Energy efficient resource allocation for type-I HARQ under the Rician channel

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Abstract

This paper addresses the per-link power and bandwidth allocation problem with the objective of maximizing energy efficiency (EE) related metrics under per-link minimum goodput constraint when only statistical channel state information is available to perform the resource allocation (RA). We consider the Rician channel model, which encompasses both Rayleigh and additive white Gaussian noise channels as special cases. We also consider type-I hybrid automatic repeat request with practical modulation and coding schemes. The addressed problems are the maximization of the sum of the user's EE, the maximization of the EE of the user with the lowest EE and the maximization of the EE of the network. We derive the optimal solution of these problems in closed form using fractional programming and convex optimization. We show that substantial gains can be achieved by taking into account the line of sight (LoS) between the transmitter and the receiver instead of only considering the channel variance.

Index Terms

HARQ, resource allocation, energy efficiency, fractional programming, convex optimization, D2D communications.

I. INTRODUCTION

Modern wireless communications often take place in a multiuser context. The performance of multiuser systems is led by the so-called resource allocation (RA), which requires some

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knowledge about the links' channels. In this work, we consider that only statistical channel state information (CSI) is available to perform the RA. This assumption is realistic for instance in ad hoc networks [1], or in device to device (D2D) communications, which are of central importance within 5G networks [2], [3]. Indeed, in these types of networks, the RA may be performed in an assisted fashion, i.e. there is a node called resource manager (RM) performing the RA [4]. As a consequence, the RM, which collects all the links' CSI, has only access to outdated CSI. Instead of performing the RA using unreliable outdated CSI, we consider that the RM uses statistical CSI to perform the RA [1]. Hence, the underlying statistical channel model is crucial. In this paper, we especially focus on the Rician fading channel, which is known to accurately represent the realistic statistical behaviour of wireless channel when there exists a LoS between the transmitter and the receiver [5], [6]. This channel model encompasses both the Rayleigh and the additive white Gaussian noise (AWGN) channels as special cases. The Rician channel model receives today more attention in the literature due to its accuracy to model the channel in the context of millimetre wave communications [5], [7], which is a promising technology for 5G communications [2].

Since we only have access to statistical CSI, we consider the use of the hybrid automatic repeat request (HARQ) mechanism to increase the reliability of the communications. This mechanism is a combination of automatic repeat request (ARQ) and forward error correction (FEC) allowing to improve the transmission capability. Actually, FEC provides a correction capability while ARQ allows to take advantage of the time varying nature of the wireless channel. The HARQ mechanism is today well investigated, and is used in multiuser context, for instance in 4G long term evolution (LTE) [8]. There exist different types of HARQ, differing in the way the packets are sent and decoded [9]. We find optimal closed form solutions of the RA problems for type-I HARQ. We investigate applications of these solutions to type-II HARQ by simulations.

The RA is performed by optimizing a criterion subject to quality of service (QoS) constraints. Two well established criteria are the minimization of the total transmit power [10] and the maximization of the data rate [11]. However, it is clear that maximizing the data rate leads to high energy consumption. But it is less obvious that minimizing the transmit power may not be efficient from an energy viewpoint. For these reasons, another metric called energy efficiency (EE) has appeared in the literature and has recently gained much interest [12], [13]. This metric, measured in bits/joule, is defined as the ratio between the goodput, i.e. the number of information

bits that can be transmitted without error per unit of time, and the power consumption to transmit these bits. Hence, the EE is of interest since it captures a tradeoff between the goodput and the energy consumption. In this paper, we are interested in maximizing EE related metrics for HARQ based systems when only statistical CSI is available. In details, we focus on maximizing the sum of the users' EE (SEE), the EE of the network, called global EE (GEE) and the EE of the link with the lowest EE called minimum EE (MEE). In the remainder of the paper, the maximization of the SEE, GEE and MEE criteria will be referred to as the maximum SEE (MSEE), maximum GEE (MGEE) and maximum MEE (MMEE) respectively. The considered resource to allocate are per link transmit power and bandwidth.

A. Related works

First, let us review the works studying the EE of HARQ in the single user context [14]– [27]. Notice that, in [27], the authors do not explicitely consider the HARQ mechanism, but the considered metric is valid for type-I HARQ. In [14]–[25], the authors consider statistical CSI at the transmitter, while in [26] imperfect CSI is assumed and in [27], perfect CSI is assumed to be available. These works mainly address power and/or rate optimization within HARQ mechanism, typically using convex optimization.

Second, we focus on the works dealing with the RA with EE related criteria in a multiuser context when considering perfect CSI at the transmitter side. In this category, a lot of works consider the use of capacity achieving codes [28]–[36] while practical modulation and coding schemes (MCS) are considered in [37]. Among those works, [28]–[34], [37] do not consider HARQ whereas this mechanism is taken into account in [35], [36]. In details, when capacity achieving codes are considered with no HARQ, the MSEE problem is solved in [28] while the MMEE problem is solved in [29]. In [30], several heuristics are derived for the MSEE and MMEE problems. The multi-cell context is addressed in [31], [32]. In [31], the MSEE, maximum PEE (MPEE), and MGEE problems are solved while, in [34], the MMEE problem is addressed. In [33], centralized and decentralized algorithms are proposed for the MGEE problem. In [32], a distributed algorithm is proposed to solve the MMEE problem. When capacity achieving codes are considered in [36]. When practical MCS along with perfect CSI are considered without HARQ, the MGEE problem for the LTE downlink is addressed in [37].

Third, we review the works addressing the RA problem with EE related objective functions when statistical CSI is available. This problem is addressed considering capacity achieving codes with no HARQ and the Rayleigh channel in [38], [39]. Practical MCS with HARQ are considered in [40], [41], which consider the Rayleigh channel. In [40], the authors maximize the harmonic mean of the users' EE in a relay assisted networks when type-I HARQ is considered. In [41], the MSEE problem is solved for type-II HARQ.

Finally, Table I summarizes the existing works concerning the RA problem with EE related metrics for HARQ when considering practical MCS. We see that no work addresses the RA problem with the objective of maximizing EE related metrics under the Rician channel when statistical CSI is available.

TABLE I: Existing EE based RA algorithms for HARQ with practical MCS and statistical CSI in the multiuser context.

	Rayleigh	Rice
Type-I	[40], [41]	None
Type-II	[41]	None

B. Contributions and paper organization

The contributions of this paper are the following ones.

- We optimally solve the MSEE, MGEE and MMEE problems for type-I HARQ under the Rician channel. Actually, we manage to transform these problems which have no interesting properties like convexity into convex problems. Our main technical contribution is to provide the analytical optimal solutions of these convex problems using the Karush-Kuhn-Tucker (KKT) conditions.
- We analyze the results of the proposed criteria through numerical simulations, and point out that substantial EE gains can be achieved by taking into account the Rician channel instead of the conventional Rayleigh channel. In other words, we exhibit the importance of taking into account the existence of a LoS during the RA instead of only considering the channel variance.

• We numerically study solution to perform the RA for type-II HARQ under the Rician channel. Actually, from Table I, we see that the RA for type-II HARQ under the Rayleigh channel is done in [41], while in this paper, we perform the RA for type-I HARQ under the Rician channel. We compare the RA from [41] and from this paper when applied on type-II HARQ under the Rician channel.

The rest of the paper is organised as follows. In Section II, we present the system model, our main assumptions and we formulate the RA problems. In Section III, we explain the resolution methodology used to solve these problems. In Section IV, we optimally solve the MSEE problem, while Section V is devoted to the optimal resolution of the MGEE problem and Section VI to the optimal resolution of the MMEE problem. In Section VII, we study the results of the proposed criteria through numerical simulations. Finally, in Section VIII, we draw concluding remarks. For the ease of readability, all the proofs are given in the Appendices.

