

Master MVA

Analyse des signaux Audiofréquences
Audio Signal Analysis, Indexing and Transformation

Lecture on 3D sound rendering

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Sound rendering

- Introduction
- Some elements on spatial perception

- Multi-channel systems
 - **Stereophony**
 - **'Surround' systems**
 - **Ambisonics.**
 - **Wave-field synthesis.**

- Binaural techniques

- Applications



Introduction

- **Time-frequency** : **Sound**
 Space/time-frequency : **Sound field**

- **Rendering** : **definitions.**
 - Science
 - Sound engineering
 - Art

- **Rendering in practice** : **Recording**
 : **Synthesis**

- **Approaches** : **perceptual**
 : **physics based**



Brief historical overview of 3D sound rendering in music

(from A. Dutto: <http://www.nikkojazz.fr/2009/05/la-mise-en-espace-de-la-musique.html>)

■ Premices:

- 4th century: Antiphonia, e.g. alternating between 2 choirs
- 1573: motet with 40 voices from Thomas Tallis
- Double choirs then used by Vivaldi, Bach, ..

■ 19th century:

- **Berlioz's Requiem – Tuba Mirum (1837):**
 - Monumental orchestra + large choir + 4 groups of brass instruments at the four corner of the hall
 - Question ?: where should be positioned the listener ?

■ The 20th century: space exploitation

- **Maderna, Carter, Stockhausen, Xenakis...Boulez**

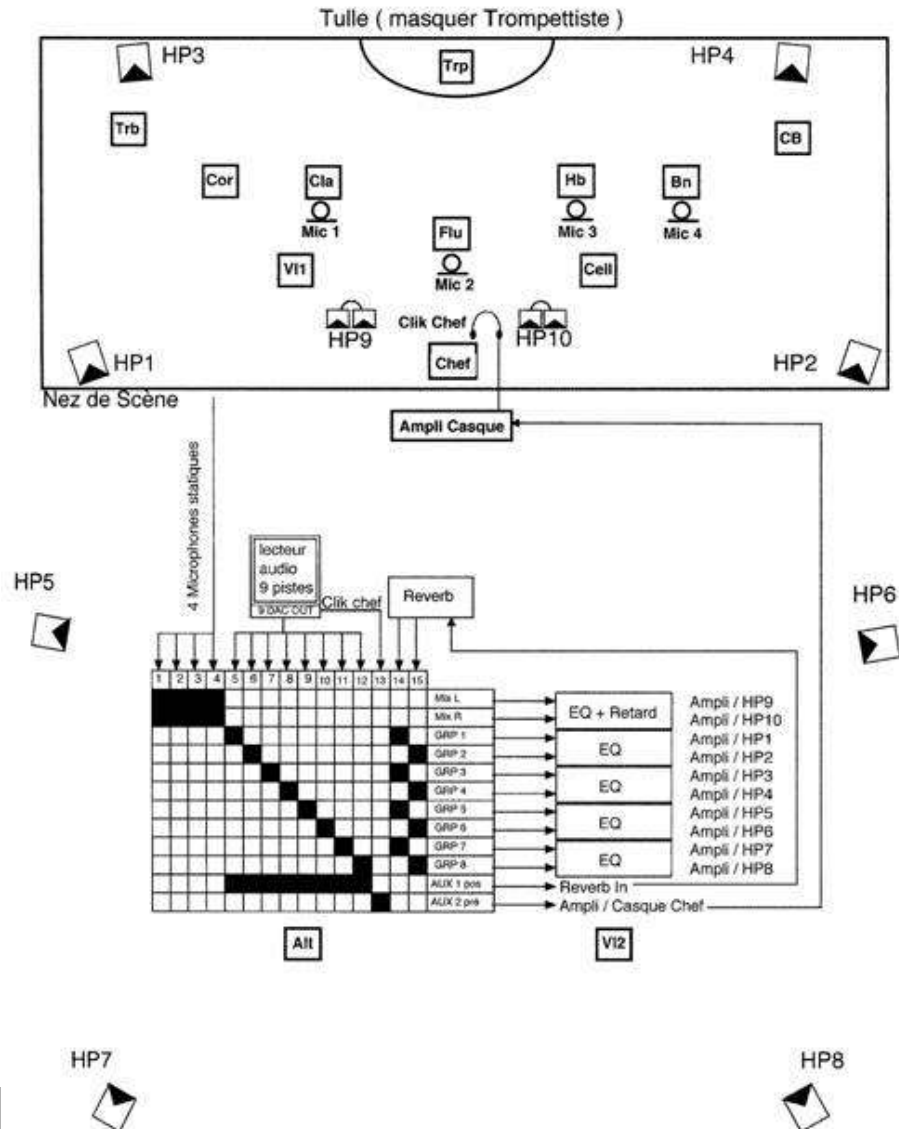


Brief historical overview ...

<http://www.nikkojazz.fr/2009/05/la-mise-en-espace-de-la-musique.html>

■ Another example : *Le plein du vide*, Xu Yi (1997)

- 8 computer tracks played on 8 loudspeakers placed on stage and in the public,
- Public is at the center



Rendering techniques

- **Physics based:** Sound field as a physical phenomenon
- **Perceptual :** Sound field as a perceived phenomenon
 - Important parameters: IID, ITD, IPD, HRTFs..
- **Multichannel** : group listening
 - Notion of sweet spot
- **Binaural** : individual listening
 - Optimal for headphone listening



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Some elements on spatial perception

■ 2 main aspects of perception of space:

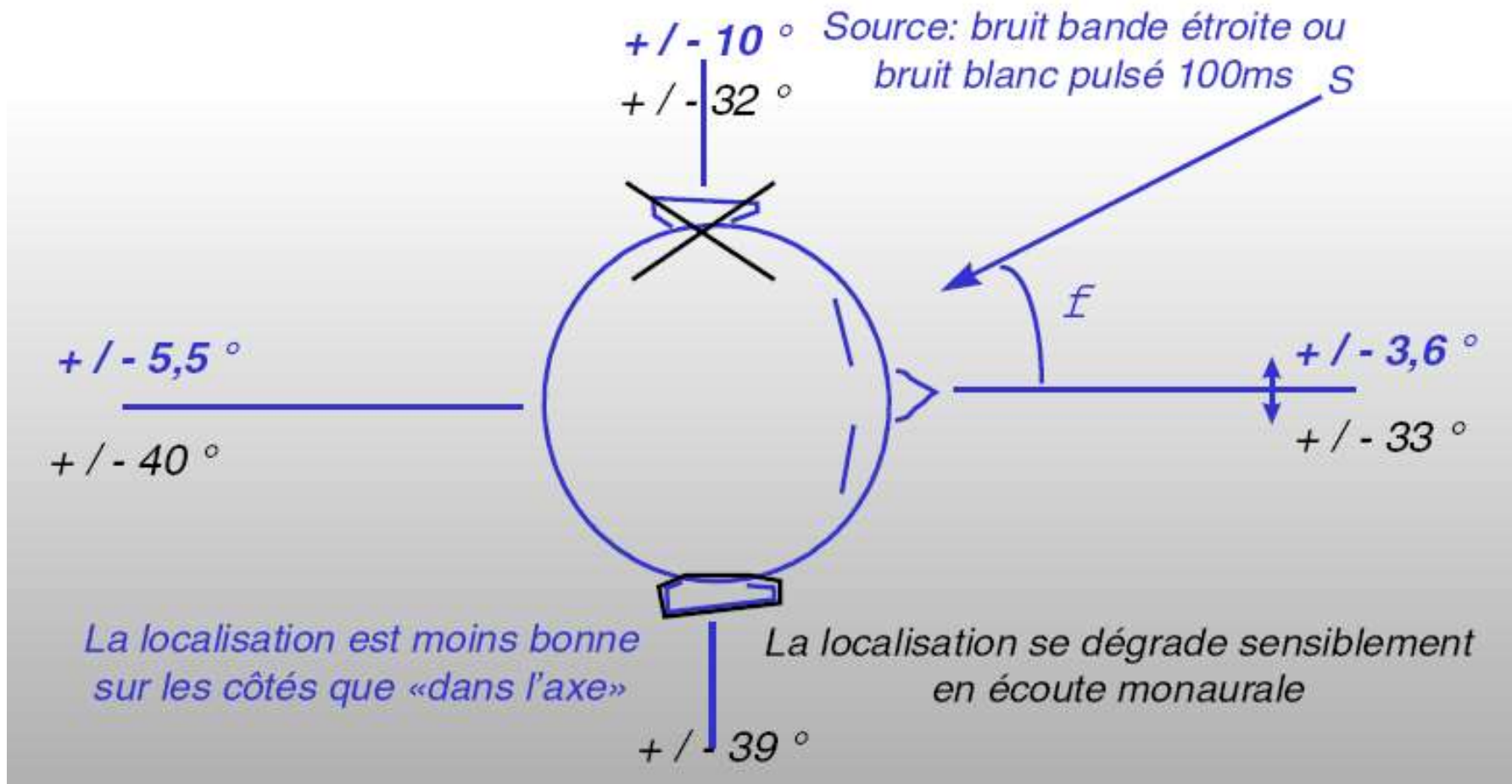
■ *Sound sources localisation*

- Remarkable human capacity for localising sounds (especially short impulsive sounds).
- We essentially use binaural indices but not only.
- Note that *localisation is not lateralisation* (with headphones, in this case sounds are “in” the head)

