# Optical Noise of Dual-State Lasing Quantum Dot Lasers

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*Abstract*—This paper theoretically investigates the optical noise characteristics of the simultaneous ground-state (GS) and excited-state (ES) lasing quantum dot lasers. The optical noise dynamics of both states are analysed through coupling the Langevin noise sources into a set of coupled rate equations. It is pointed out that the ES emission significantly changes the evolution scenario of the relative intensity noise, the frequency noise (spectral linewidth), and the linewidth broadening factor of the GS emission, as a function of the bias current. In the vicinity of the ES lasing threshold, the relative intensity noise and the frequency noise of the GS emission is lower than those of ES emission. However, the linewidth broadening factor of the GS emission is larger than the latter.

*Index Terms*—Semiconductor lasers, quantum dots, relative intensity noise, frequency noise, spectral linewidth, linewidth broadening factor.

#### I. INTRODUCTION

Quantum dot (QD) lasers are silicon-compatible laser sources for developing photonic integrated circuits (PICs), which is witnessing rapid growth driven by the increasing demands for 5G infrastructures, high speed optical interconnects in data centers and LIDAR for self-driving automobiles [1], [2]. Thanks to the low sensitivity of QDs to the epitaxial growth defects [3], [4], the steady-state performances of QD lasers epitaxially grown on silicon are becoming comparable to their counterparts grown on the native GaAs or InP substrate, including the low threshold current density and the high temperature stability [3]–[6]. QD lasers also exhibit low optical noise characteristics, including both relative intensity noise (RIN) and frequency noise (FN) [7]–[10]. It has been shown that the RIN of QD lasers reached down to -160 dB/Hz [7], [11], [12], and the record spectral linewidth was as low as

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60 kHz [8]. In addition, QD lasers are highly tolerant to optical feedback, owing to the large damping factor and/or small linewidth broadening factor (LBF) [10], [13], [14], which are significantly beneficial for isolator-free integration in silicon-based PICs.

In addition to the usual ground-state (GS) emission, QD lasers can also emit solely on the excited state (ES), or simultaneously on both states [15]-[19]. The ES-lasing QD lasers usually exhibit higher modulation bandwidth than that of GS-lasing ones, owing to the faster carrier relaxation rate and higher differential gain [16], [17], [20], [21]. In addition, the ES emission shows a smaller LBF than the GS emission [21], [22]. However, the ES-lasing QD lasers are found to be more sensitive to the optical feedback due to the smaller damping rate [22], [23]. On the other hand, dual-state lasing in QD lasers enhances the modulation bandwidth as well [19], [24]. Interestingly, dual-state laser emission exhibits lower intensity noise than sole GS or ES emission, which is attributed to the quasi-antiphase dynamics through the carrier relaxation process. [25]. Optical feedback usually triggers mode switching or mode competition between the GS and the ES [26], [27], while feedback with finely controlled phase is helpful to reduce the RIN of two-state lasing QD laser [28]. However, the QD laser operated at the ES lasing threshold is very sensitive to the optical feedback [29]. Recently, Xiong and Zhang theoretically proved that the the phonon bottleneck effect and the inhomogenous broadening effect play crucial roles on the dual-state lasing behavior [30].

In this work, we theoretically investigate the optical noise characteristics of InAs/InP QD lasers emitting simultaneously on the GS and the ES. We present a dual-state lasing QD rate equation model including all the Langevin noise sources. Increasing the bias current generally reduces the RIN and the spectral linewidth of the GS emission, except at the ES lasing threshold. However, the ES emission is found to significantly change the evolution scenario of the GS emission noise, with respect to the bias current. We also analyze the optical noise characteristics of ES emission, which show monotonic reduction with increasing bias currents. It is shown that in the vicinity of the ES lasing threshold, the optical noise of ES emission is higher than that of GS emission. Finally, through the analysis of FN spectra, we obtain LBFs of the GS emission and the ES emission, respectively. Below the ES lasing threshold, raising the bias current increases the LBF of the GS emission. Above the ES lasing threshold, however,

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Fig. 1. The schematic of carrier dynamics in a QD laser.

the LBF of the GS emission is reduced while the LBF of the ES emission is almost constant. The paper is organized as follows: In Section II, we introduce the rate equation model of dual-state lasing InAs/InP QD lasers, as well as its linearized form in the frequency domain. Section III discusses the dualsate lasing characteristics including the RIN, the FN, and the LBF. Section IV summarizes this work.