II. SYSTEM MODEL, ASSUMPTIONS AND PROBLEM FORMULATION

A. Channel model and HARQ mechanism

Let us consider a network with a total bandwidth B divided in N_c subcarriers, which are shared between L active links using the orthogonal frequency division multiple access (OFDMA) as the multi access technology. Notice that our derivations extend straightforwardly to any multiple access multicarrier scheme and to single-carrier frequency division multiplexing as long as there is no interference between users. We suppose that the RM centralizes the statistical CSI of the links to perform the RA. We consider for each link a multipath channel, which is constant within one orthogonal frequency division multiplexing (OFDM) symbol and varies independently from OFDM symbol to OFDM symbol. Hence, similarly to [42], the received signal on link ℓ on the *n*th subcarrier at OFDMA symbol *i* writes as

$$Y_{\ell}(i,n) = H_{\ell}(i,n)X_{\ell}(i,n) + Z_{\ell}(i,n),$$
(1)

with $H_{\ell}(i,n) \sim C\mathcal{N}(a_{\ell}, \zeta_{\ell}^2)$ where $\mathcal{N}(a_{\ell}, \zeta_{\ell}^2)$ stands for the complex Gaussian distribution with mean a_{ℓ} and variance ζ_{ℓ}^2 , $X_{\ell}(i,n)$ is the transmitted symbol on the *n*th subcarrier of the *i*th OFDMA symbol and $Z_{\ell}(i,n) \sim C\mathcal{N}(0, N_0 B/N_c)$, with N_0 the noise level in the power spectral density. We assume that $H_{\ell}(i,n)$ is known at the receiver of the ℓ th link. We can define the average gain-to-noise ratio (GNR) G_{ℓ} and Rician K factor K_{ℓ} of the ℓ th link as

$$G_{\ell} := \frac{\mathbb{E}[|H_{\ell}(i,n)|^2]}{N_0} = \frac{\Omega_{\ell}}{N_0},$$
(2)

$$K_{\ell} := \frac{|a_{\ell}|^2}{\zeta_{\ell}^2},\tag{3}$$

with $\Omega_{\ell} := |a_{\ell}|^2 + \zeta_{\ell}^2$. Notice that $K_{\ell} = 0$ corresponds to the Rayleigh channel while $K_{\ell} \to +\infty$ corresponds to the AWGN channel. It is assumed that the RM only knows the average GNR and the Rician K factor of each link to perform the RA. Moreover, we suppose that well-designed time and frequency interleavers are used such that each modulated symbol experiments independent channel realization i.e. the channel can be seen as fast fading.

We assume that, at the medium access (MAC) layer, each link uses a type-I HARQ scheme. The information bits are grouped into packets of \mathcal{L}_{ℓ} bits, which are encoded by a FEC with rate R_{ℓ} to obtain the MAC packets. A MAC packet is sent on the channel at most \mathcal{T} times. At the received side, after decoding the *m*th received packet, the information bits are checked using a cyclic redundancy check (CRC) which is assumed to be error free. An acknowledgement (ACK) is sent if the information bits are correctly decoded, while otherwise a negative ACK (NACK) is sent. Since type-I HARQ is considered, the MAC packets received in error are discarded.

B. Energy consumption model

We suppose that a quadrature amplitude modulation (QAM) modulation with m_{ℓ} bits per symbol is used on link ℓ . Let n_{ℓ} (resp. $\gamma_{\ell} := n_{\ell}/N_c$) be the number of subcarriers (resp. the bandwidth proportion) allocated to the ℓ th link. Because the channel coefficients on each subcarrier are identically distributed, the same power is used on all the subcarriers, and we allocate bandwidth proportion instead of specific subcarriers. We then define $P_{\ell} := \mathbb{E}[|X_{\ell}(j,n)|^2]$ as the power allocated per subcarrier to the ℓ th link.

The total energy consumed to transmit and receive one packet is the sum of the transmission energy and the circuitry consumption of both the transmitter and the receiver. The power used by the ℓ th link to transmit and receive one OFDMA symbol is

$$P_{T,\ell} := N_c \gamma_k P_\ell \kappa_\ell^{-1} + P_{ctx,\ell} + P_{crx,\ell}, \tag{4}$$

with $\kappa_{\ell} \leq 1$ the efficiency of the power amplifier and $P_{ctx,\ell}$ (resp. $P_{crx,k}$) the circuitry power consumption of the transmitter (resp. the receiver).

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C. Energy efficiency

The EE \mathcal{E}_{ℓ} of link ℓ is the ratio between its goodput η_{ℓ} and its power consumption:

$$\mathcal{E}_{\ell} := \frac{\eta_{\ell}[\mathsf{bits/s}]}{P_{T,\ell}[\mathsf{W}]}.$$
(5)

Similarly, the GEE is the ratio of the sum of the users' goodput and the sum of their power consumption, which writes:

$$\mathcal{G} = \frac{\sum_{\ell=1}^{L} \eta_{\ell}}{\sum_{\ell=1}^{L} P_{T,\ell}}.$$
(6)

For type-I HARQ and when the channel has no correlation between the HARQ rounds, the goodput is given by [9]:

$$\eta_{\ell} = B\alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}E_{\ell})), \tag{7}$$

where $q_{\ell}(x)$ is the packet error rate (PER) on the ℓ th link for signal-to-noise ratio (SNR) x, $E_{\ell} := N_c P_k / B$ and $\alpha_{\ell} := m_{\ell} R_{\ell}$. Notice that because type-I HARQ is considered and since the channel is uncorrelated between the HARQ round, (7) is independent of \mathcal{T} . By plugging (7) and (4) into (5) and (6), we obtain the following expressions of the EE and GEE:

$$\mathcal{E}_{\ell}(E_{\ell},\gamma_{\ell}) = \frac{\alpha_{\ell}\gamma_{\ell}(1-q_{\ell}(G_{\ell}E_{\ell}))}{\kappa_{\ell}^{-1}\gamma_{\ell}E_{\ell}+C_{\ell}}, \quad \forall \ell,$$
(8)

$$\mathcal{G}(\mathbf{E}, \boldsymbol{\gamma}) = \frac{\sum_{\ell=1}^{L} \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell}(G_{\ell} E_{\ell}))}{\sum_{\ell=1}^{L} (\kappa_{\ell}^{-1} \gamma_{\ell} E_{\ell} + C_{\ell})},\tag{9}$$

where $C_{\ell} := (P_{ctx,\ell} + P_{crx,\ell})/B$, and $\mathbf{E} := [E_1, \cdots, E_L]$, $\boldsymbol{\gamma} := [\gamma_1, \cdots, \gamma_L]$ are the optimization variables i.e. the resource that have to be allocated to the links.

D. Assumptions on the packet error rate

For future derivations, we make now three assumptions on the PER $q_{\ell}(x)$.

Assumption 1. $q_{\ell}(x)$ is strictly convex i.e. for all x in \mathbb{R}^{+*} , $q''_{\ell}(x) > 0$.

Assumption 2. $q_{\ell}(x)$ is a strictly decreasing function on \mathbb{R}^{+*} i.e. for all x in \mathbb{R}^{+*} , $q'_{\ell}(x) < 0$.

Assumption 3. $\lim_{x\to\infty} q_\ell(x) = 0$ and $\lim_{x\to\infty} q'_\ell(x) = 0$.

In Section VII devoted to simulations, we use the PER approximation provided in [42] for the Rician fast fading channel. One can check that Assumptions 1-3 hold for this approximation.

E. Considered constraints

In this paper, we consider a QoS constraint by imposing a target minimum goodput constraint per link, denoted by $\eta_{\ell}^{(t)}$, which writes, for link ℓ :

$$B\alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}E_{\ell})) \ge \eta_{\ell}^{(t)}.$$
(10)

In addition, from the definition of the bandwidth parameter, the following inequality has to hold:

$$\sum_{\ell=1}^{L} \gamma_{\ell} \le 1. \tag{11}$$

F. Problems formulation

We address the MSEE, MGEE and MMEE problems, which write respectively as follows:

P1:
$$\max_{\mathbf{E},\gamma} \sum_{\ell=1}^{L} \frac{\alpha_{\ell} \gamma_{\ell} (1 - q_{\ell}(G_{\ell}E_{\ell}))}{\kappa_{\ell}^{-1} \gamma_{\ell} E_{\ell} + C_{\ell}}, \qquad \text{s.t. (10), (11),}$$

P2:
$$\max_{\mathbf{E},\boldsymbol{\gamma}} \quad \frac{\sum_{\ell=1}^{L} \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell}(G_{\ell}E_{\ell}))}{\sum_{\ell=1}^{L} (\gamma_{\ell}E_{\ell}\kappa_{k}^{-1} + D_{\ell})}, \qquad \text{s.t. (10), (11),}$$

P3:
$$\max_{\mathbf{E},\boldsymbol{\gamma}} \quad \min_{\ell \in \{1,\cdots,L\}} \frac{\alpha_{\ell} \gamma_{\ell} (1 - q_{\ell}(G_{\ell} E_{\ell}))}{\kappa_{\ell}^{-1} \gamma_{\ell} E_{\ell} + C_{\ell}}, \qquad \text{s.t. (10), (11)}$$

In the rest of this paper, we address the optimal resolution of Problems 1-3.