■ *Source subjective width*

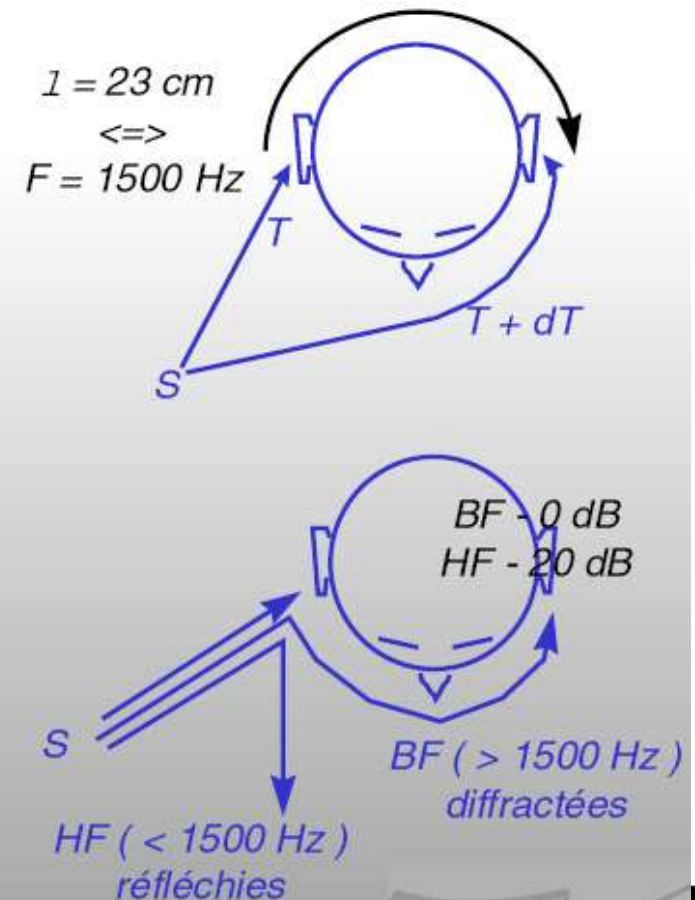


Sound localisation in azimuth



Sound localisation in azimuth

- **2 types of indices (Steven and Newman, 1936):**
 - Interaural Time Difference (ITD)
... Especially in low frequency
 - Interaural Intensity Difference (IID)
... Especially in high frequencies.
- **max. ambiguity ambigüité around 1500Hz**



Sound localisation in elevation

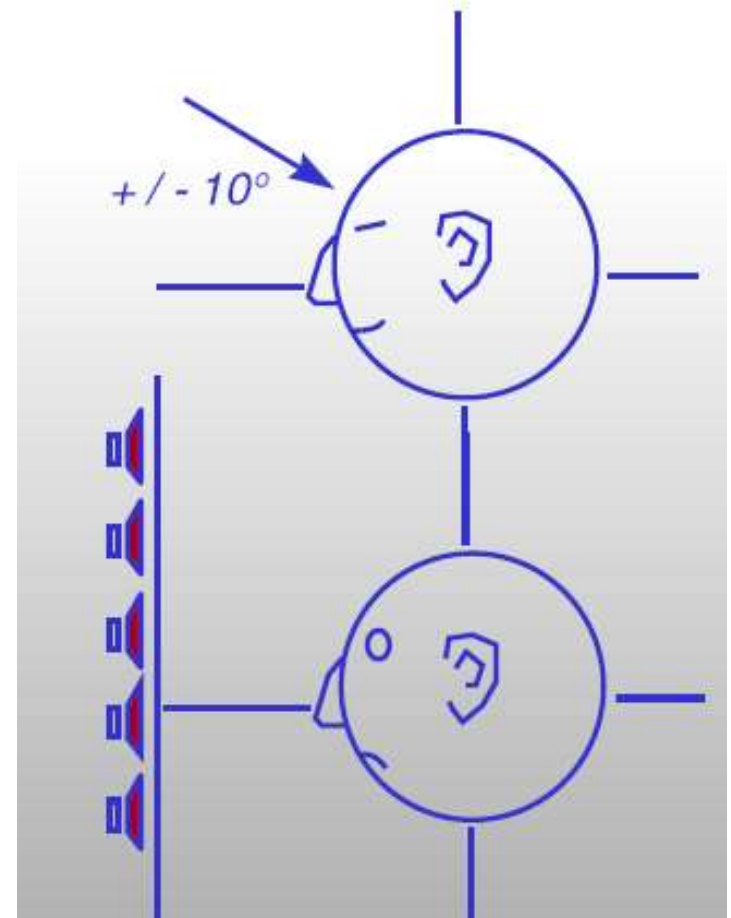
■ Speech sounds localisation:

- + or - 10° / sound in front,
- ~ less good / sound behind

■ Pur sounds : « localisation » is only depending on the frequency !

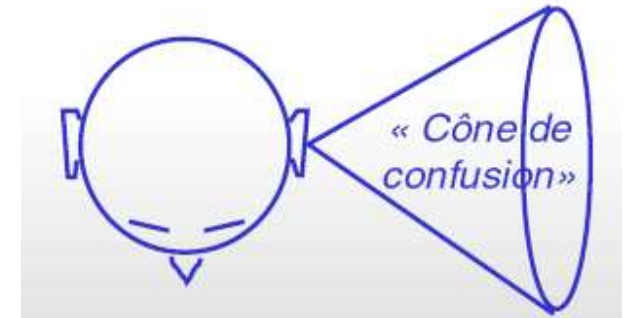
- Low frequency => source « low »,
- High frequency => source « high »

■ One needs at least 2/3 of frequency range for a sound to be localised



Monaural capacities: confusion cône

- All sources on the cone have the same ITD
- Ambiguities are solved by head movements
- If head movements are authorized, monaural localization is almost as good as binaural localization
- Other indices than ITD and IID are used: in particular change of the spectral patterns which is function of the sound direction of arrival



Impact of head and auricle (or pinna)

- *ITDs+IIDs+head movements are not enough to explain our capacity in localization (incl. elevation)*
- **Head+ pinna : complex filtering with a clear effect between 500 and 16 000 Hz**
 - pinna: essential for high frequencies (> 6 kHz)
 - Lowering of HF capacities if pinna relief are filled
- **Localization exploits knowledge of the source and listening room (with very fast acquisition)**



Subjective width of sound sources

■ Normalised intercorrelation:

$$F_{xy}(\tau) = \frac{\int_{-T}^T x(t)y(t+\tau)dt}{\int_{-T}^T x^2(t)dt \int_{-T}^T y^2(t)dt}$$

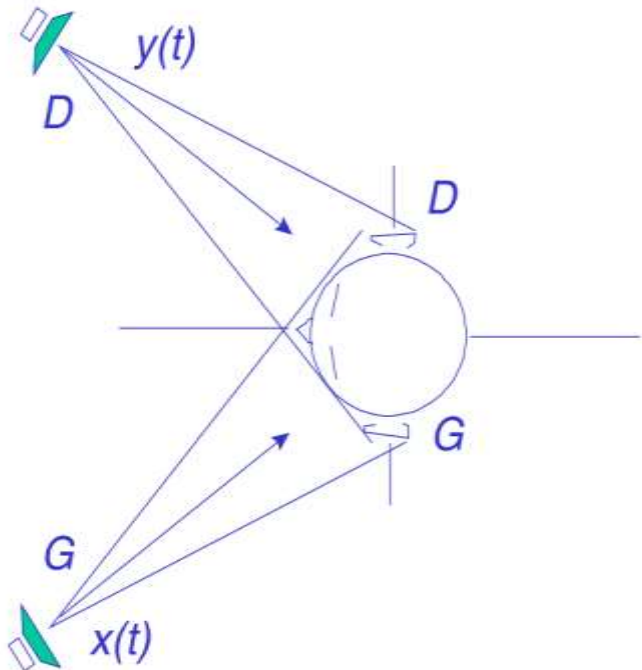
• Let

$$k = \max |F_{xy}(\tau)|$$

$k = 1$ signals are coherent (perfectly correlated) and a single event is heard

$k = 0$ Signals are decorrelated (2 events are heard in each loudspeaker)

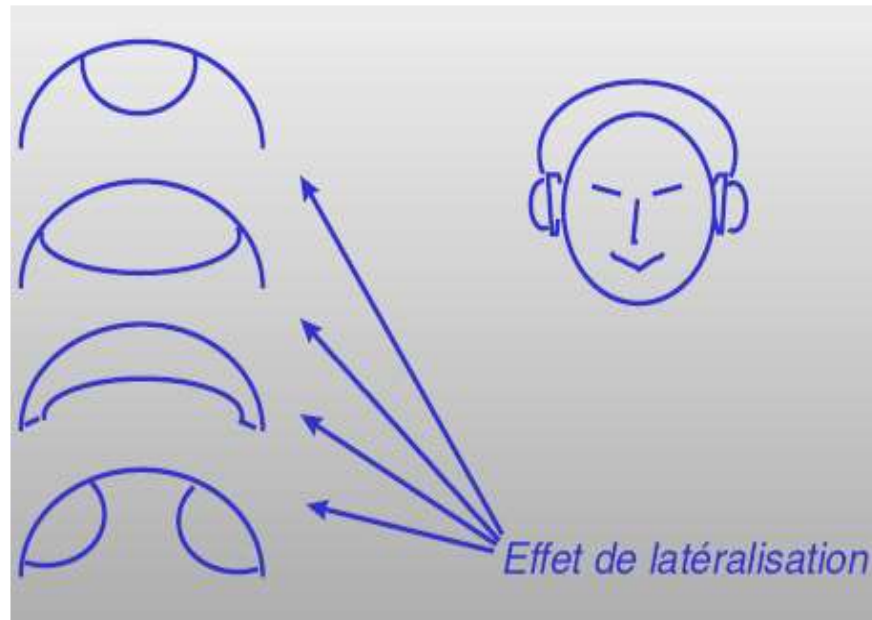
$k = 0.4$ Well balanced listening



Application to lateralisation

- Using filters (low pass, high pass) one may impose a desired k value

- $k=1$
- $k=0,85$
- $k=0,4$
- $k=0$



Conclusion about perception of space

■ Numerous indices, and in particular :

