different $f_{\text{ext}}$ in the LCR of the ES laser. As can be seen, $f_{\text{SO}}$ coincides well with $f_{\text{ext}}$ in the QRP states. The slight discrepancy is attributed to the overestimation in $f_{\text{ext}}$, where the internal laser cavity and the refractive index of optics were neglected when measuring $L_{\text{ext}}$.

Figures 6(a)–6(d) show mappings of the dynamical states of the GS and ES lasers under different feedback conditions at $1.5 \times I_{\text{th}}$ and $1.75 \times I_{\text{th}}$, respectively. The red dashed lines depict the boundaries between the SCR and the LCR. As can be seen in Fig. 6(a), at $1.5 \times I_{\text{th}}$, the GS laser oscillates in FL states when $\xi_f$ exceeds 0.3 in the LCR. In the SCR, the laser enters $P$, and then RPP states as $\xi_f$ increases. At a larger bias current of $1.75 \times I_{\text{th}}$, as shown in Fig. 6(b), the GS laser becomes even more stable where the region of the steady states (S) expanded and $\xi_f$ needed for the laser to excite instability increases. Note that the laser is more sensitive to the feedback phase in the SCR than in the LCR. As can be seen, the edge of the $S$ region humps higher in $\xi_f$ (more stable) when the laser is constructively interfered with one of its external cavity modes [28,32].

![Fig. 5](image.png)

![Fig. 6](image.png)
For the ES laser at $1.5 \times I_{th}$, as shown in Fig. 6(c), it enters QRP, and then $C$ states as $\xi_f$ increase in the LCR. In the SCR, $P$ and QCPP states are found before the laser enters $C$ states. Note that complex dynamics, especially $C$ states are only found in the ES laser, but not in the GS laser, even for the highest $\xi_f$ attainable in this setup. Moreover, when the bias current increases to $1.75 \times I_{th}$, as shown in Fig. 6(d), the ES laser is easily excitable and can enter $C$ states with a relatively lower $\xi_f$.

From these results, it is obvious that, although the GS and ES lasers have the same active medium, their response to the feedback is very different. Unlike the ES laser, the carrier dynamics of the GS laser involves transport, capture, and relaxation, leading to a larger damping rate $\gamma_D$ that stabilizes the laser and prevents the development of complex dynamics. As reported in [25], $\gamma_D$ of 18 GHz is estimated for this GS laser, while it is only 0.6 GHz for the ES laser. Moreover, the ES laser has a stronger modal competition [25] which also makes it easier to be driven into instabilities.

We investigated the dynamical states and their spectral characteristics of multimode optical feedback QD lasers emitting exclusively on the GS or the ES in both the SCR and LCR. Although these GS and ES lasers are made from the same active medium, their feedback dynamics is found to be very different. The GS laser is shown to be more resistant to feedback, especially at a higher bias level, attributed to its large damping rate. No $C$ states can be found with the attainable feedback parameters in this Letter. $P$ and RPP states are observed in the SCR, and FL states are found in the LCR. Compared to the RPP states reported previously in QW lasers that typically have less than 10 oscillations in a pulse package, the RPP states from the GS laser are densely packed with more than 40 oscillations. Moreover, the fast oscillation frequencies are found to be no longer coincident with $f_{ext}$, but with $f_{RO}$.

The ES laser, in contrast, is shown to be easily excitable and can enter $C$ states with a relatively lower $\xi_f$, especially at a higher bias level. In the SCR, $P$, QCPP, and then $C$ states emerge as $\xi_f$ increases and, in the LCR, $C$ states are developed after QRP states. While the $f_{SC}$ for RPP and QCPP are much lower than both $f_{ext}$ and $f_{RO}$, they are shown to be governed and increase linearly with $f_{ext}$. While the more stable GS laser can be important for the development of isolator-free transmitters benefiting from its great resistance against feedback, the ES laser, on the other hand, is suitable for applications taking advantages of $C$ such as $C$ lidars, $C$ radars, and high-speed random bit generations. Feedback dynamics of InAs/GaAs distributed feedback QD lasers [33] will be investigated in our future work.

**Funding.** Ministry of Science and Technology, Taiwan (MOST) (103-2112-M-007-019-MY3, 105-2911-I-007-501); Campus France (PhC Orchid No. 33721SC); Institut Mines Télécîm (IMT) (the Futurs & Ruptures Program).

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