## II. RATE EQUATION MODEL OF DUAL-STATE LASING QD LASERS

Figure 1 illustrates the schematic of the carrier dynamics in QD lasers [21], [31]. It is assumed that the active region consists of only one ensemble, that is, all the QDs have the same size. Therefore, the inhomogeneous effect due to the dot size dispersion is not considered in this work. The QD laser is simplified as a three-level system: a two-dimensional carrier reservoir (RS), a four-fold degenerate ES, and a twofold degenerate GS, where the electron-hole pairs are treated as neutral excitons. Carriers are injected directly from the electrodes to the RS, followed by a capture process into the ES with a capture time  $\tau_{GS}^{RS}$ . Finally, carriers relax into the GS with a relaxation time  $\tau_{GS}^{RS}$ . It is noted that the direct carrier capture process from the RS to the GS is neglected, which otherwise can accelerate the carrier scattering rate to the GS [32]. However, the incorporation of the direct carrier capture channel will not affect the conclusion of this work. On the other hand, due to the thermal excitation, some carriers are excited from the GS to the ES with a time  $\tau_{ES}^{GS}$ , and from the ES to the RS with a time  $\tau_{RS}^{ES}$ , respectively. Carriers in all the three states recombine spontaneously with times  $\tau_{RS,ES,GS}^{spon}$ , respectively. Both the GS and the ES exhibit stimulated emission simultaneously. Dynamics of the carrier numbers  $N_{RS,ES,GS}$ , the photon numbers  $S_{ES,GS}$ , and the phases of the two electric fields  $\phi_{ES,GS}$  are expressed as:

$$\frac{dN_{RS}}{dt} = \frac{I}{q} + \frac{N_{ES}}{\tau_{RS}^{ES}} - \frac{N_{RS}}{\tau_{ES}^{RS}}(1 - \rho_{ES}) - \frac{N_{RS}}{\tau_{RS}^{spon}} + F_{RS} \quad (1)$$

$$\frac{dN_{ES}}{dt} = \left(\frac{N_{RS}}{\tau_{ES}^{RS}} + \frac{N_{GS}}{\tau_{ES}^{GS}}\right)(1 - \rho_{ES}) - \frac{N_{ES}}{\tau_{GS}^{ES}}(1 - \rho_{GS}) - \frac{N_{ES}}{\tau_{RS}^{ES}} - \Gamma_p v_g g_{ES} S_{ES} - \frac{N_{ES}}{\tau_{ES}^{spon}} + F_{ES}$$
(2)

$$\frac{dN_{GS}}{dt} = \frac{N_{ES}}{\tau_{GS}^{ES}} (1 - \rho_{GS}) - \frac{N_{GS}}{\tau_{ES}^{GS}} (1 - \rho_{ES}) - \Gamma_p v_g g_{GS} S_{GS} - \frac{N_{GS}}{\tau_{GS}^{spon}} + F_{GS}$$
(3)

$$\frac{dS_{ES}}{dt} = \left(\Gamma_p \upsilon_g g_{ES} - \frac{1}{\tau_p}\right) S_{ES} + \beta_{sp} \frac{N_{ES}}{\tau_{ES}^{spon}} + F_{S_{ES}} \tag{4}$$

$$\frac{dS_{GS}}{dt} = \left(\Gamma_p v_g g_{GS} - \frac{1}{\tau_p}\right) S_{GS} + \beta_{sp} \frac{N_{GS}}{\tau_{GS}^{spon}} + F_{S_{GS}} \tag{5}$$