III. RESOLUTION PROCEDURE

Problems P1-P3 have no special properties like convexity and thus they cannot be directly solved with affordable complexity. To overcome this issue, we propose the following change of variables, enabling us to apply convex optimization tools to solve them: $(\gamma, \mathbf{E}) \mapsto (\gamma, \mathbf{Q})$, with $\mathbf{Q} := [Q_1, \cdots, Q_L]$, and

$$Q_{\ell} := \gamma_{\ell} E_{\ell}, \quad \forall \ell. \tag{12}$$

Using (12), constraints (10) can be rewritten as

$$\eta_{\ell}^{(0)} \le \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell})), \quad \forall \ell,$$
(13)

with $\eta_{\ell}^{(0)} := \eta_{\ell}^{(t)}/B$. Then, problems P1-P3 can be rewritten equivalently as follows:

P1':
$$\max_{\mathbf{E},\gamma} \quad \sum_{\ell=1}^{L} \frac{\alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell}))}{\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell}}, \qquad \text{s.t. (13), (11),}$$

P2':
$$\max_{\mathbf{E},\gamma} \quad \frac{\sum_{\ell=1}^{L} \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell}))}{\sum_{\ell=1}^{L} (\kappa_{\ell}^{-1}Q_{\ell} + C_{\ell})}, \qquad \text{s.t. (13), (11),}$$

P3':
$$\max_{\mathbf{E},\boldsymbol{\gamma}} \quad \min_{\ell \in \{1,\cdots,L\}} \frac{\alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell}))}{\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell}}, \qquad \text{s.t. (13), (11)}$$

We characterize P1'-P3' in the following lemma, whose proof is provided in Appendix A.

Lemma 1. The numerators of the objective functions of Problems P1' to P3' are concave, their denominators are convex and the feasible set defined by (13) and (11) is convex.

According to Lemma 1, we know that P1'-P3' (and thus P1-P3 since they are equivalent) can be optimally solved iteratively: P1' can be solved using the Jong's algorithm [43], P2' using the Dinkelbach's algorithm [44] and P3' using the generalized Dinkelbach's algorithm [45]. At each iteration, these three algorithms require to solve a convex optimization problem. The major technical contribution of this paper is to provide the optimal solution of these convex optimization problems using the so-called KKT conditions [46].

For the three problems, our resolution is organized as follows: we first express the optimal solution as a function of a single parameter, and second we find the optimal value of this parameter.

IV. MSEE PROBLEM (P1)

We apply the Jong's algorithm [43], which has been used in the RA context with EE related metrics for instance in [28], [47], [48]. At iteration i, we have to solve the following problem:

P1.1:
$$\max_{\mathbf{Q},\gamma} \sum_{\ell=1}^{L} u_{\ell}^{(i)} \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell})) - u_{\ell}^{(i)} \beta_{\ell}^{(i)} (\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell}), \qquad \text{s.t. (13), (11),}$$

where, $\forall \ell, u_{\ell}^{(i)} > 0$ and $\beta_{\ell}^{(i)} > 0$ depend on the optimal solution at iteration (i - 1).

P1.1 is the maximization of a concave function over a convex set. Hence, the KKT conditions are necessary and sufficient to find its global optimal solution [46]. Defining $\boldsymbol{\delta} := [\delta_1, \dots, \delta_L]$ and λ as the Lagrangian multipliers associated with constraints (13) and (11), respectively, the KKT conditions of P1.1 write:

$$\alpha_{\ell} G_{\ell} q_{\ell}' (G_{\ell} Q_{\ell} / \gamma_{\ell}) (u_{\ell}^{(i)} + \delta_{\ell}) + u_{\ell}^{(i)} \beta_{\ell}^{(i)} \kappa_{\ell}^{-1} = 0, \quad \forall \ell,$$
(14)

$$\alpha_{\ell}h_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell})(u_{\ell}^{(i)}+\delta_{\ell})+\lambda=0,\quad\forall\ell,$$
(15)

with $h_{\ell}(x) := -1 + q_{\ell}(x) - xq'_{\ell}(x)$. In addition, the following complementary slackness conditions hold at the optimum:

$$\delta_{\ell}(\eta_{\ell}^{(0)} - \alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell}))) = 0, \quad \forall \ell,$$
(16)

$$\lambda(\sum_{\ell=1}^{L} \gamma_{\ell} - 1) = 0.$$
(17)

To solve the optimality conditions (14)-(17), in a first time we consider the value of λ as fixed and we find the optimal solution as a function of this multiplier. In a second time, we search for the optimal value of this multiplier.

A. Resolution for fixed λ

From (14), we obtain the following L relations:

$$u_{\ell}^{(i)} + \delta_{\ell} = \frac{-u_{\ell}^{(i)} \beta_{\ell}^{(i)} \kappa_{\ell}^{-1}}{\alpha_{\ell} G_{\ell} q_{\ell}'(x_{\ell}^*(\lambda))}, \quad \forall \ell,$$

$$(18)$$

with, $\forall \ell, x_{\ell}^*(\lambda) := G_{\ell}Q_{\ell}^*(\lambda)/\gamma_{\ell}^*(\lambda)$, where $Q_{\ell}^*(\lambda)$ (resp. $\gamma_{\ell}^*(\lambda)$) is the optimal Q_{ℓ} (resp. γ_{ℓ}) for given λ . Then, by plugging (18) into (15), we get

$$g_{\ell}(x_{\ell}^*(\lambda)) = \frac{\lambda}{u_{\ell}^{(i)}\beta_{\ell}^{(i)}\kappa_{\ell}^{-1}}, \quad \forall \ell,$$
(19)

with $g_{\ell}(x) := h_{\ell}(x)/(G_{\ell}q'_{\ell}(x))$. By computing the derivative of $g_{\ell}(x)$, one can prove that it is strictly increasing, allowing us to obtain $x^*_{\ell}(\lambda)$ using (19) as:

$$x_{\ell}^{*}(\lambda) = g_{\ell}^{-1} \left(\frac{\lambda}{u_{\ell}^{(i)} \beta_{\ell}^{(i)} \kappa_{\ell}^{-1}} \right), \quad \forall \ell.$$

$$(20)$$

We can then plug this optimal value into P1.1, which can be rewritten as:

P1.2:
$$\max_{\gamma} \quad \sum_{\ell=1}^{L} \mathcal{K}_{\ell}(\lambda) \gamma_{\ell}, \text{ s.t. } \gamma_{\ell} \geq \gamma_{\ell,\min}(\lambda), \forall \ell, \quad (11),$$

with, $\forall \ell$, $\mathcal{K}_{\ell}(\lambda) := \alpha_{\ell} u_{\ell}^{(i)} (1 - q_{\ell}(x_{\ell}^{*}(\lambda))) - u_{\ell}^{(i)} \beta_{\ell}^{(i)} \kappa_{\ell}^{-1} x_{\ell}^{*}(\lambda) G_{\ell}^{-1}$ and $\gamma_{\ell,\min}(\lambda) := \eta_{\ell}^{(0)} / (\alpha_{\ell}(1 - q_{\ell}(x_{\ell}^{*}(\lambda))))$. P1.2 is a linear program depending only on the optimization variables γ . In addition, since there is only one coupling constraint (11), its optimal solution is obtained straightforwardly according to the following two possible cases.

- 1) If, $\forall \ell$, $\mathcal{K}_{\ell}(\lambda) < 0$: $\forall \ell$, $\gamma_{\ell}^*(\lambda)$, the optimal value of $\gamma_{\ell}(\lambda)$, is given by $\gamma_{\ell}^*(\lambda) = \gamma_{\ell,\min}(\lambda)$.
- 2) If, $\exists \ell$, such that $\mathcal{K}_{\ell}(\lambda) \geq 0$: let $\ell_{M,\mathcal{K}}$ be such that, for all ℓ , $\mathcal{K}_{\ell_{M,\mathcal{K}}}(\lambda) \geq \mathcal{K}_{\ell}(\lambda)$. Then, $\forall \ell \neq \ell_{M,\mathcal{K}}, \gamma_{\ell}^*(\lambda) = \gamma_{\ell,\min}(\lambda) \text{ and } \gamma_{\ell_{M,\mathcal{K}}}^*(\lambda) = 1 - \sum_{\ell \neq \ell_{M,\mathcal{K}}} \gamma_{\ell,\min}(\lambda).$

B. Search for the optimal λ

To find λ^* , the optimal value of λ , we need to identify two possibilities: either there exists ℓ such that $\delta_{\ell} = 0$, or for all ℓ , $\delta_{\ell} > 0$. In the following, we discuss these two possible cases.

Case 1: $\exists \ell$ such that $\delta_{\ell} = 0$. In the following lemma whose proof is in Appendix B, we exhibit λ^* .

Lemma 2. If there is at least one link ℓ_1 with $\delta_{\ell_1} = 0$, then we have

$$\lambda^* = -\arg\min_{\ell} \{ \alpha_{\ell} u_{\ell} h_{\ell}(x^*_{\ell,\delta_{\ell}=0}) \},$$
(21)

with $x_{\ell,\delta_{\ell}=0}^* := q_{\ell}'^{-1}(-\beta_{\ell}^{(i)}\kappa_{\ell}^{-1}/(\alpha_{\ell}G_{\ell})).$

Thanks to Lemma 2, we can optimally solve P1' solving P1.2 with low complexity. Moreover, $\exists \ell$ such that $\delta_{\ell} = 0$ constraint iff P1.1 is feasible with λ^* as defined in (21).