- ITD
- IID
- Pinna filtering, depending on sound direction of arrival

■ Redundancy is very useful in adverse situations

■ Our localisation capacity is

- Very good in azimuth, much worse in elevation



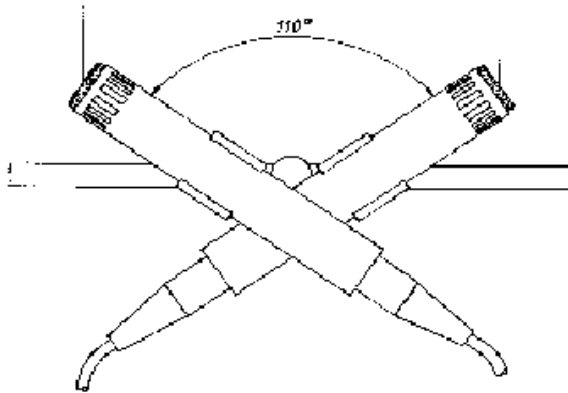
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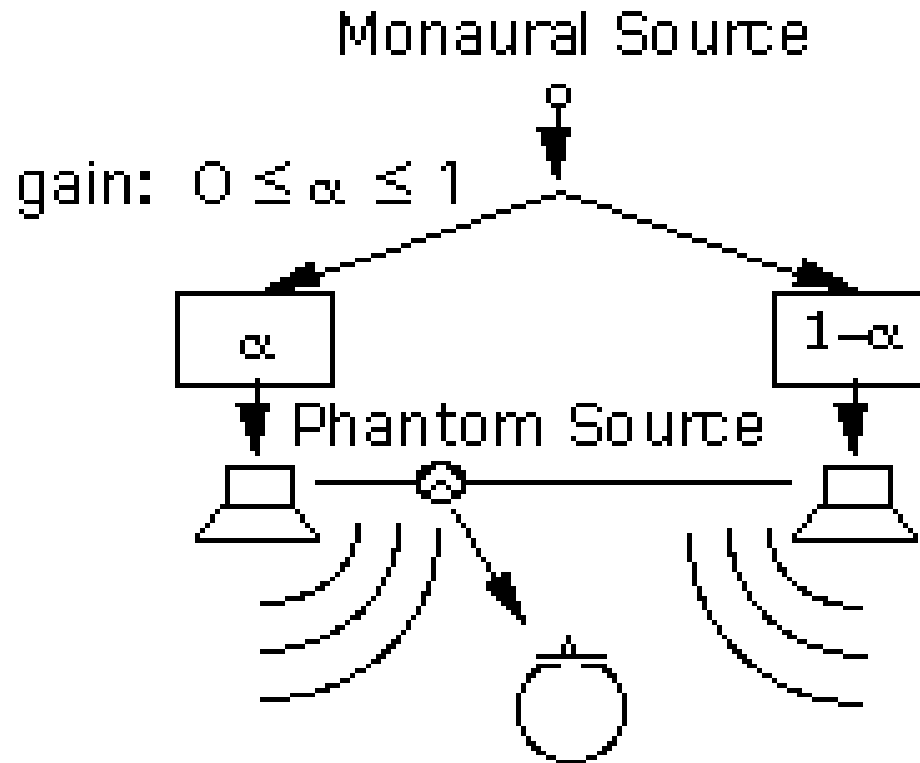


Stereo recordings

- Use the intensity difference (IID) and time differences (ITD) or Phase differences (IPD).
- For instance, recording using 2 microphones of different directivity (XY) or placed at different positions (AB)



Stereo synthesis





Stereo rendering

- **On Loudspeakers: two loudspeakers with an aperture of 60 degrees**
 - Phantom images on a straight line between loudspeakers
 - Sweet spot
- **Headphones**
 - Localization inside the head



Surround: multi-channel systems

■ 2 channels systems:

- **Limitation of the localization in a specific zone (in front in stereo)**
- **Constraint on the listener position**

⇒ **Solution: increase the number of channels**

■ « surround » approaches

- **1940: Fantasia (« Fantasound »)**
 - 3 channels (left wall, center, right wall)
- **In the fifties: 4 channels format 4**
 - Compatibility problem with mono
 - No commercial success

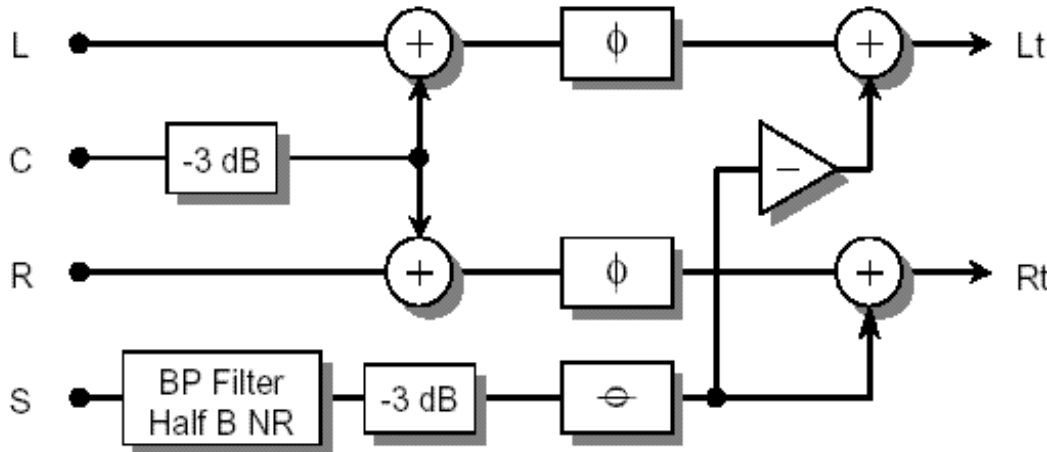


Brief history

- 1977 : **Dolby Stereo** for movie (*Starwars*)
- 1982 : **Dolby Surround** for home
- 4 channels system (G,D,C,S) but on on 2 channels.
- 1992: **Dolby AC-3** coding, digital system with 5.1 channels (which became *Dolby Digital*)
- 2012 : **Dolby Atmos** (up to 128 different audio elements rendered to up to 64 individual speakers)
- **Dolby** but also **DTS, Auro, THX,...: Auro 3D, DTS:X**



Dolby surround: coding



$$L_t = L + \frac{C}{\sqrt{2}} + i \frac{S}{\sqrt{2}}$$

$$R_t = R + \frac{C}{\sqrt{2}} - i \frac{S}{\sqrt{2}}$$

$$L_d\acute{e}c\acute{o}d\acute{e} = L_t$$

(Stereo compatibility)

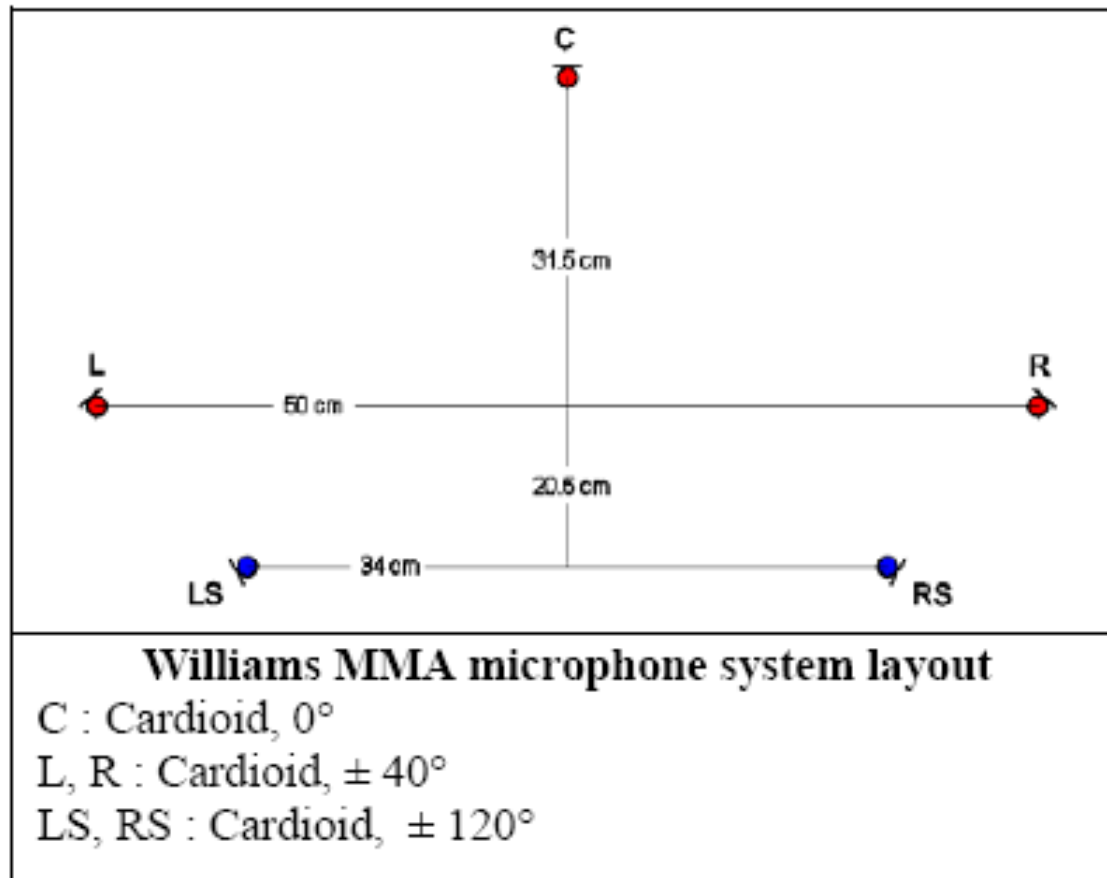
$$R_d\acute{e}c\acute{o}d\acute{e} = R_t$$

$$C_d\acute{e}c\acute{o}d\acute{e} = \frac{1}{\sqrt{2}} (L_t + R_t) = C + \frac{1}{\sqrt{2}} (L + R)$$