$$\frac{d\phi_{ES}}{dt} = \frac{1}{2}\Gamma_p v_g (g_{GS}\kappa_{ES}^{GS} + g_{ES}\alpha_{ES} + g_{RS}\kappa_{ES}^{RS}) + F_{\phi_{ES}}$$
(6)

$$\frac{d\phi_{GS}}{dt} = \frac{1}{2}\Gamma_p v_g (g_{GS}\alpha_{GS} + g_{ES}\kappa_{GS}^{ES} + g_{RS}\kappa_{GS}^{RS}) + F_{\phi_{GS}}$$
(7)

where *I* is the injected current, *q* is the elementary charge, and  $\rho_{ES,GS}$  are the carrier occupation probabilities in each state [33].  $\tau_p$  is the photon lifetime,  $\Gamma_p$  is the optical confinement factor,  $\beta_{Sp}$  is the spontaneous emission factor, and  $v_g$  is the group velocity of the light.  $\alpha_{ES,GS}$ are self-contributions of the carrier population in the ES, GS to the LBF of ES, GS, respectively.  $\kappa_{ES}^{RS,GS}$  are crosscontributions of carrier population in the RS, GS to the LBF of ES, respectively.  $\kappa_{GS}^{RS,ES}$  are cross-contributions of carrier population in the RS, ES to the LBF of GS, respectively.  $g_{ES,GS}$  are material gains of each state, which are expressed as [33]:

$$g_{ES} = \frac{a_{ES}}{1 + \xi_{ES} \frac{S_{ES}}{V_S}} \frac{N_B}{V_B} (2\rho_{ES} - 1)$$
(8)

$$g_{GS} = \frac{a_{GS}}{1 + \xi_{GS} \frac{S_{GS}}{V_S}} \frac{N_B}{V_B} (2\rho_{GS} - 1)$$
(9)

where  $a_{ES,GS}$  are the differential gains, and  $\xi_{ES,GS}$  are the gain compression factors of each state.  $N_B$  is the total number of QDs,  $V_B$  is the volume of the active region, and  $V_S$  is the volume occupied by the photons in the laser cavity.  $g_{RS}$  is the RS gain [33].

The carrier noise and the spontaneous emission noise are characterized by the Langevin approach [34].  $F_{RS,ES,GS}$  are the carrier noise sources in each state.  $F_{S_{ES,GS}}$  are the photon noise sources of spontaneous emission, and  $F_{\phi_{ES,GS}}$  are the phase noise sources of spontaneous emission. Both the carrier noise and the spontaneous emission noise are white noise, and hence the expectation values of all the above Langevin noise sources are zero. The auto- and cross-correlations of all the noise sources are given by:

$$\langle F_i(t)F_i(t')\rangle = U_{i,j}\delta(t-t') \tag{10}$$

where *i*, *j* are representing *RS*, *ES*, *GS*, *S<sub>ES</sub>*, *S<sub>GS</sub>*,  $\phi_{ES}$ , and  $\phi_{GS}$ . The correlation coefficients  $U_{i,j}$  are derived using the classical method described in [34], and non-zero coefficients are given by (11)-(18):

$$U_{RS,RS} = 2 \times \left[ \frac{N_{RS}}{\tau_{ES}^{RS}} (1 - \rho_{ES}) + \frac{N_{RS}}{\tau_{RS}^{spon}} \right]$$
(11)

$$U_{ES,ES} = 2 \times \left[ \left( \frac{N_{RS}}{\tau_{ES}^{RS}} + \frac{N_{GS}}{\tau_{ES}^{GS}} (1 - \rho_{ES}) - \Gamma_p v_g g_{ES} S_{ES} + \beta_{sp} \frac{N_{ES}}{\tau_{ES}^{spon}} S_{ES} \right]$$
(12)