Case 2: $\forall \ell, \delta_{\ell} > 0$. In this case, $\gamma_{\ell}^*(\lambda)$ can be obtained more easily using (16), which gives us

$$\gamma_{\ell}^{*}(\lambda) = \frac{\eta_{\ell}^{(0)}}{1 - q_{\ell}(x_{\ell}^{*}(\lambda))}, \quad \forall \ell,$$
(22)

where $x_{\ell}^*(\lambda)$ is given by (20). Since $g_{\ell}(x)$ is strictly increasing, $x_{\ell}^*(\lambda)$ is also increasing, implying that $\gamma_{\ell}^*(\lambda)$ is strictly decreasing due to (22). To find λ^* , we use the complementary slackness condition (29). To this end, we define the following function representing the sum of the bandwidth parameters:

$$\Gamma(\lambda) := \sum_{\ell=1}^{L} \gamma_{\ell}^{*}(\lambda).$$
(23)

Since $\gamma_{\ell}^*(\lambda)$ is strictly decreasing, there are two possibilities: either $\Gamma(0) \leq 1$ and in this case $\lambda^* = 0$, or λ^* is such that $\Gamma(\lambda^*) = 1$. Hence, λ^* can be found by a one dimensional linesearch method.

C. Optimal resolution of MSEE (P1)

Gathering all the pieces together, the optimal solution of P1 is depicted in Algorithm 1, for which we define $\psi(\beta^{(i)}, \mathbf{u}^{(i)}, \boldsymbol{\gamma}, \mathbf{Q}) := [\psi_1(\beta_1^{(i)}, u_1^{(i)}, \gamma_1, Q_1), \cdots, \psi_{2L}(\beta_L^{(i)}, u_L^{(i)}, \gamma_L, Q_L)]$, with $\boldsymbol{\beta}^{(i)} := [\beta_1^{(i)}, \cdots, \beta_L^{(i)}]$ and $\mathbf{u}^{(i)} := [u_1^{(i)}, \cdots, u_L^{(i)}]$ and, for $\ell = 1, \cdots, L$:

$$\psi_{\ell}(\beta_{\ell}^{(i)}, u_{\ell}^{(i)}, \gamma_{\ell}, Q_{\ell}) := -\alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell})) + \beta_{\ell}^{(i)} (\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell}),$$
(24)

$$\psi_{\ell+L}(\beta_{\ell}^{(i)}, u_{\ell}^{(i)}, \gamma_{\ell}, Q_{\ell}) := -1 + u_{\ell}^{(i)}(\kappa_{\ell}^{-1}Q_{\ell} + C_{\ell}).$$
(25)

Algorithm 1 Optimal resolution of P1.

- 1: Set $\epsilon > 0$, i = 0, $C = \epsilon + 1$.
- 2: Initialize $\beta^{(0)}$ and $\mathbf{u}^{(0)}$.
- 3: while $C > \epsilon$ do

4: Set
$$\lambda^* = -\min_{\ell} \alpha_{\ell} u_{\ell} h_{\ell}(x^*_{\ell,\delta_{\ell}=0})$$
, where $\forall \ell, x^*_{\ell,\delta_{\ell}=0}$ is computed as indicated in Lemma 2

- 5: If P1.1 is feasible with λ^* then
- 6: Find $(\mathbf{Q}^*, \boldsymbol{\gamma}^*)$ by solving P1.2
- 7: **else**
- 8: Find $(\mathbf{Q}^*, \boldsymbol{\gamma}^*)$ using a linesearch method (case 2 in Section IV-B)
- 9: end if
- 10: Set $C = || \boldsymbol{\psi}(\boldsymbol{\beta}^{(i)}, \mathbf{u}^{(i)}, \boldsymbol{\gamma}^*, \mathbf{Q}^*) ||.$
- 11: Update $\mathbf{u}^{(i)}$ and $\boldsymbol{\beta}^{(i)}$ using the modified Newton method detailed in [28, Eqs. (33)-(34)]
- 12: i = i + 1.
- 13: end while

V. MGEE PROBLEM (P2)

The MGEE problem is a fractional programming problem, which can be solved using the Dinkelbach's algorithm [44]. This iterative algorithm has been used in numerous works dealing with RA (see [12] and reference therein), and requires to solve the following problem at the ith iteration:

P2.1: max
$$\sum_{\ell=1}^{L} (\alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} \frac{Q_{\ell}}{\gamma_{\ell}})) - \nu^{(i)} (\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell})), \text{ s.t. (13), (11),}$$

where $\nu^{(i)} \ge 0$ depends on the optimal solution of the (i-1)th iteration. Using the same notations for the Lagrangian multipliers as for the MSEE, the KKT conditions of P2.1 write as follows

$$\alpha_{\ell}G_{\ell}q_{\ell}'(G_{\ell}\frac{Q_{\ell}}{\gamma_{\ell}})(1+\delta_{\ell}) + \nu^{(i)}\kappa_{\ell}^{-1} = 0, \quad \forall \ell,$$
(26)

$$\alpha_{\ell}h_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell})(1+\delta_{\ell})+\lambda=0, \quad \forall \ell,$$
(27)

and the complementary slackness conditions are given by

$$\delta_{\ell}(\eta_{\ell}^{(0)} - \alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}\frac{Q_{\ell}}{\gamma_{\ell}}))) = 0, \quad \forall \ell,$$
(28)

$$\lambda(\sum_{\ell=1}^{L} \gamma_{\ell} - 1) = 0.$$
(29)

We observe that, if $\forall \ell$ we let $u_{\ell}^{(i)} = 1$ and $\beta_{\ell}^{(i)} = \nu^{(i)}$, then the optimality conditions of the MSEE problem i.e. (14)-(17) are the same as the ones of the MGEE problem, i.e. (26)-(29). Hence, we can apply the same procedure to solve P2.1 as the one of P1.1.

The optimal solution of P2 can be found using Algorithm 2.

VI. MMEE PROBLEM (P3)

The MMEE problem falls into the framework of generalized fractional programming, which can be efficietly handled using the so-called generalized Dinkelach's algorithm [45]. This iterative algorithm has been used in the RA context for instance in [29], and requires to solve the following convex optimization problem at the *i*th iteration:

$$\max_{\mathbf{Q},\boldsymbol{\gamma}} \qquad \min_{\ell} \left\{ \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell})) - \psi^{(i)} (\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell}) \right\},$$
(30)

s.t.
$$(13),(11),$$
 (31)

DRAFT

Algorithm 2 Optimal resolution of P2.

- 1: Set $\epsilon > 0$, $\nu^{(0)} = 0$, i = 0, $C = \epsilon + 1$
- 2: while $|\mathcal{C}| > \epsilon_D$ do
- 3: Set $\lambda^* = -\min_{\ell} \alpha_{\ell} h_{\ell}(x^*_{\ell,\delta_{\ell}=0})$, where $\forall \ell, x^*_{\ell,\delta_{\ell}=0}$ is computed as indicated in Lemma 2
- 4: If P2.1 is feasible with λ^* then
- 5: Find $(\mathbf{Q}^*, \boldsymbol{\gamma}^*)$ by solving P1.2, where for all ℓ , $u_{\ell}^{(i)}$ is replaced by 1 and $\beta_{\ell}^{(i)}$ is replaced by $\nu^{(i)}$.

6: **else**

- 7: Find $(\mathbf{Q}^*, \boldsymbol{\gamma}^*)$ using a linesearch method (case 2 in Section IV-B) where for all ℓ , $u_{\ell}^{(i)}$ is replaced by 1 and $\beta_{\ell}^{(i)}$ is replaced by $\nu^{(i)}$.
- 8: end if
- 9: Set $C = \sum_{\ell=1}^{L} \psi_{\ell}(\nu^{(i)}, 1, \gamma_{\ell}^{*}, Q_{\ell}^{*})$
- 10: Update $u^{(i+1)} = \mathcal{G}(\mathbf{Q}^*, \boldsymbol{\gamma}^*)$
- 11: i = i + 1
- 12: end while

where $\psi^{(i)} \ge 0$ depends on the optimal solution at iteration (i-1). We solve this problem using its epigraph formulation [46], i.e. we introduce an auxiliary optimization variable t along with the following L new constraints:

$$t \le \alpha_{\ell} \gamma_{\ell} (1 - q_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell})) - \psi^{(i)} (\kappa_{\ell}^{-1} Q_{\ell} + C_{\ell}), \quad \forall \ell,$$
(32)

allowing us to rewrite it equivalently as follows:

P3.1:
$$\max_{\mathbf{Q}, \gamma, t} t$$
, s.t. (13), (11), (32)

This problem is the maximization of a concave function over a convex set. Defining $\omega := [\omega_1, \cdots, \omega_L]$ as the Lagrangian multipliers associated with constraints (32) and using the same notations as in Section IV for the multipliers associated with constraints (13) and (11), the KKT conditions of P3.1 are given by

$$\sum_{\ell=1}^{L} \omega_{\ell} - 1 = 0, \tag{33}$$

$$\alpha_{\ell}G_{\ell}q_{\ell}'(G_{\ell}Q_{\ell}/\gamma_{\ell})(\omega_{\ell}+\delta_{\ell})+\omega_{\ell}\psi^{(i)}\kappa_{\ell}^{-1}=0,\quad\forall\ell,$$
(34)

$$\alpha_{\ell}h_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell})(\omega_{\ell}+\delta_{\ell})+\lambda=0,\quad\forall\ell.$$
(35)

In addition, the following complementary slackness conditions hold at the optimum:

$$\omega_{\ell}(t - \alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell})) + \psi^{(i)}(\kappa_{\ell}^{-1}Q_{\ell} + C_{\ell})) = 0, \quad \forall \ell,$$
(36)

$$\delta_{\ell}(\eta_{\ell}^{(0)} - \alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell}))) = 0, \quad \forall \ell,$$
(37)

$$\lambda(\sum_{\ell=1}^{L} \gamma_{\ell} - 1) = 0.$$
(38)

We observe an important difference between the KKT conditions related to P3.1 as compared with the ones of P1.1 and P2.1: $\forall \ell$, the optimality condition (35) involves three distinct Lagrangian multipliers, λ , ω_{ℓ} and δ_{ℓ} , preventing us to express the optimal solution of P3.1 as a function of a single multiplier. Fortunately, in the following lemma whose proof is in Appendix C, we are able to prove that constraints (11) and (32) hold with equality.