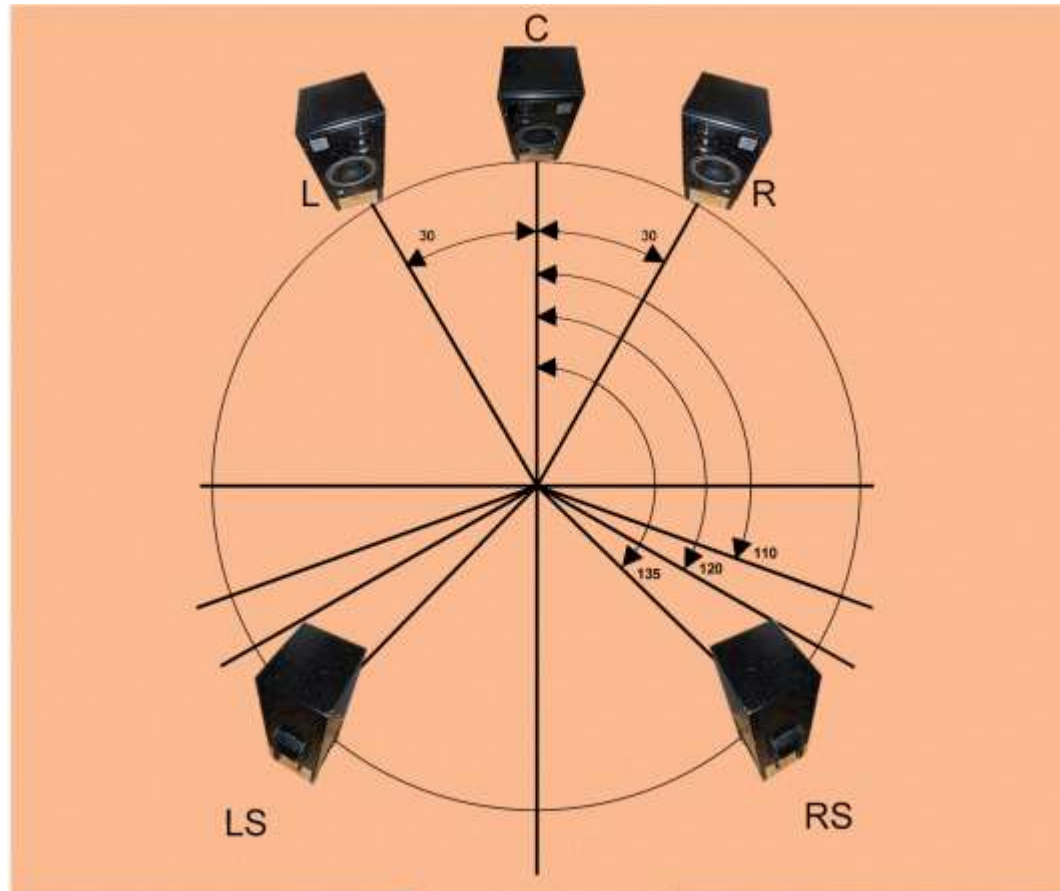
$$S_d\acute{e}c\acute{o}d\acute{e} = \frac{1}{\sqrt{2}} (L_t - R_t) = i * S + \frac{1}{\sqrt{2}} (L - R)$$



Dolby 5.1: recording



Reproduction (5.1)



Dolby Atmos

(> 1000 movies in this format (first is « Rebelle in 2012)
around 20 theater equipped in France in 2019

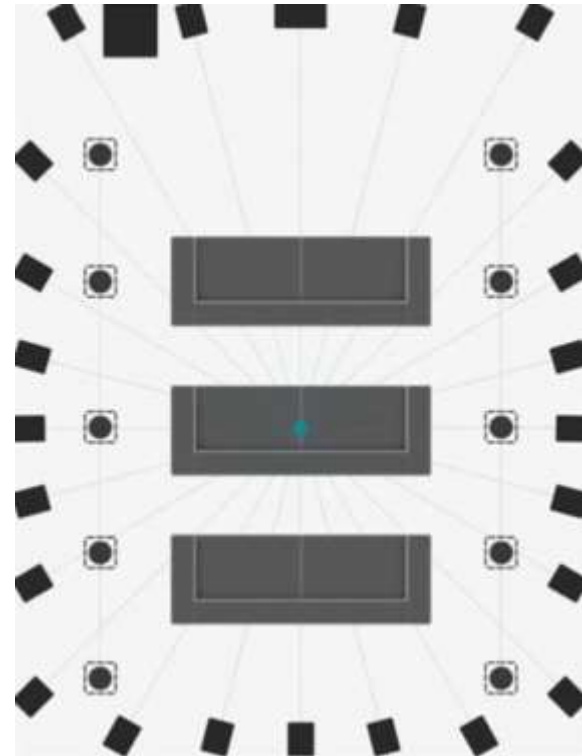
■ example of configurations for reproduction

4 specific speakers + bass



4 x R50 et 1 caisson de basses

24 speakers
+ 8 overhead speakers



Sound rendering

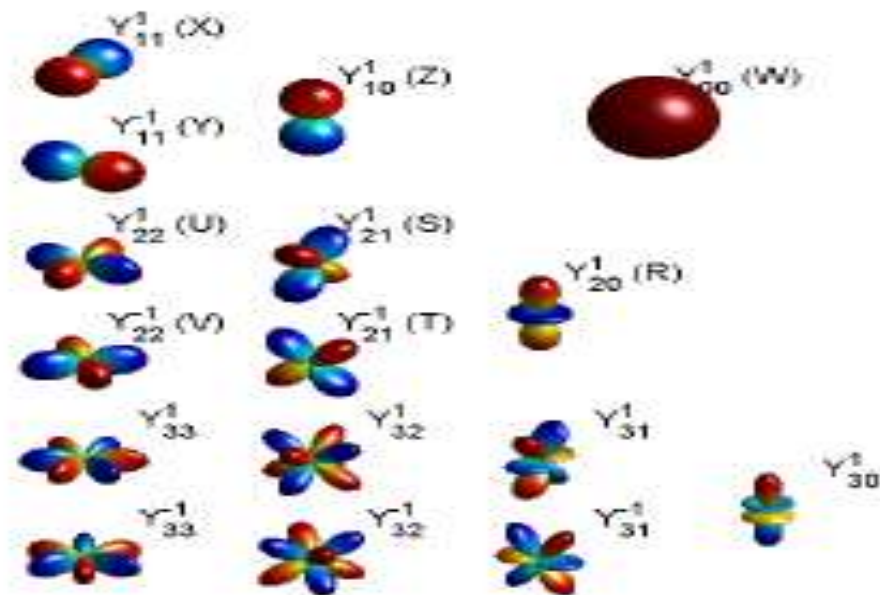
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Ambisonics

- System with a central reference
- Based on the decomposition of the sound field in spherical harmonics

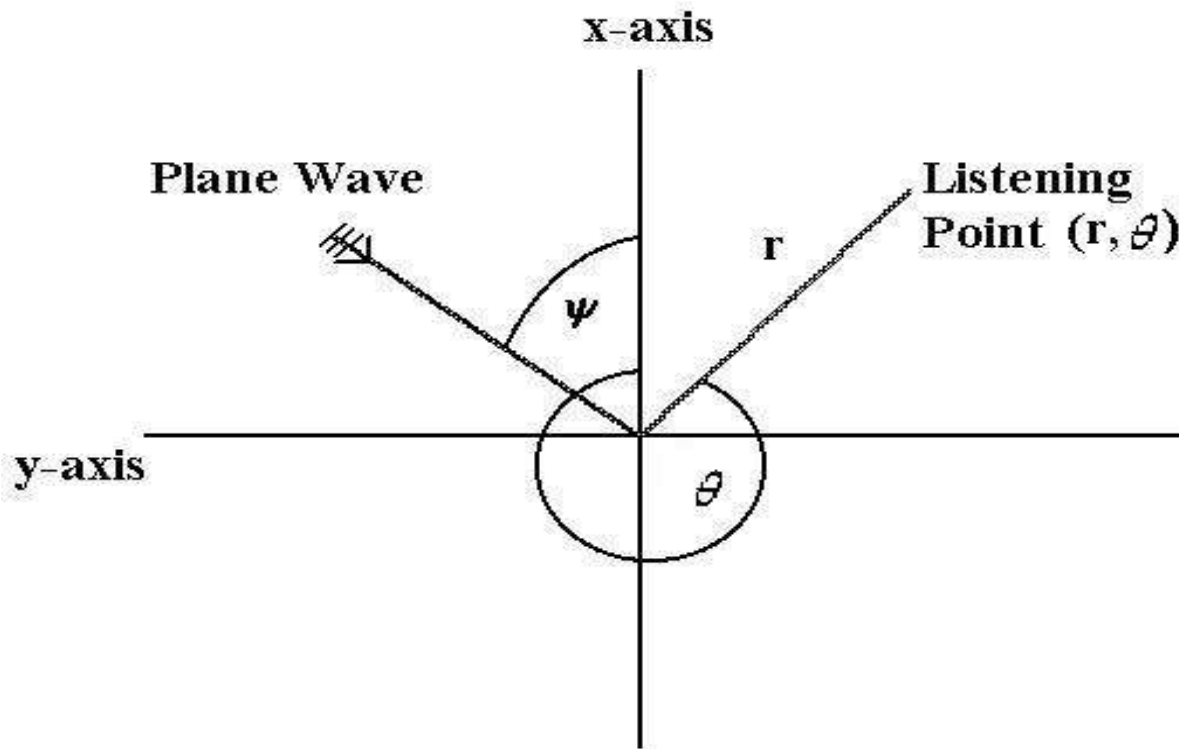
$$p(r, \theta, \varphi) = \sum_{m, n, \sigma} \tilde{A}_{mn}^{\sigma} \tilde{Y}_{mn}^{\sigma}(\theta, \varphi) j^m j_m(kr)$$



Ambisonics: synthesis of a plane wave

■ Plane wave

$$S_\psi = P_\psi e^{ikr \cos(\theta - \psi)}$$



Ambisonics: synthesis of a plane wave

- Plan wave in terms of spherical harmonics is given by:

$$S_\psi = P_\psi J_0(kr) + P_\psi \left(\sum_{m=1}^{\infty} 2i^m J_m(kr) [\cos(m\psi)\cos(m\theta) + \sin(m\psi)\sin(m\theta)] \right)$$

- If we suppose that the wave that comes from each loudspeaker is approximately a plane wave at the listening point and if the loudspeaker is at position ϕ_n

$$S_n = P_n J_0(kr) + P_n \left(\sum_{m=1}^{\infty} 2i^m J_m(kr) [\cos(m\phi_n)\cos(m\theta) + \sin(m\phi_n)\sin(m\theta)] \right)$$

$$S = \sum_{n=1}^N P_n J_0(kr) + \sum_{m=1}^{\infty} 2i^m J_m(kr) \left(\sum_{n=1}^N P_n \cos(m\phi_n)\cos(m\theta) + \sum_{n=1}^N P_n \sin(m\phi_n)\sin(m\theta) \right)$$