$$U_{GS,GS} = 2 \times \left[ \frac{N_{ES}}{\tau_{GS}^{ES}} (1 - \rho_{GS}) - \Gamma_p v_g g_{GS} S_{GS} + \beta_{sp} \frac{N_{GS}}{\tau_{GS}^{spon}} S_{GS} \right]$$
(13)

$$U_{S_{ES(GS)},S_{ES(GS)}} = 2 \times \beta_{sp} \frac{N_{ES(GS)}}{\tau_{ES(GS)}^{spon}} S_{ES(GS)}$$
(14)

$$U_{\phi_{ES(GS)},\phi_{ES(GS)}} = \frac{1}{2S_{ES(GS)}} \beta_{sp} \frac{N_{ES(GS)}}{\tau_{ES(GS)}^{spon}}$$
(15)

$$U_{RS,ES} = -\left[\frac{N_{RS}}{\tau_{ES}^{RS}}(1-\rho_{ES}) + \frac{N_{ES}}{\tau_{RS}^{ES}}\right]$$
(16)

$$\begin{split} \gamma_{11} &= \frac{1 - \rho_{ES}}{\tau_{ES}^{RS}} + \frac{1}{\tau_{RS}^{spon}}; \gamma_{12} = \frac{1}{\tau_{RS}^{ES}} + \frac{1}{4N_B} \frac{N_{RS}}{\tau_{ES}^{RS}}; \\ \gamma_{21} &= \frac{1 - \rho_{ES}}{\tau_{ES}^{RS}}; \\ \gamma_{22} &= \frac{1 - \rho_{ES}}{\tau_{ES}^{RS}} + \frac{1}{\tau_{RS}^{ES}} + \frac{1}{\tau_{ES}^{spon}} + \frac{1}{4N_B} \left( \frac{N_{RS}}{\tau_{ES}^{RS}} + \frac{N_{GS}}{\tau_{ES}^{GS}} \right) \\ &\quad + \frac{1}{2} \Gamma_p v_g a_{ES} S_{ES}; \gamma_{23} = \frac{1 - \rho_{ES}}{\tau_{ES}^{GS}} + \frac{1}{2N_B} \frac{N_{ES}}{\tau_{ES}^{ES}}; \\ \gamma_{24} &= -\Gamma_p v_g g_{ES} + \Gamma_p v_g a_{p_{ES}} S_{ES}; \\ \gamma_{32} &= \frac{1 - \rho_{ES}}{\tau_{ES}^{ES}} + \frac{1}{4N_B} \frac{N_{GS}}{\tau_{ES}^{GS}}; \\ \gamma_{33} &= \frac{1 - \rho_{ES}}{\tau_{ES}^{ES}} + \frac{1}{4N_B} \frac{N_{GS}}{\tau_{ES}^{GS}}; \\ \gamma_{33} &= \frac{1 - \rho_{ES}}{\tau_{ES}^{GS}} + \frac{1}{\tau_{S}^{spon}} + \frac{1}{2N_B} \frac{N_{ES}}{\tau_{ES}^{ES}} + \Gamma_p v_g a_{GS} S_{GS}; \\ \gamma_{42} &= \frac{1}{2} \Gamma_p v_g a_{ES} S_{ES} + \frac{\beta_{sp}}{\tau_{ES}^{spon}}; \\ \gamma_{44} &= \frac{1}{\tau_p} - \Gamma_p v_g g_{ES} + \Gamma_p v_g a_{p_{ES}} S_{ES}; \\ \gamma_{53} &= \Gamma_p v_g a_{GS} S_{GS} + \frac{\beta_{sp}}{\tau_{GS}^{SG}}; \\ \gamma_{55} &= \frac{1}{\tau_p} - \Gamma_p v_g g_{GS} + \Gamma_p v_g a_{p_{ES}} S_{ES}; \\ \gamma_{61} &= \Gamma_p v_g a_{RS} \kappa_{ES}^{RS}; \gamma_{62} = \frac{1}{4} \Gamma_p v_g a_{ES} \alpha_{ES}; \\ \gamma_{63} &= \frac{1}{2} \Gamma_p v_g a_{GS} \kappa_{ES}^{GS}; \gamma_{71} = \Gamma_p v_g a_{RS} \kappa_{GS}^{RS}; \\ \gamma_{72} &= \frac{1}{4} \Gamma_p v_g a_{ES} \kappa_{GS}^{ES}; \gamma_{73} = \frac{1}{2} \Gamma_p v_g a_{GS} \alpha_{GS}; \\ \gamma_{74} &= -\frac{1}{2} \Gamma_p v_g a_{p_{ES}} \kappa_{GS}^{ES}; \gamma_{75} = -\frac{1}{2} \Gamma_p v_g a_{p_{GS}} \alpha_{GS}; \\ (20) \end{split}$$