Lemma 3. At the optimum, $\lambda > 0$ and, $\forall \ell, \omega_{\ell} > 0$.

Since $\lambda > 0$, the conditions (34) and (35) can be rewritten as follows:

$$\alpha_{\ell}G_{\ell}q_{\ell}'(G_{\ell}Q_{\ell}/\gamma_{\ell})(\tilde{\omega}_{\ell}+\tilde{\delta}_{\ell})+\tilde{\omega}_{\ell}\psi^{(i)}\kappa_{\ell}^{-1}=0,\quad\forall\ell,$$
(39)

$$\alpha_{\ell} h_{\ell} (G_{\ell} Q_{\ell} / \gamma_{\ell}) (\tilde{\omega}_{\ell} + \tilde{\delta}_{\ell}) + 1 = 0, \quad \forall \ell,$$
(40)

with, for all ℓ , $\tilde{\omega}_{\ell} := \omega_{\ell}/\lambda$ and $\tilde{\delta}_{\ell} := \delta_{\ell}/\lambda$.

Thanks to Lemma 3, we can use tools from the multilevel waterfilling theory [49] to find the optimal solution of P3.1. The idea is to express parameters $x_{\ell} := G_{\ell}Q_{\ell}/\gamma_{\ell}$ (which is equal to $G_{\ell}E_{\ell}$) and γ_{ℓ} of link ℓ as a function of the single parameter t using (36). The condition (38) is then used to obtain the optimal value of t, enabling us to find the optimal values of γ_{ℓ} and x_{ℓ} , and as a consequence the optimal Q_{ℓ} and then E_{ℓ} .

Let us define $\tilde{\boldsymbol{\omega}} := [\tilde{\omega}_1, \cdots, \tilde{\omega}_L]$. We also define I_t (resp. \bar{I}_t) as the set of links with $\tilde{\delta}_\ell = 0$ (resp. $\tilde{\delta}_\ell > 0$). In the following, we first consider $\tilde{\boldsymbol{\omega}}$ as fixed, and we find the optimal values of x_ℓ and γ_ℓ for the links in I_t and \bar{I}_t as a function of t, as well as a characterization of these two sets.

A. Resolution for fixed $\tilde{\boldsymbol{\omega}}$ and t

Case 1: $\ell \in I_t$. From (39), we obtain $x_{\ell,1}^*$, the optimal value of x_ℓ , as follows:

$$x_{\ell,1}^* = q_{\ell}^{\prime-1} \left(\frac{-\psi^{(i)} \kappa_{\ell}^{-1}}{\alpha_{\ell} G_{\ell}} \right).$$
(41)

Using Lemma 3 and (36), we obtain $\gamma_{\ell,1}^*(t)$, the optimal value of γ_ℓ , depending only on t as:

$$\gamma_{\ell,1}^*(t) = \frac{t + \psi^{(i)} C_{\ell}}{\alpha_{\ell} (1 - q_{\ell}(x_{\ell,1}^*)) - \psi^{(i)} \kappa_{\ell}^{-1} G_{\ell}^{-1} x_{\ell,1}^*}.$$
(42)

The following lemma, whose proof is in Appendix D, enables us to check whether ℓ belongs to I_t or not.

Lemma 4. A link ℓ is in I_t iff the following inequality holds:

$$t \ge t_{\ell}^T, \tag{43}$$

with $t_{\ell}^T := -\psi^{(i)}C_{\ell} + \eta_{\ell}^{(0)}(1 - (\psi^{(i)}\kappa_{\ell}^{-1}G_{\ell}^{-1}x_{\ell,1}^*)/(\alpha_{\ell}(1 - q_{\ell}(x_{\ell,1}^*)))).$

Case 2: $\ell \in \overline{I}_t$.

1) Optimal solution as a function of $\tilde{\omega}_{\ell}$: Similarly to the derivations related to P1.1, using (39) and (40) we obtain $x_{\ell,2}^*(\tilde{\omega}_{\ell})$, the optimal x_{ℓ} , as follows:

$$x_{\ell,2}^*(\tilde{\omega}_\ell) := g_\ell^{-1} \left(\frac{1}{\tilde{\omega}_\ell \psi^{(i)} \kappa_\ell^{-1}} \right).$$
(44)

Since $\tilde{\delta}_{\ell} > 0$, we obtain from (37) $\gamma^*_{\ell,2}(\tilde{\omega}_{\ell})$, the optimal γ_{ℓ} , depending only on $\tilde{\omega}_{\ell}$ as:

$$\gamma_{\ell,2}^{*}(\tilde{\omega}_{\ell}) = \frac{\eta_{\ell}^{(0)}}{\alpha_{\ell}(1 - q_{\ell}(x_{\ell,2}^{*}(\tilde{\omega}_{\ell}))))}.$$
(45)

We managed to obtain the optimal values of x_{ℓ} and γ_{ℓ} for fixed $\tilde{\omega}$ and t. Now, we turn our attention to exhibit a relation between $\tilde{\omega}_{\ell}$ and t in order to express $x_{\ell,2}^*(\tilde{\omega}_{\ell})$ and $\gamma_{\ell,2}^*(\tilde{\omega}_{\ell})$ as function of t.

2) Relation between $\tilde{\omega}_{\ell}$ and t: Using Lemma 3, we obtain the following L relations by plugging (44) and (45) into (36):

$$t = \mathcal{M}_{\ell}(\tilde{\omega}_{\ell}), \quad \forall \ell, \tag{46}$$

with $\omega \mapsto \mathcal{M}_{\ell}(\omega) := \eta_{\ell}^{(0)} - \psi^{(i)}(\kappa_{\ell}^{-1}\alpha_{\ell}^{-1}x_{\ell,2}^{*}(\omega)/(1 - q_{\ell}(x_{\ell,2}^{*}(\omega))) + C_{\ell})$. To express $\tilde{\omega}_{\ell}$ as a function of t, the following lemma, whose proof is in Appendix E, is of interest.

Lemma 5. For all ℓ , the function \mathcal{M}_{ℓ} is continuous and strictly increasing, and thus \mathcal{M}_{ℓ}^{-1} exists and is strictly increasing.

Using Lemma 5 in conjunction with (46) yields

$$\tilde{\omega}_{\ell} = \mathcal{M}_{\ell}^{-1}(t), \quad \forall \ell, \tag{47}$$

and then we can obtain $\gamma_{\ell,2}^*$ as a function of t by plugging (47) into (45). As a consequence, $\gamma_{\ell,2}^*(\mathcal{M}_{\ell}^{-1}(t))$, shortened to $\gamma_{\ell,2}^*(t)$ by abuse of notation, is given by:

$$\gamma_{\ell,2}^*(t) = \frac{\eta_{\ell}^{(0)}}{\alpha_{\ell}(1 - q_{\ell}(x_{\ell,2}^*(\mathcal{M}_{\ell}^{-1}(t))))}.$$
(48)

For a given t, we succeeded to find a necessary and sufficient condition given in Lemma 4 to check whether a node belongs to I_t or \overline{I}_t , and we found the optimal parameters in both cases. Now we search for the optimal value of t.

B. Search for the optimal t

To find t^* , the optimal value of t, we use the complementary slackness condition (38). Let us define the following function representing the sum of the bandwidth parameters for given value of t

$$\tilde{\Gamma}(t) := \sum_{\ell \in I_t} \gamma_{\ell,1}^*(t) + \sum_{\ell \in \bar{I}_t} \gamma_{\ell,2}^*(t).$$
(49)

Due to (38), t^* is such that $\tilde{\Gamma}(t^*) = 1$. In the following lemma whose proof is in Appendix F, we prove such a t^* always exists, and can be found through a linesearch.