Ambisonics: synthesis of a plane wave

- We can then obtain the following equations (term by term identification):

$$P_\psi = \sum_{n=1}^N P_n$$

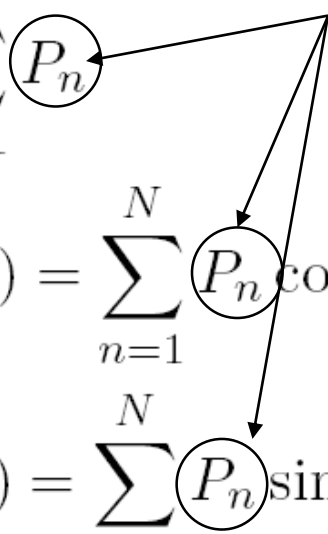
$$P_\psi \cos(m\psi) = \sum_{n=1}^N P_n \cos(m\phi_n)$$

$$P_\psi \sin(m\psi) = \sum_{n=1}^N P_n \sin(m\phi_n)$$



Ambisonics: synthesis of a plane wave

■ B-Format : only 1st order

$$\begin{aligned} W &= P_\psi = \sum_{n=1}^N P_n && \text{omnidirectionnal component} \\ X &= P_\psi \cos(\psi) = \sum_{n=1}^N P_n \cos(\phi_n) && X \text{ axis component} \\ Y &= P_\psi \sin(\psi) = \sum_{n=1}^N P_n \sin(\phi_n) && Y \text{ axis component} \end{aligned}$$


□ We can show that (*for a plane wave*)

$$P_n = \frac{1}{N} (W + 2X \cos \phi_n + 2Y \sin \phi_n)$$



Ambisonics: decoding and rendering

- Ambisonics system: in matrix form

$$\mathbf{b} = \mathbf{A} \cdot \mathbf{x}$$

$$\mathbf{b} = [W, X, Y, U, V, \dots]^T$$

$$\mathbf{x} = [P_1, P_2, P_3, \dots, P_N]^T$$

$$\mathbf{A} = \begin{bmatrix} 1 & 1 & \dots & 1 \\ \cos(\varphi_1) & \cos(\varphi_2) & & \cos(\varphi_N) \\ \sin(\varphi_1) & \sin(\varphi_2) & & \sin(\varphi_N) \\ \vdots & \vdots & & \vdots \\ \sin(m\varphi_1) & \sin(m\varphi_2) & \dots & \sin(m\varphi_N) \end{bmatrix}$$

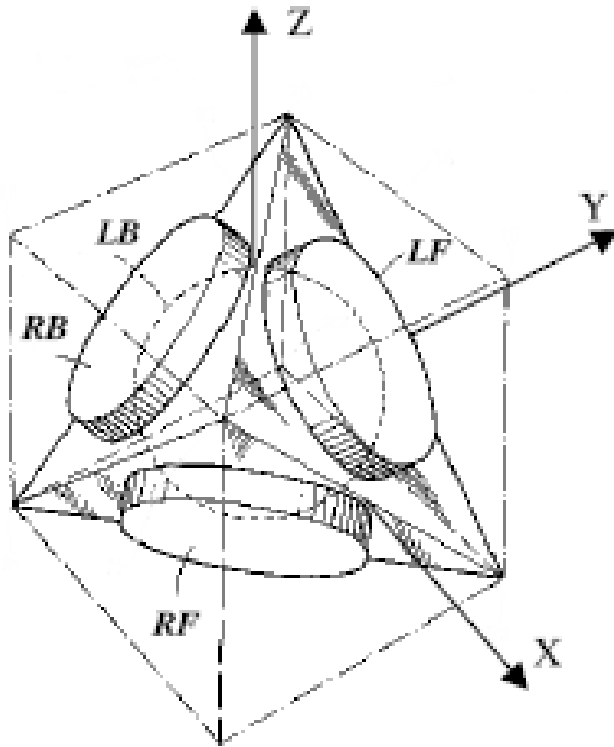
- Solution given by :

$$\mathbf{x} = \mathbf{A}^T \cdot (\mathbf{A} \cdot \mathbf{A}^T)^{-1} \cdot \mathbf{b}$$



Ambisonics: recording

■ SoundField microphone



$$\left\{ \begin{array}{l} W \\ X \\ Y \\ Z \end{array} \right. = \begin{array}{l} LF + LB + RF + RB \\ LF - LB + RF - RB \\ LF + LB - RF - RB \\ LF - LB - RF + RB \end{array}$$

Format-B

Format-A



Microphone HOA or « soundfield »



Experimental:
France Telecom, JES 2006)



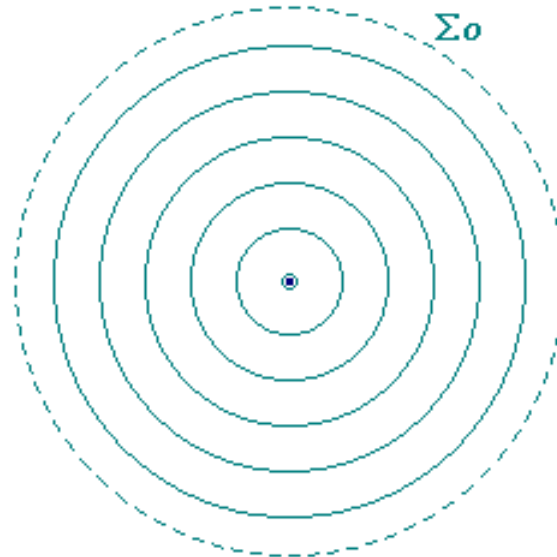
Tetramic (Coresound)



Microphone NAB

Wave field synthesis

- Huyghens principle : « **Vibrations which propagates inside a closed surface Σ_0 containing the source are identical to those that we would obtain by replacing this source by new sources adequately placed on the surface Σ_0 »**



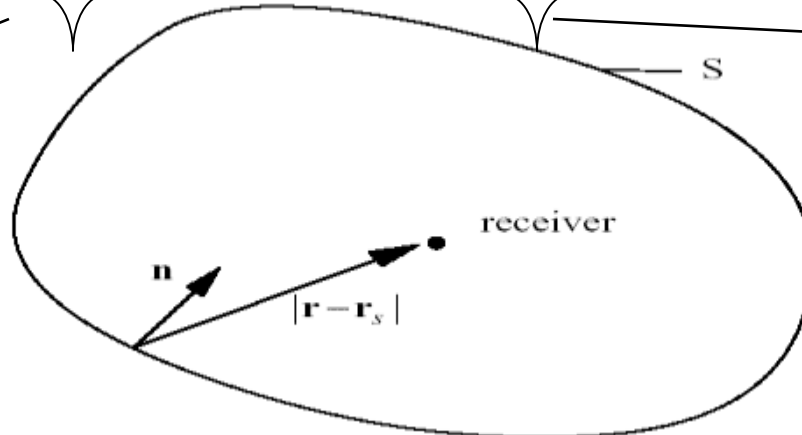
Wave Field Synthesis

(DELFT, IRCAM, ORANGE, University of Erlangen Nuremeberg)

- Linear acoustic theory: **It is possible to reproduce any sound field inside a volume enclosed by a surface by placing sources (monopoles and dipoles) on this surface (considering that there are no other sources inside this volume).**
- Kirchoff-Helmholtz integral

$$P(\mathbf{r}, \omega) = \frac{1}{4\pi} \iint_S \left[P(\mathbf{r}_s, \omega) \frac{\partial}{\partial n} \left(\frac{e^{-jk|\mathbf{r}-\mathbf{r}_s|}}{|\mathbf{r}-\mathbf{r}_s|} \right) - \frac{\partial P(\mathbf{r}_s, \omega)}{\partial n} \frac{e^{-jk|\mathbf{r}-\mathbf{r}_s|}}{|\mathbf{r}-\mathbf{r}_s|} \right] dS$$

Dipoles:
sources linked
to pressure

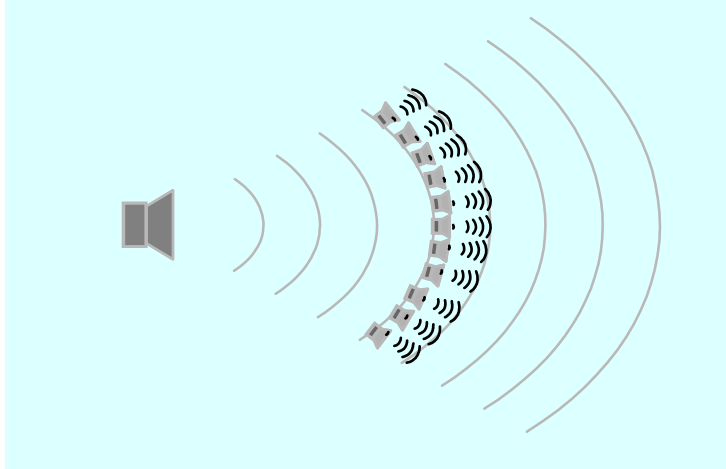


Monopoles:
sources linked to
sound field
velocity



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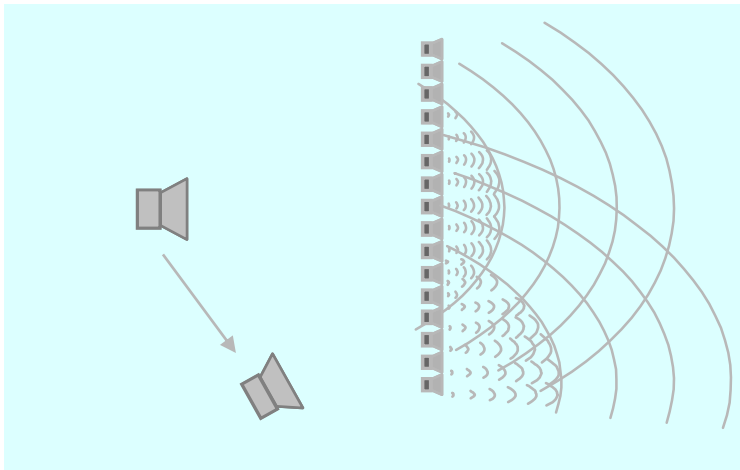
Wave Field Synthesis (WFS) – Concept



- Physical reproduction of the sound field produced by a primary source with an ensemble of secondary sources.