Through standard small signal analysis of the rate equations (1)-(7), the linearized rate equations in the frequency domain is derived in (19) and the matrix components are expressed



Fig. 2. (a) Photon numbers emitted from the GS, the ES, and their summation. (b) Carrier numbers of GS, ES and RS as a function of the bias current.  $I_{th}^{GS} = 49$  mA,  $I_{th}^{ES} = 284$  mA.

in (20). In the small signal analysis, the gain compression effect is approximated by considering  $a_{PES,GS}$  with  $dg_{ES,GS} = a_{ES,GS}dN_{ES,GS} - a_{PES,GS}dS_{ES,GS}$  [34]. Applying Cramer's rule, small-signal variations of the carrier number  $\delta N$ , the photon number  $\delta S$ , and the phase  $\delta \phi$  can be obtained. The RIN and the FN of each lasing state are defined as:

$$RIN(\omega)_i = |\frac{\delta S_i(\omega)}{S_i}|^2$$
(21)

$$FN(\omega)_i = |\frac{j\omega}{2\pi}\delta\phi_i(\omega)|^2$$
(22)

with *i* being ES and GS,  $\omega$  being the angular frequency, *S* being the average photon number,  $\delta S(\omega)$  being the photon number variation, and  $\delta \phi(\omega)$  being the phase variation. The laser under study is an InAs/InP QD laser, and the laser parameters used for the simulations are listed in Table I [21], [31]. It is worthwhile to mention that the optical confinement factor is dependent on the QD density, the number of stacked QD layers, and the structure of cladding layer [35]–[37]. The value of the optical confinement factor used in the simulation is 0.06 [38].

## **III. RESULTS AND DISCUSSION**

Figure 2(a) depicts  $S_{GS}$ ,  $S_{ES}$ , and the total photon number  $S_{total}$  as a function of the bias current. The GS lasing threshold is  $I_{th}^{GS} = 49$  mA, and the ES one is  $I_{th}^{ES} = 284$  mA. Above the ES lasing threshold, the slope efficiency of the GS emission significantly decreases, which is smaller than that of the ES emission. On the other hand, the slope efficiency of the total laser emission slightly increases. This behavior is consistent