Lemma 6. The function $\tilde{\Gamma}(t)$ is continuous, strictly decreasing, and there exists t^* such that $\tilde{\Gamma}(t^*) = 1$.

The optimal solution of P3.1 can be found by solving $\tilde{\Gamma}(t^*) = 1$, which always has a solution. Then, the optimal values $x_{\ell,i}^*(t^*)$ and $\gamma_{\ell,i}^*(t^*)$, $i \in \{1, 2\}$, are computed. We deduce the optimal $Q_{\ell}^*(t^*)$.

C. Optimal resolution of P3

The optimal solution of P3 can be found using Algorithm 3.

Algorithm 3 Optimal resolution of P3.

Set ε > 0, ψ⁽⁰⁾ = 0, i = 0, t* = ε + 1
 while t* > ε do
 Compute t*, Q* and γ* by solving P3.1 with ψ⁽ⁱ⁾.
 Update ψ⁽ⁱ⁺¹⁾ = min_{ℓ∈{1,...,L}} E_ℓ(Q^{*}_ℓ/γ^{*}_ℓ, γ^{*}_ℓ).
 i = i + 1.

6: end while

VII. NUMERICAL EXAMPLES

In this section, the results of the proposed algorithms are numerically studied. First, we compare the performance of the proposed criteria under both the Rayleigh and the Rician channel. Second, we investigate the benefits of considering the Rician channel instead of the conventional Rayleigh channel. Finally, we study possible extension of the proposed criterion to type-II HARQ. We also compare the proposed criteria with the minimum power (MPO) from [42], which minimizes the total transmit power.

We use the convolutional code with generator polynomial $[171, 133]_8$, and we use the quadrature phase shift keying (QPSK) modulation, i.e. $m_{\ell} = 2$. The number of link is L = 5 and the link distances D_{ℓ} are uniformly drawn in [50 m, 1 km]. We consider that all the links have identical Kfactor value. We simulate both Rician channel with $K_{\ell} = 10$ and Rayleigh channel with $K_{\ell} = 0$. We set B = 5 MHz, $N_0 = -170$ dBm/Hz and $\mathcal{L}_{\ell} = 128$. The carrier frequency is $f_c = 2400$ MHz and we put $\zeta_{\ell}^2 = (4\pi f_c/c)^{-2} D_{\ell}^{-3}$ where c is the celerity of light in vacuum. We assume that the required goodput per link is equal for all links. We put $\forall \ell$, $P_{ctx,\ell} = P_{crx,\ell} = 0.05$ W and $\kappa_{\ell} = 0.5$. We use the approximation of the PER provided and validated through simulations in [42] to perform the RA.

A. Performance of the proposed algorithms

In Figs. 1-3, we plot the SEE, MEE and GEE obtained with the proposed criteria and with the MPO versus the minimum required goodput. We perform the optimal RA according to the links channel distribution: Rayleigh RA under Rayleigh channel and Rician RA under Rician channel. As expected, the maximization of a given criterion yields the highest value for this criterion.

The proposed criteria yield higher EE than the MPO, especially for low goodput constraint. In addition, due to the LoS component, the performance under the Rician channel are much higher than those obtained under the Rayleigh channel.

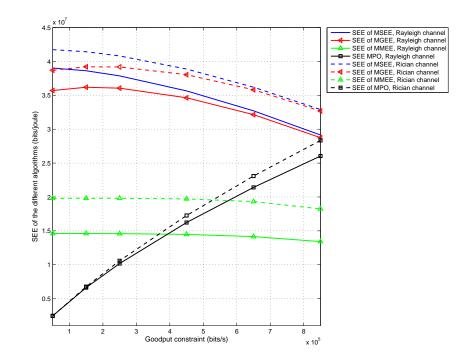


Fig. 1: SEE obtained for the considered criteria versus the minimum goodput constraint.

To illustrate the influence of the channel model mismatch on the RA, we have simulated the EE metrics under the Rician channel in two cases: a) the RA is performed assuming a Rayleigh channel (i.e. $K_{\ell} = 0$) and b) the RA is performed knowing the true Rician channel (i.e. $K_{\ell} = 10$). To evaluate this mismatch, we define \mathbf{E}_R^* and γ_R^* as the optimal values of E and γ when the Rician channel model is considered ($K_{\ell} = 10$). We also define \mathbf{E}_C^* and γ_C^* as the optimal values of E and γ when considering the Rayleigh channel ($K_{\ell} = 0$). In Fig. 4, we plot the EE gains between the Rician and the Rayleigh allocations under the Rician channel by computing $100 \times (\mathcal{Z}_R(\mathbf{E}_R^*, \gamma_R^*) - \mathcal{Z}_R(\mathbf{E}_C^*, \gamma_C^*))/\mathcal{Z}_R(\mathbf{E}_C^*, \gamma_C^*)$, where \mathcal{Z}_R stands for either the SEE, the MEE or the GEE versus the minimum goodput constraint calculated under the Rician channel with $K_{\ell} = 10$. We observe that substantial gains can be achieved for all the criteria, and especially for the MMEE. It is thus beneficial to incorporate the knowledge of the Rician

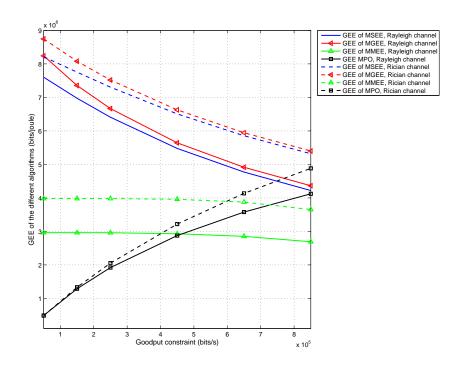


Fig. 2: GEE obtained for the considered criteria versus the minimum goodput constraint.

K-factor in the RA.

B. Application to type-II HARQ

We did not succeed to identify specific properties such as convexity enabling us to find the optimal solution for EE based RA problems for type-II HARQ under the Rician channel. Therefore, we propose to investigate the performance obtained when using type-I HARQ Rician RA on type-II HARQ, which leads to a mismatch on the HARQ type. We also propose an alternative way by considering a mismatch on the channel model where the RA is obtained when using type-II HARQ under the Rayleigh channel [41]. We focus on the MSEE as in [41].

Let $\mathbf{E}_{\mathrm{I}}^{*}$ and γ_{I}^{*} be the optimal values of \mathbf{E} and γ when considering type-I HARQ under the Rician channel. These values are obtained using the Algorithm 1. Let $\mathbf{E}_{\mathrm{II}}^{*}$ and γ_{II}^{*} be the optimal values of \mathbf{E} and γ when considering type-II under the Rayleigh channel. These values are obtained using the algorithm described in [41].

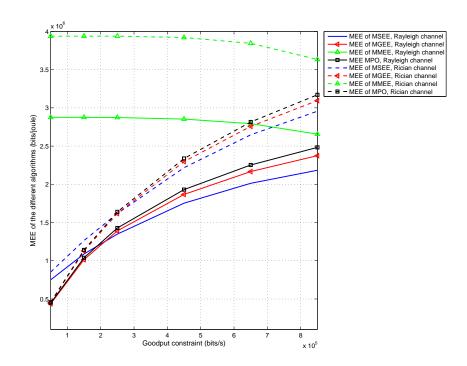


Fig. 3: MEE obtained for the considered criteria versus the minimum goodput constraint.

When type-II HARQ is simulated, the SEE is given by

$$S(\mathbf{E}, \boldsymbol{\gamma}) := \sum_{\ell=1}^{L} \tilde{\mathcal{E}}_{\ell}(E_{\ell}, \gamma_{\ell})$$

with [41]:

$$\tilde{\mathcal{E}}_{\ell}(E_{\ell},\gamma_{\ell}) := \frac{\alpha_{\ell}\gamma_{\ell}(1-q_{\ell,\mathcal{T}}(G_{\ell}E_{\ell}))}{(1+\sum_{t=1}^{\mathcal{T}-1}q_{\ell,t}(G_{\ell}E_{\ell}))(\kappa_{\ell}^{-1}\gamma_{\ell}E_{\ell}+C_{\ell})},\tag{50}$$

where $q_{\ell,t}$ is the probability that the first t transmissions are all received in error.

In order to compare the different RA, we plot $S(\mathbf{E}_{\mathrm{I}}^{*}, \gamma_{\mathrm{I}}^{*})$ and $S(\mathbf{E}_{\mathrm{II}}^{*}, \gamma_{\mathrm{II}}^{*})$ in Fig. 5, where we consider that, $\forall \ell, K_{\ell} = 10$. The considered type-II HARQ is chase combining (CC) with $\mathcal{T} = 3$. As we observe that $S(\mathbf{E}_{\mathrm{I}}^{*}, \gamma_{\mathrm{I}}^{*})$ is much higher than $S(\mathbf{E}_{\mathrm{II}}^{*}, \gamma_{\mathrm{II}}^{*})$ whatever the goodput constraint, we advocate a type mismatch approach rather than a channel mismatch approach to perform suboptimal type-II RA under the Rician channel.