- Impedance relation: the knowledge of pressure is enough.

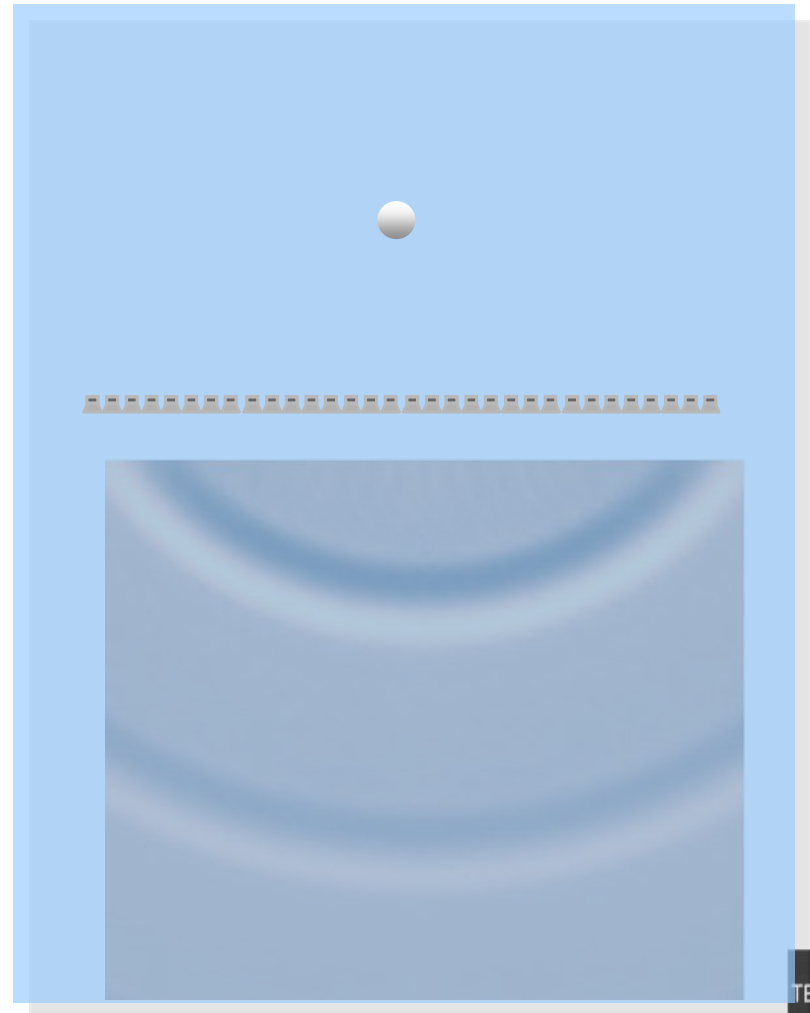
- Possible to adapt to any geometry of loudspeaker.



Recording and reproduction in WFS

(from E. Corteels)

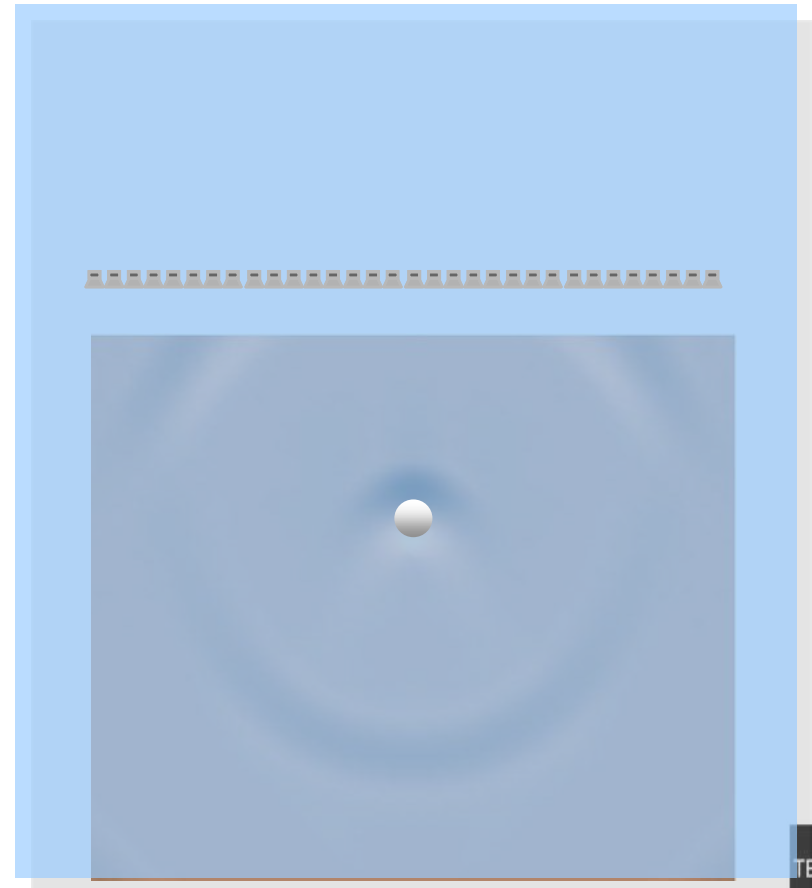
- Recording
- Reproduction
- Synthesis
 - Virtual punctual source
 - Large zone reproduction.



Reproduction in WFS

(from E. Corteels)

- Potentially in front of the loudspeakers
- But not realistic between loudspeakers and virtual source
- ...

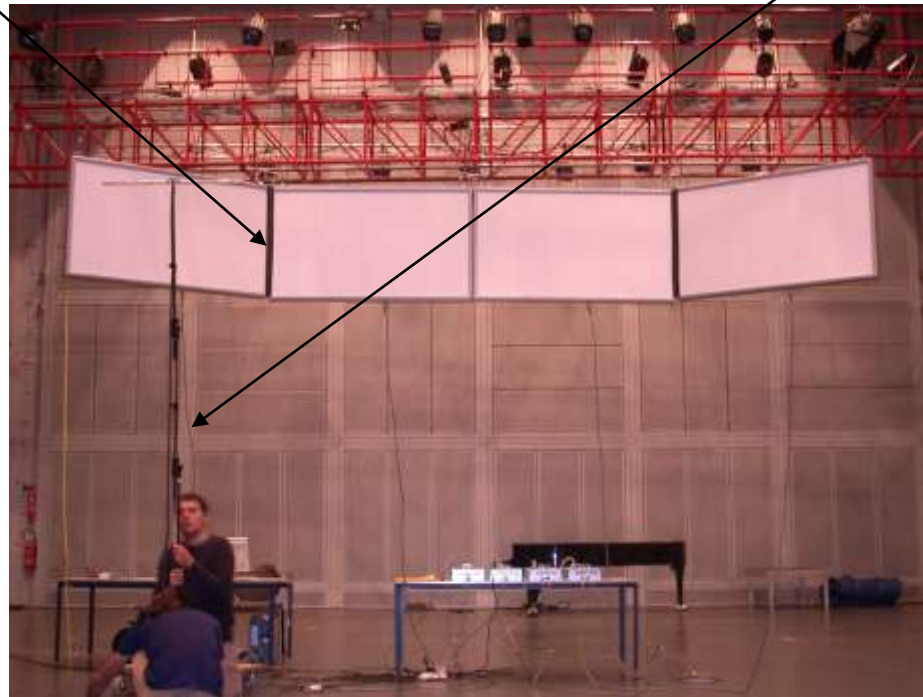


Examples at IRCAM

**Loudspeakers MAP « Multi
Actuator Panel »**

(8 actuators per panel)

**Microphone array
for room
corrections**



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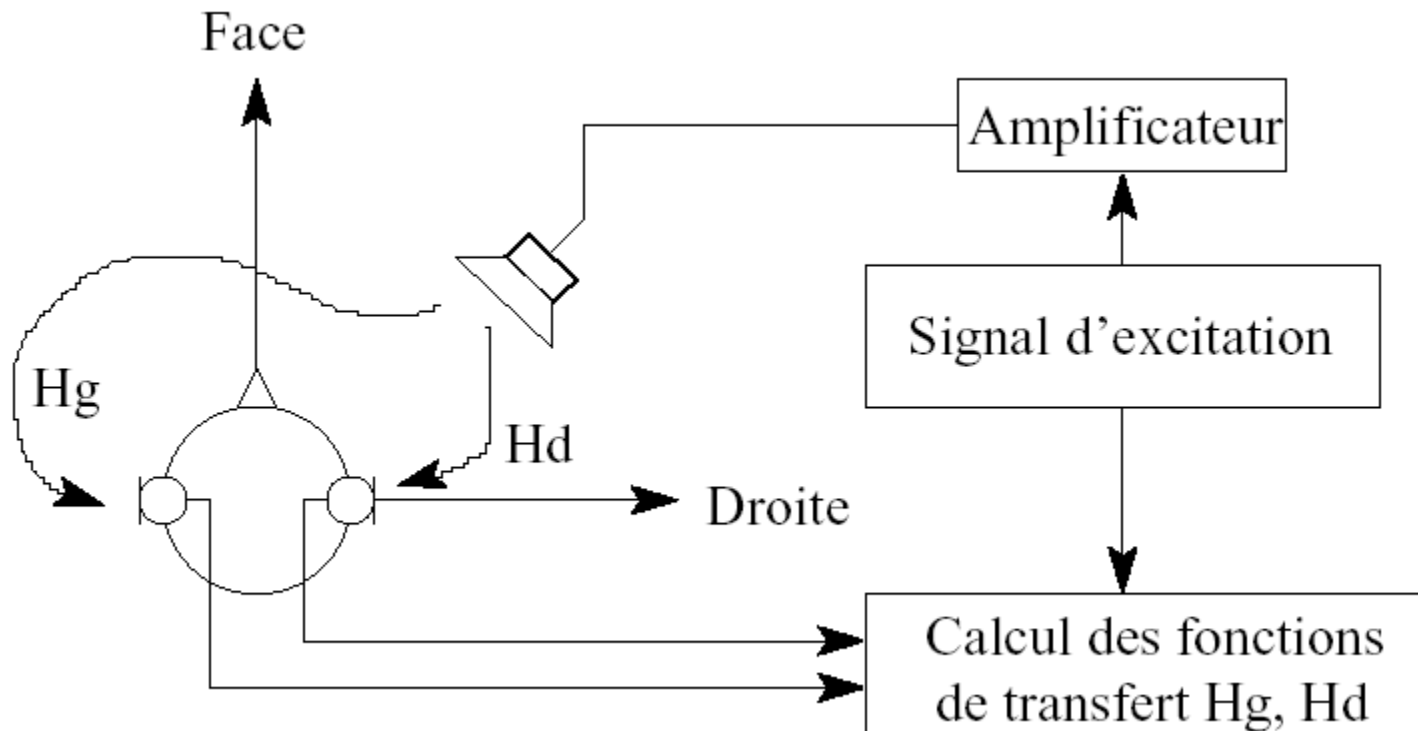
Binaural approaches