TABLE I MATERIAL AND OPTICAL PARAMETERS OF THE QD LASER

Symbol	Description	Value
$E_{RS}$	RS transition energy	0.97 eV
$E_{ES}$	ES transition energy	0.87 eV
$E_{GS}$	GS transition energy	0.82 eV
$ au_{ES}^{RS}$	RS to ES capture time	6.3 ps
$\tau_{GS}^{ES}$	ES to GS relaxation time	2.9 ps
$\tau_{RS}^{ES}$	ES to RS escape time	2.7 ns
$ au_{ES}^{GS}$	GS to ES escape time	10.4 ps
$ au_{RS}^{spon}$	RS spontaneous emission time	0.5 ns
$\tau_{ES}^{spon}$	ES spontaneous emission time	0.5 ns
$\tau_{GS}^{spon}$	GS spontaneous emission time	1.2 ns
$ au_p$	Photon lifetime	4.1 ps
$T_2$	Polarization dephasing time	0.1 ps
$\beta_{sp}$	Spontaneous emission factor	$5.0 \times 10^{-6}$
$a_{GS}$	GS Differential gain	$5.0 \times 10^{-15} \text{ cm}^2$
$a_{ES}$	ES Differential gain	$10{\times}10^{-15}~{ m cm}^2$
$\xi_{ES}$	ES Gain compression factor	$1.0 \times 10^{-15} \text{ cm}^3$
$\xi_{GS}$	GS Gain compression factor	$1.0 \times 10^{-15} \text{ cm}^3$
$\Gamma_p$	Optical confinement factor	0.06
$\alpha_{GS}$	intrinsic $\alpha$ -factor of GS	0.50
$\alpha_{ES}$	intrinsic $\alpha$ -factor of ES	0.50
$\kappa_{ES}^{RS}$	RS to ES contribution coefficient	0.059
$\kappa_{ES}^{GS}$	GS to ES contribution coefficient	-0.137
$\kappa^{RS}_{GS}$	RS to GS contribution coefficient	0.037
$\kappa^{ES}_{GS}$	ES to GS contribution coefficient	0.122
$N_B$	Total dot number	$1.0 \times 10^7$
$D_{RS}$	Total RS state number	$4.8 \times 10^{6}$
$V_B$	Active region volume	$5.0 \times 10^{-11} \text{ cm}^3$
$V_{RS}$	RS region volume	$1.0 \times 10^{-11} \text{ cm}^3$
R	Mirror reflectivity	0.32
$lpha_i$	Internal modal loss	$6.0 \ {\rm cm}^{-1}$
n	Refractive index	3.5
Ν	QD layer number	5
L	Cavity length	0.5 mm
W	Cavity width	$4.0 \ \mu m$

with the experimental observation in [32]. In Fig. 2(b), both  $N_{GS}$  and  $N_{ES}$  have clear kinks at both lasing thresholds.

The above-threshold  $N_{ES}$  is higher than the above-threshold  $N_{GS}$ , due to the larger degeneracy of the ES. Both carriers are not completely clamped but slightly increased with increasing bias current. This is due to the gain compression effect, which is characterized by the gain compression factor in (8) and (9). Increasing the photon number reduces the effective differential gain, and hence more carrier populations (or higher carrier occupation probabilities) are demanded to maintain a constant gain value, which is governed by the cavity loss [34]. On the other hand, the RS carrier number  $N_{RS}$  is much smaller than  $N_{GS}$  and  $N_{ES}$  for all the bias currents.

## A. Relative Intensity Noise Characteristics

Figure 3(a) shows the RIN of the GS emission ( $RIN_{GS}$ ) at several bias currents. Below the ES lasing threshold,  $RIN_{GS}$ shows a clear resonance peak, and the resonance frequency increases with the bias current as expectation. Meanwhile, increasing the bias current reduces the whole RIN spectrum. Above the ES lasing threshold, the resonance peak of  $RIN_{GS}$ is almost completely suppressed. The RIN evolution of the ES emission ( $RIN_{ES}$ ) in Fig. 3(b) is similar as  $RIN_{GS}$  below the ES lasing threshold. However, the resonance frequency of  $RIN_{ES}$  is about 3 times larger than the latter, which leads to the higher modulation bandwidth of the ES emission as observed in [16], [21].

Figure 4 depicts the low-frequency (at 1.0 MHz) RINs of both GS and ES emissions as a function of the bias current. Below the ES lasing threshold, RIN<sub>GS</sub> decreases rapidly from -126.3 dB/Hz at  $1.2 \times I_{th}^{GS}$  down to -154.9 dB/Hz at  $5.2 \times I_{th}^{GS}$ . However, at the ES lasing threshold, RIN<sub>GS</sub> abruptly increases to -149.4 dB/Hz. This significant increase of RIN<sub>GS</sub> is in agreement with the experimental observation in [25]. The high RIN<sub>GS</sub> can be attributed to the large optical power fluctuations induced by the strong spontaneous emission of the ES, due to the coupling of the GS and the ES through the carrier relaxation process [25]. Beyond the ES lasing threshold, RIN<sub>GS</sub> reduces slightly, and becomes almost constant around -155 dB/Hz. On the other hand, RIN<sub>ES</sub> significantly decreases from -135.4 dB/Hz at  $1.1 \times I_{th}^{ES}$  to -156.8 dB/Hz at  $2.0 \times I_{th}^{ES}$ .