VIII. CONCLUSION

In this paper, we addressed the problem of joint bandwidth and power allocation for type-I HARQ with practical MCS and statistical CSI under the Rician channel by providing the

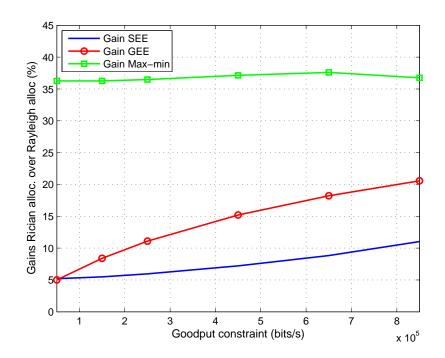


Fig. 4: Gains between the Rician and the Rayleigh allocations under the Rician channel, versus the per-link minimum goodput constraint.

analytical optimal solution of three RA problems: the MSEE, the MMEE and the GEE. Through simulations, we exhibited that substiantial gains can be achieved by taking into account the existence of a LoS between the transmitter and the receiver instead of only considering the channel variance. We also studied the behaviour of our proposed algorithms when applied on type-II HARQ. Numerical results indicated that, when the channel is Rician distributed, it is more beneficial to apply the RA corresponding to type-I HARQ for the Rician channel instead of the type-II RA for the Rayleigh channel.

APPENDIX A

PROOF OF LEMMA 1

First, let us prove that the feasible set defined by constraints (11) and (13) is convex. Constraint (11) is linear and as a consequence it is convex. Moreover, $\gamma_{\ell}(1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell}))$ is the so called perspective [46] of the concave function $1 - q_{\ell}(G_{\ell}E_{\ell})$ and thus it is concave, meaning that constraint (13) is convex.

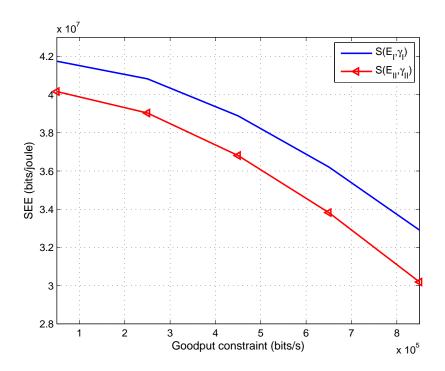


Fig. 5: SEE obtained for the considered criteria versus the minimum goodput constraint.

Second, let us focus on the objective functions of P1'-P3'. We remark that there denominators are linear and thus they are convex. The numerators of the objective functions of P1' and P2' are given by $\alpha_{\ell}\gamma_{\ell}(1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell}))$ and hence they are concave as the perspective of concave functions. For P3', the numerator is given by $\sum_{\ell=1}^{L} \alpha_{\ell}(\gamma_{\ell}(1 - q_{\ell}(G_{\ell}Q_{\ell}/\gamma_{\ell})))$ and then it is concave as a sum of concave functions.

APPENDIX B

PROOF OF LEMMA 2

First due to (15), we are only interested in solutions yielding non positive values for h_{ℓ} . If there exists at least one link ℓ_1 with $\delta_{\ell_1} = 0$, we obtain the optimal value of x_{ℓ_1} using (14) as:

$$x_{\ell_1}^* = x_{\ell_1,\delta_{\ell_1}=0}^* = q_{\ell_1}^{\prime-1} \left(\frac{-\beta_{\ell_1}^{(i)} \kappa_{\ell_1}^{-1}}{\alpha_{\ell_1} G_{\ell_1}} \right).$$
(51)

By plugging (51) into (15), we obtain the optimal value of λ as:

$$\lambda^* = -\alpha_{\ell_1} u_{\ell_1}^{(i)} h_{\ell_1}(x_{\ell_1,\delta_{\ell_1}=0}^*) \ge 0.$$
(52)

Hence, we prove that $\ell_1 \in \arg \min_{\ell} \{ \alpha_{\ell} u_{\ell}^{(i)} h_{\ell}(x_{\ell,\delta_{\ell}=0}) \}$. To do so, we proceed by contradiction: we assume that $\exists \ell_2$ such that $\alpha_{\ell_2} u_{\ell_2}^{(i)} h_{\ell_2}(x_{\ell_2,\delta_{\ell_2}=0}^*) < \alpha_{\ell_1} u_{\ell_1}^{(i)} h_{\ell_1}(x_{\ell_1,\delta_{\ell_1}=0}^*)$, and we prove that the KKT condition (15) cannot hold for ℓ_2 . This condition writes as follows:

$$\alpha_{\ell_2} u_{\ell_2}^{(i)} h_{\ell_2}(x_{\ell_2}^*) (u_{\ell_2}^{(i)} + \delta_{\ell_2}) - \alpha_{\ell_1} u_{\ell_1}^{(i)} h_{\ell_1}(x_{\ell_1,\delta_{\ell_1}=0}^*) = 0.$$
(53)

To prove that (53) cannot hold, we upper bound it by a term stricly lower than 0. To this end, the following proposition is of interest.

Proposition 1. For all ℓ , the following inequality holds:

$$h_{\ell}(x_{\ell}^{*}) \le h_{\ell}(x_{\ell,\delta_{\ell=0}}^{*}).$$
 (54)

Proof: First, let us study the monotonicity of $h_{\ell}(x)$ by computing its first order derivative:

$$h'_{\ell}(x) = -xq''_{\ell}(x).$$
(55)

Due to the strict convexity of q_{ℓ} , it results from (55) that h_{ℓ} is strictly decreasing.

Second, let us compare x_{ℓ}^* with $x_{\ell,\delta_{\ell=0}}^*$. From (14), we have

$$x_{\ell}^{*} = q_{\ell}^{\prime-1} \left(\frac{-u_{\ell}^{(i)} \beta_{\ell}^{(i)} \kappa_{\ell}^{-1}}{\alpha_{\ell} G_{\ell} (u_{\ell}^{(i)} + \delta_{\ell})} \right),$$
(56)

since $q_{\ell}^{\prime-1}$ is increasing, the following inequality holds

$$x_{\ell}^* \ge x_{\ell,\delta_{\ell}=0}^*. \tag{57}$$

Finally, the proof is completed using (55).

Using Proposition 1 we can upper bound (53) as follows

$$\alpha_{\ell_2} u_{\ell_2}^{(i)} h_{\ell_2}(x_{\ell_2}^*) (u_{\ell_2}^{(i)} + \delta_{\ell_2}) - \alpha_{\ell_1} u_{\ell_1}^{(i)} h_{\ell_1}(x_{\ell_1,\delta_{\ell_1}=0}^*) \le$$

$$(58)$$

$$\alpha_{\ell_2} u_{\ell_2}^{(i)} h_{\ell_2}(x_{\ell_2,\delta_{\ell_2}=0}^*) (u_{\ell_2}^{(i)} + \delta_{\ell_2}) - \alpha_{\ell_1} u_{\ell_1}^{(i)} h_{\ell_1}(x_{\ell_1,\delta_{\ell_1}=0}^*).$$

Since by hypothesis, $\alpha_{\ell_2} u_{\ell_2} h_{\ell_2}(x^*_{\ell_2,\delta_{\ell_2}=0}) < \alpha_{\ell_1} u_{\ell_1} h_{\ell_1}(x^*_{\ell_1,\delta_{\ell_1}=0}), \ \alpha_{\ell_1} u_{\ell_1} h_{\ell_1}(x^*_{\ell_1,\delta_{\ell_1}=0}) = -\lambda^* \le 0$ and $\delta_{\ell_2} \ge 0$ we obtain from (58)

$$\alpha_{\ell_2} u_{\ell_2}^{(i)} h_{\ell_2}(x_{\ell_2}^*) (u_{\ell_2}^{(i)} + \delta_{\ell_2}) - \alpha_{\ell_1} u_{\ell_1}^{(i)} h_{\ell_1}(x_{\ell_1,\delta_{\ell_1}=0}^*) < 0.$$
(59)

Due to (59), the KKT condition (15) cannot hold for link ℓ_2 yielding a contradiction.

APPENDIX C

PROOF OF LEMMA 3

First, let us prove that $\lambda > 0$. We need the following intermediate result.

Proposition 2. At any iteration *i*, the optimal *t* is such that $t \ge 0$.

Proof: The proof is similar to the one of [45, Proposition 2] and is thus omitted.

The rest of the proof is by contradiction: we assume that $\lambda = 0$, and we prove that it yields a strictly negative value for t, which contradicts Proposition 2. To do so, we remark from (33) that $\sum_{\ell=1}^{L} \omega_{\ell} = 1$, meaning that $\exists \ell$ such that $\omega_{\ell} > 0$. Let us focus on this link. We consider the following two possible cases: either $\delta_{\ell} = 0$ or $\delta_{\ell} > 0$.