- **Recording:** to record exactly the signal received at the listener ears (artificial head, binaural microphones)
- **Synthesis:** from a monophonic recording (anechoic) using binaural filters to synthesize a binaural listening
 - **For headphone listening: localisation « outside the head »**
 - **For loudspeaker listening (transaural): 3D localisation with 2 loudspeakers (and not only in a plane between loudspeakers)**



Binaural synthesis

- Measuring binaural filters (Head Related Transfer Functions, HRTFs)



Measuring filter's impulse response

■ Using Maximum Length sequences (LMS)

- Periodic signals of period $L=2^k-1$
- Signals take only +1 ou -1 values
- Their autocorrelation function is almost a dirac :

$$C_{xx}^L(n) = \frac{1}{L} \sum_{m=0}^{L-1} x_{m-n}x_m = \left(1 + \frac{1}{L}\right)\delta_{[L]}(n) - \frac{1}{L}$$

—We then have:

$$C_{xy}^L(n) = \frac{1}{L} \sum_{m=0}^{L-1} x_{m-n}y_m = \left(1 + \frac{1}{L}\right)\delta_{[L]}(n) \star h_n - \frac{1}{L}\bar{h}$$

■ Sweep



Measuring binaural filters (Head Related Transfer Functions, HRTFs)

- Using a KEMAR head (*example from CIPIC*)



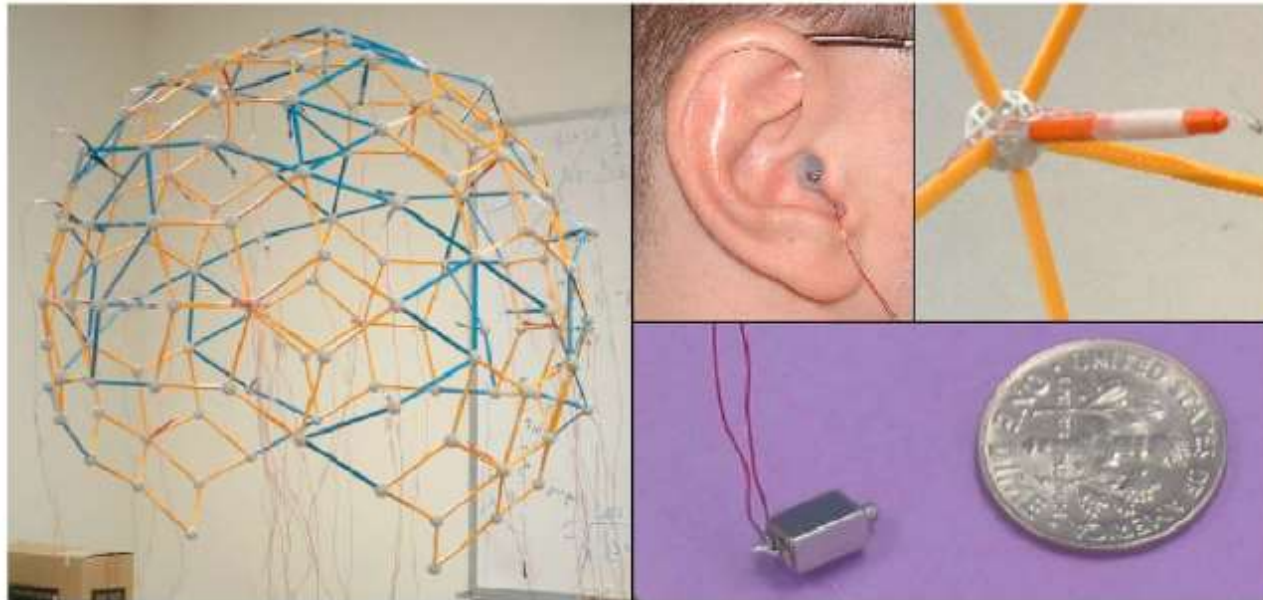
Measuring binaural filters (Head Related Transfer Functions, HRTFs)

■ Examples from (Telecom ParisTech, IRCAM)

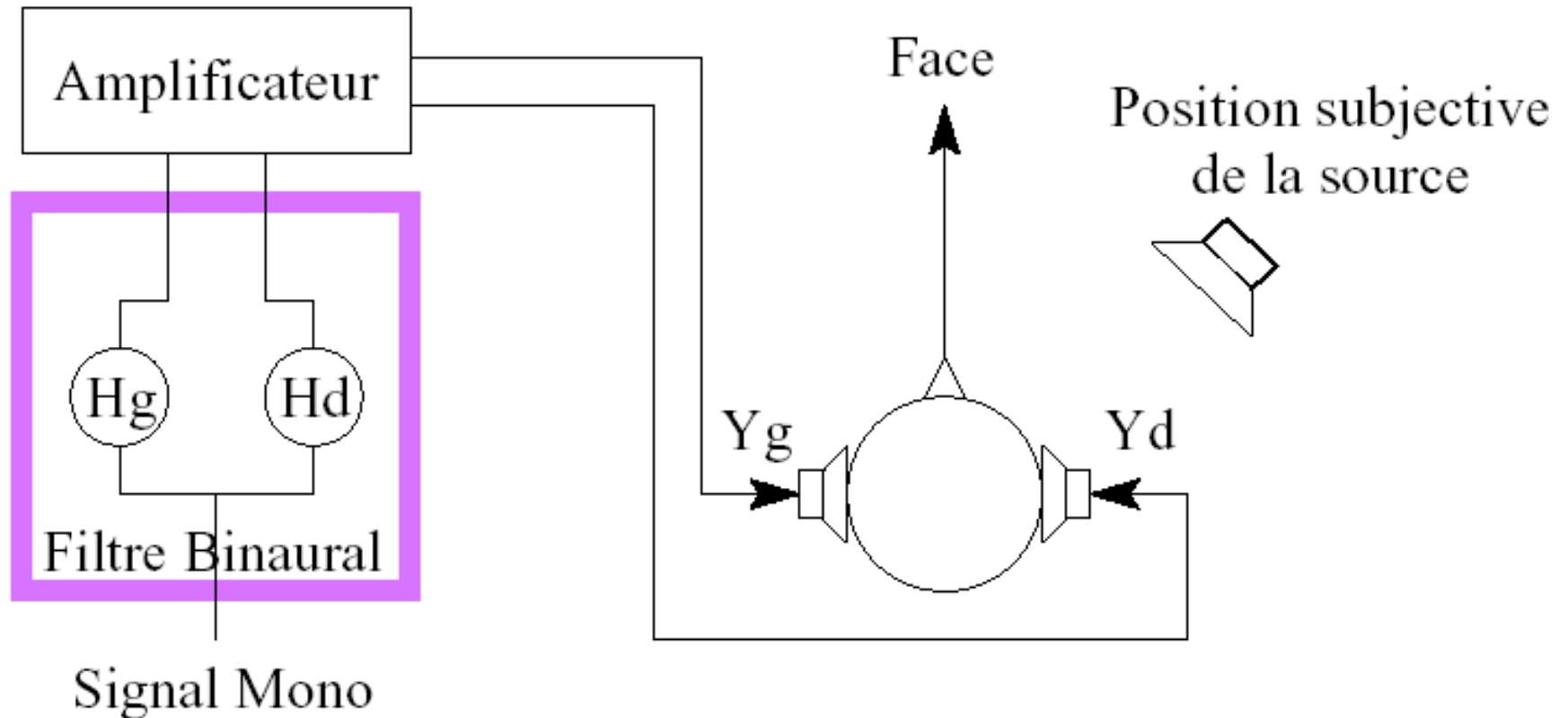


Measuring binaural filters (Head Related Transfer Functions, HRTFs)

- For individuals (*from Maryland University*)



Binaural synthesis



Problems with HRTFs

- A major problem: individualization of HRTFs
- Dynamic systems: interpolation of HRTFs and head tracking
- Distance rendering
- HRTFs modelling ...