$$U_{ES,GS} = -\begin{bmatrix} \frac{N_{GS}}{\tau_{ES}^{GS}} (1 - \rho_{ES}) + \frac{N_{ES}}{\tau_{GS}^{ES}} (1 - \rho_{GS}) \end{bmatrix}$$
(17)  

$$U_{ES(GS),S_{ES(GS)}} = -\begin{bmatrix} 2\beta_{sp} \frac{N_{ES(GS)}}{\tau_{ES(GS)}^{spon}} S_{ES(GS)} - \Gamma_{p} \upsilon_{g} g_{ES(GS)} S_{ES(GS)} \end{bmatrix}$$
(18)  

$$\begin{bmatrix} \gamma_{11} + j\omega - \gamma_{12} & 0 & 0 & 0 & 0 & 0 \\ -\gamma_{21} & \gamma_{22} + j\omega - \gamma_{23} & -\gamma_{24} & 0 & 0 & 0 \\ 0 & -\gamma_{42} & 0 & \gamma_{44} + j\omega & 0 & 0 & 0 \\ 0 & 0 & -\gamma_{53} & 0 & \gamma_{55} + j\omega & 0 & 0 \\ 0 & 0 & -\gamma_{53} & 0 & \gamma_{55} + j\omega & 0 & 0 \\ -\gamma_{61} & -\gamma_{62} & -\gamma_{63} & -\gamma_{64} & -\gamma_{65} & j\omega & 0 \\ -\gamma_{71} & -\gamma_{72} & -\gamma_{73} & -\gamma_{74} & -\gamma_{75} & 0 & j\omega \end{bmatrix} \times \begin{bmatrix} \delta N_{RS} \\ \delta N_{ES} \\ \delta N_{ES} \\ \delta S_{ES} \\ \delta \phi_{ES} \\ \delta \phi_{ES} \\ \delta \phi_{GS} \end{bmatrix} = \begin{bmatrix} F_{RS} \\ F_{S} \\ F_{S} \\ F_{S} \\ F_{\phi_{ES}} \\ F_{\phi_{GS}} \\ F_{\phi_{GS}} \end{bmatrix}$$
(19)



Fig. 3. RIN spectra of laser emitted from (a) the GS and (b) the ES at several bias currents.  $I_{tb}^{FS} \approx 5.8 \times I_{tb}^{GS}$ .



Fig. 4. Low-frequency RINs at 1 MHz of GS emission and ES emission as a function of the normalized bias current.

#### **B.** Frequency Noise Characteristics

Figure 5(a) shows that the FN of the GS emission (FN<sub>GS</sub>) generally decreases with increasing bias current, and the resonance peak is suppressed. However, at the ES lasing threshold, the low frequency part of FN<sub>GS</sub> is significantly increased, due to the high LBF described in Fig. 7. The FN of the ES emission (FN<sub>ES</sub>) in Fig. 5(b) shows similar evolution as FN<sub>GS</sub> below the ES lasing threshold.

From the low-frequency value of the FN spectrum, we obtain the intrinsic linewidth of semiconductor lasers through the simple relation  $\Delta v_{OL} = 2\pi F N|_{(f=1.0 \text{ MHz})}$ [33], [39]. The intrinsic linewidth is determined by both the



Fig. 5. FN spectra of laser emissions from (a) the GS and (b) the ES at several bias currents.  $I_{th}^{ES} \approx 5.8 \times I_{th}^{GS}$ .