Public datasets

■ IRCAM: LISTEN

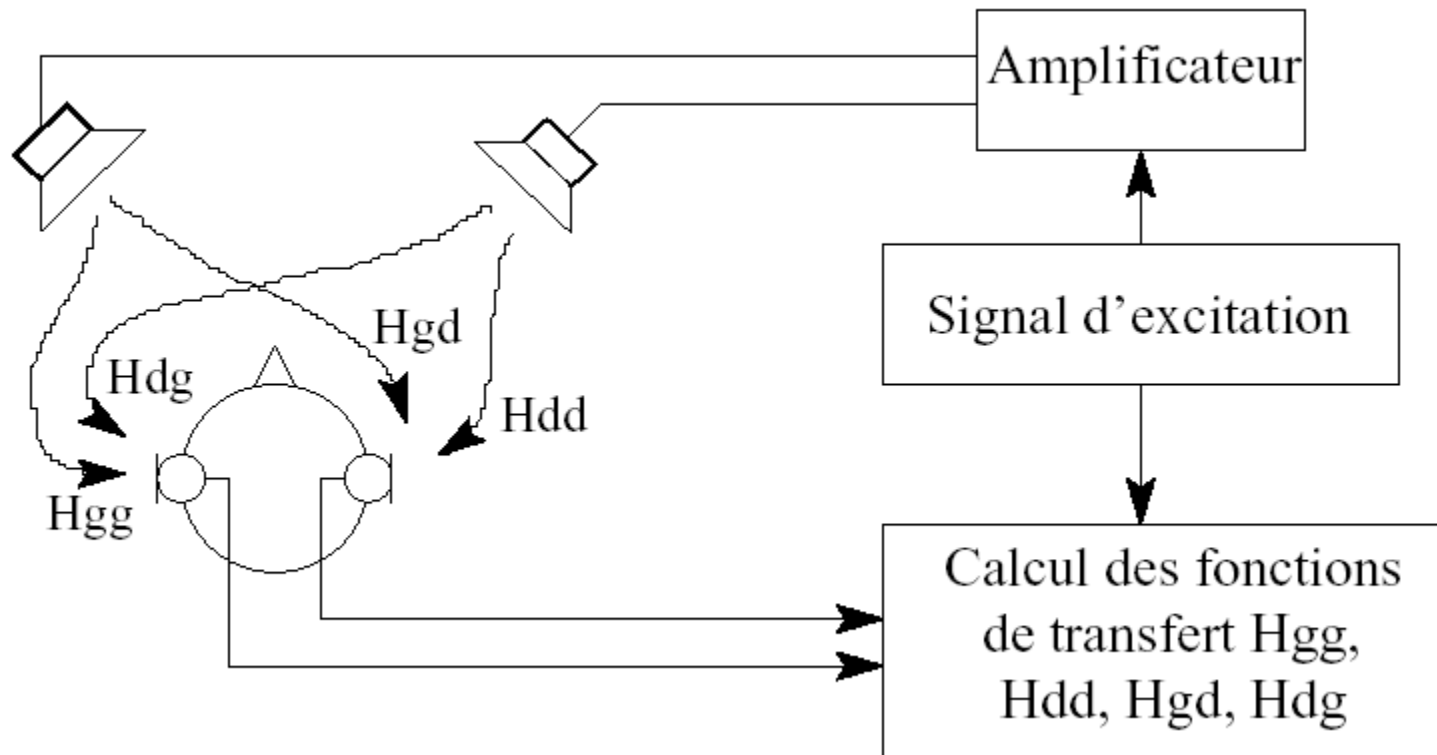
■ CIPIC

- **HRTFs measured for discrete values of azimuth, elevation and time**
 - Sampled at 44.1 kHz (200 samples)
 - 25 azimuths (between -90° and $+90^\circ$)
 - 50 elevations (between -45° and 230° by steps of 5.625°)
- **HRTFs measured for over 90 persons (the public dataset comprises 45 persons!)**



Conversion binaural \Leftrightarrow transaural

- Needs the measurements of the 2 transfer functions from the loudspeakers to the listener.



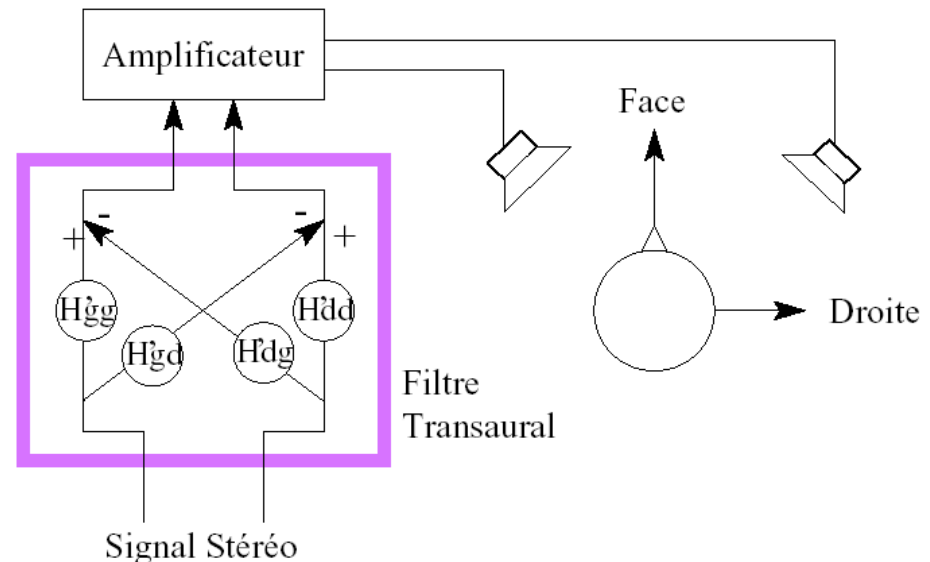
Conversion binaural ↔ transaural

- Transfer matrix characterizing the transformations of the signals played at the loudspeakers to the signals received at listener's ears Y_g et Y_d

$$\begin{bmatrix} Y_g \\ Y_d \end{bmatrix} = \begin{bmatrix} H_{gg} & H_{dg} \\ H_{gd} & H_{dd} \end{bmatrix} \begin{bmatrix} Z_g \\ Z_d \end{bmatrix}$$

- The conversion binaural \Rightarrow transaural is the inverse matrix

$$\begin{bmatrix} Z_g \\ Z_d \end{bmatrix} = \frac{\begin{bmatrix} H_{dd} & -H_{dg} \\ -H_{gd} & H_{gg} \end{bmatrix}}{H_{gg}H_{dd} - H_{dg}H_{gd}} \begin{bmatrix} Y_g \\ Y_d \end{bmatrix}$$



Conversion binaural \Leftrightarrow transaural

- Possible Symetry hypotheses (reproduction symetry and hearing property symetry)

$$H_g = G \quad ; \quad H_d = D \quad ; \quad H_{gg} = H_{dd} = G_0 \quad ; \quad H_{gd} = H_{dg} = D_0$$

✓ Binaural transfer functions

✓ ***G et D*** : for any source position

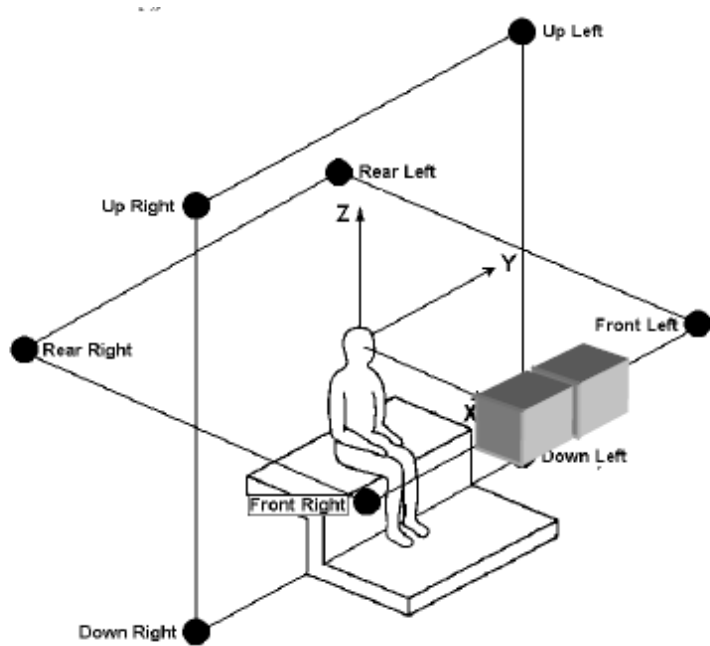
✓ ***G₀ et D₀*** : for the position of the left loudspeaker

✓ **We then obtain:**

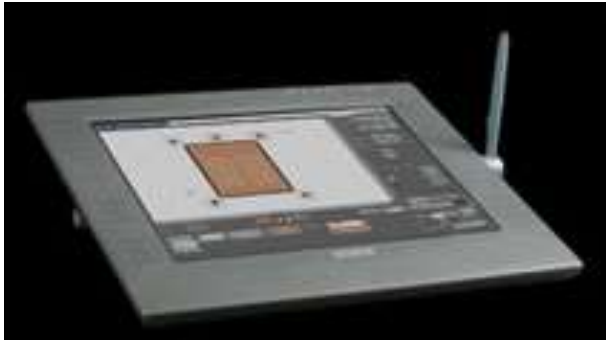
$$\begin{bmatrix} Z_g \\ Z_d \end{bmatrix} = \frac{\begin{bmatrix} G_0 & -D_0 \\ -D_0 & G_0 \end{bmatrix}}{G_0^2 - D_0^2} \begin{bmatrix} Y_g \\ Y_d \end{bmatrix} = \frac{1}{2} \left(\frac{\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}}{G_0 + D_0} + \frac{\begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}}{G_0 - D_0} \right) \begin{bmatrix} Y_g \\ Y_d \end{bmatrix}$$



A transaural system : Ambiophonics



Some rendering systems examples: IOSONO



Existing applications...

- **Ambiophonics Playstation**
- **Home Theaters (5.1 et Virtual Speaker Technology)**
- **WFS: cinéma**
- **3D Sound by Arkamys sur Renault Mégane (2009)**



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Existing applications...

- Ambisonics (<http://www.ambisonic.net/>): used in sound engineering...micro Soundfield

- Dolby Headphones

..or almost

- MPEG Surround
- Binaural Mobile
- Binaural iPod
- Spatial music production



A few organisation active in 3D rendering

- IRCAM
- Orange Labs
- LMA Marseille
- Genesis acoustics
- Trinnov Audio
- Télécom ParisTech...
- A-Volute
- LIMSI
- Euphonia
- ARKAMYS
- Sonic emotion
- Immersion



A few links

■ An overview on spatial reproduction

- http://www.deutsche-telekom-laboratories.de/~sporssas/publications/talks/AES128_Tutorial_Spatial_Audio_Reproduction.pdf