Fig. 6. Intrinsic linewidths of GS emission and ES emission as a function of the normalized bias current.

spontaneous emission noise and the LBF [34]. It is noted that the rate equations do not take into account technical noise sources including current source noise, temperature fluctuation, and mechanical vibration, which can significantly raise the low-frequency FN. Figure 6 depicts that the intrinsic linewidth of the GS emission decreases from 6.7 MHz at  $1.2 \times I_{th}^{GS}$  down to 0.5 MHz at  $5.2 \times I_{th}^{GS}$ . At the ES lasing threshold, the intrinsic linewidth exhibits an abrupt increase to 2.0 MHz as the low-frequency RIN in Fig. 4. Above the ES lasing threshold, the intrinsic linewidth of the GS becomes almost constant around 0.26 MHz. Meanwhile, the intrinsic linewidth of the ES emission declines from 7.6 MHz at  $1.1 \times I_{th}^{ES}$  to 0.88 MHz at  $2.0 \times I_{th}^{ES}$ .



Fig. 7. LBFs of the GS and the ES as a function of the normalized bias current.

On the other hand, from the high-frequency value of the FN spectrum, the Schawlow-Townes linewidth of semiconductor lasers is extracted through  $\Delta v_{ST} = 2\pi F N|_{(f=100 \text{ GHz})}$ . The intrinsic linewidth  $\Delta v_{OL}$  of semiconductor lasers is broadened by the LBF from the Schawlow-Townes linewidth  $\Delta v_{ST}$  as

$$\Delta \nu_{OL} = \Delta \nu_{ST} (1 + \alpha^2) \tag{23}$$

Using the above formula, Fig. 7 extracts the LBFs of both the GS and the ES. Below the ES lasing threshold, the LBF of the GS increases from 0.7 at  $1.2 \times I_{th}^{GS}$  to 1.2 at  $5.2 \times I_{th}^{GS}$ , due to the increased contribution of carrier variations in the ES and in the RS [21], [33]. At the ES lasing threshold, the LBF dramatically increases to 2.9, due to the strong carrier perturbation induced by the onset of ES emission. This increased LBF results in the poor resistance to optical feedback at the ES lasing threshold, as experimentally observed in [29]. Interestingly, the LBF of the GS becomes declining for bias currents above the ES lasing threshold. This phenomenon is qualitatively in good agreement with the experimental observation in [40], where a giant LBF is observed around the ES threshold. The LBF reduction can be attributed to the stimulated emission of the ES, which stabilizes the carrier vibration induced by the spontaneous emission, because the stimulated emission consumes much more carriers than the spontaneous emission [41]. On the other hand, the LBF of the ES is almost constant around 0.57, which is slightly smaller than the LBF of the GS for the same bias current.

### IV. CONCLUSION

In summary, we propose a rate equation model of dualstate lasing InAs/InP QD lasers including the Langevin noise sources, which enables the investigation of RIN and FN dynamics. The RIN and the intrinsic linewidth of both GS emission and ES emission generally decrease with increasing bias current. However, at the ES lasing threshold, both the lowfrequency RIN and the linewidth of the GS emission abruptly increase. Beyond the ES lasing threshold, both become almost constant. In addition, it is found that the LBF of the GS increases with bias current below the ES lasing threshold, while becomes decreasing when it is above the ES threshold. Interestingly, the QD laser exhibits a giant LBF at the ES lasing threshold. On the other hand, the LBF of the ES is also almost constant, which is slightly smaller than the GS one. The findings in this work suggest that the ES emission in QD lasers hardly degrades the noise performance of the GS emission, except at the ES lasing threshold. Therefore, practical applications of QD lasers should avoid current operation in the vicinity of the ES threshold. Finally, although the simulations in this work are based on InAs/InP lasers, we believe that the conclusions are also suitable for InAs/GaAs dual-state emission QD lasers, which can be obtained by replacing the parameters in Table I with the InAs/GaAs ones.

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