Case 1: $\delta_{\ell} = 0$. Using (34) and (35), we obtain:

$$\alpha_{\ell}(q_{\ell}(x_{\ell}) - 1) + \frac{x_{\ell}\kappa_{\ell}^{-1}\psi^{(i)}}{G_{\ell}} = 0,$$
(60)

with $x_{\ell} := G_{\ell}Q_{\ell}/\gamma_{\ell}$. In addition, since $\omega_{\ell} > 0$, plugging (60) into (36) yields

$$t = \gamma_{\ell}(\alpha_{\ell}(1 - q_{\ell}(x_{\ell})) - \frac{x_{\ell}\psi^{(i)}\kappa_{\ell}^{-1}}{G_{\ell}}) - \psi^{(i)}C_{\ell} = -\psi^{(i)}C_{\ell} < 0.$$
(61)

 $\langle \alpha \rangle$

Case 2: $\delta_{\ell} > 0$. The condition (34) gives us:

$$\alpha_{\ell}(-1 + q_{\ell}(x_{\ell}) - x_{\ell}q'_{\ell}(x_{\ell})) = 0.$$
(62)

Since $\delta_{\ell} > 0$, we obtain:

$$\gamma_{\ell} = \frac{\eta_{\ell}^{(0)}}{\alpha_{\ell}(1 - q_{\ell}(x_{\ell}))}.$$
(63)

By plugging (62) and (63) into (36), we obtain

$$t = \eta_{\ell}^{(0)} \left(1 + \frac{\psi^{(i)} \kappa_{\ell}^{-1}}{\alpha_{\ell} G_{\ell} q_{\ell}'(x_{\ell})} \right) - \psi^{(i)} C_{\ell}.$$
 (64)

To upper bound (64), we use (35) which gives us

$$\frac{\psi^{(i)}\kappa_{\ell}^{-1}}{\alpha_{\ell}G_{\ell}q_{\ell}'(x_{\ell})} < -1.$$
(65)

Using (65) into (64) yields t < 0.

Gathering case 1 and case 2 together, we obtain that $\lambda = 0$ yields t < 0, contradicting Proposition 2. Hence, we deduce that $\lambda > 0$.

Now, let us prove that, $\forall \ell$, $\omega_{\ell} > 0$. Assume that there exists ℓ such that $\omega_{\ell} = 0$. We can see from (34) that $\delta_{\ell} = 0$. However, plugging $\omega_{\ell} = 0$ and $\delta_{\ell} = 0$ into (35) implies $\lambda = 0$, which contradicts $\lambda > 0$. Hence, for all ℓ , $\omega_{\ell} > 0$ which concludes the proof.

APPENDIX D

PROOF OF LEMMA 4

First, assume that a link ℓ belongs to I_t . Its optimal values for x_ℓ and γ_ℓ are given by (41) and (42), respectively. Moreover, ℓ has to satisfy its goodput constraint (13). By plugging (41) and (42) into (13), the direct part of Lemma 4 is proved.

Second, we prove the converse part of Lemma 4 by contradiction: assuming that there exists a link ℓ such that inequality (43) holds and which is not in I_t , we prove that the optimality condition (37) cannot hold. Let us define $x_{\ell,2}^*(\delta_\ell)$ (resp. $\gamma_{\ell,2}^*(\delta_\ell, t)$) the optimal value of x_ℓ (resp. γ_ℓ) for fixed ω_ℓ and t. Notice that $x_{\ell,2}^*(0)$ (resp. $\gamma_{\ell,2}(0,t)$) coincides with $x_{\ell,1}^*$ (resp. $\gamma_{\ell,1}^*(t)$). With these notations, (43) can be rewritten as follows:

$$\eta_{\ell}^{(0)} \le \alpha_{\ell} \gamma_{\ell,2}^*(0,t) (1 - q_{\ell}(x_{\ell,2}^*(0))).$$
(66)

Since $\delta_{\ell} > 0$, (37) yields:

$$\eta_{\ell}^{(0)} = \alpha_{\ell} \gamma_{\ell,2}^*(\delta_{\ell}, t) (1 - q_{\ell}(x_{\ell,2}^*(\delta_{\ell}))).$$
(67)

To arrive at a contradiction, the following proposition is of interest.

Proposition 3. For all $\delta_{\ell} > 0$ and for all ℓ , the following inequalities hold:

$$x_{\ell,2}^*(\delta_\ell) > x_{\ell,2}^*(0) \tag{68}$$

$$\gamma_{\ell,2}^*(\delta_{\ell}, t) > \gamma_{\ell,2}^*(0, t) \tag{69}$$

Proof: We start by proving (68). Using (40), we obtain

$$x_{\ell,2}^*(\delta_\ell) = q_\ell^{\prime-1} \left(\frac{-\omega_\ell \psi^{(i)} \kappa_\ell^{-1}}{\alpha_\ell G_\ell(\omega_\ell + \delta_\ell)} \right).$$
(70)

Since $q_{\ell}^{\prime-1}$ is continuous, differentiable with non zero derivative and strictly increasing, $x_{\ell,2}^*(\delta_{\ell})$ is a continuous, differentiable and strictly increasing function of δ_{ℓ} , which proves (68).

Now, let us focus on $\gamma_{\ell,2}^*(\delta_\ell, t)$. Using Lemma 3, we can obtain:

$$\gamma_{\ell,2}^*(\delta_\ell, t) = \frac{t + \psi^{(i)}C_\ell}{f_\ell(\delta_\ell)},\tag{71}$$

with $f_{\ell}(\delta_{\ell}) := \alpha_{\ell}(1 - q_{\ell}(x_{\ell,2}^*(\delta_{\ell})) - \psi^{(i)}\kappa_{\ell}^{-1}G_{\ell}^{-1}x_{\ell,2}^*(\delta_{\ell}))$. To prove (69), let us prove that $f_{\ell}(\delta_{\ell})$ is strictly decreasing by computing its derivative:

$$f'_{\ell}(\delta_{\ell}) = -x^{*'}_{\ell,2}(\delta_{\ell})g_{\ell}(\delta_{\ell}),\tag{72}$$

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with $x_{\ell,2}^{*'}(\delta_{\ell}) > 0$ the derivative of $x_{\ell,2}^{*}(\delta_{\ell})$ with respect to δ_{ℓ} , and $g_{\ell}(\delta_{\ell}) := (\alpha_{\ell}q'_{\ell}(x_{\ell,2}^{*}(\delta_{\ell})) + \psi^{(i)}\kappa_{\ell}^{-1}G_{\ell}^{-1})$. Using (70), we can see that $g_{\ell}(0) = 0$, meaning that $f'_{\ell}(0) = 0$. In addition, we can prove that $g_{\ell}(\tilde{\delta}_{\ell})$ is strictly increasing by computing its derivative, meaning that, for all $\tilde{\delta}_{\ell} > 0$, $g_{\ell}(\delta_{\ell}) > 0$ which, together with (72) concludes the proof.

Using Proposition 3, we hence have, for all $\delta_{\ell} > 0$:

$$\alpha_{\ell}\gamma_{\ell,2}^{*}(\delta_{\ell},t)(1-q_{\ell}(x_{\ell,2}^{*}(\delta_{\ell}))) > \alpha_{\ell}\gamma_{\ell,2}^{*}(0,t)(1-q_{\ell}(x_{\ell,2}^{*}(0))) \ge \eta_{\ell}^{(0)},\tag{73}$$

which contradicts (67) and concludes the proof.

APPENDIX E

PROOF OF LEMMA 5

It is sufficient to prove that $\mathcal{F}_{\ell}(\omega_{\ell}) := x_{\ell,2}^*(\omega_{\ell})/(1 - q_{\ell}(x_{\ell,2}^*(\omega_{\ell})))$ is strictly decreasing. Let us compute the derivative of $\mathcal{F}_{\ell}(\omega_{\ell})$:

$$\mathcal{F}'_{\ell}(\omega_{\ell}) = -\frac{x_{\ell,2}^{*'}(\omega_{\ell})h_{\ell}(x_{\ell,2}^{*}(\omega_{\ell}))}{(1 - q_{\ell}(x_{\ell,2}^{*}(\omega_{\ell})))^2}$$
(74)

where $x_{\ell,2}^{*'}(\omega_{\ell}) = -1/(\omega_{\ell}^2 \psi^{(i)} \kappa_{\ell}^{-1})(g_{\ell}^{-1})'(\omega_{\ell}^{-1} \kappa_{\ell}/\psi^{(i)}) < 0$. Moreover, due to (40), we are only interested in the values of $x_{\ell,2}^{*'}(\omega_{\ell})$ such that $h(\omega_{\ell}) < 0$. As a consequence, $\mathcal{F}_{\ell}(\omega_{\ell})$ is strictly decreasing and hence $\mathcal{M}_{\ell}(\omega_{\ell})$ is strictly increasing, which concludes the proof.

APPENDIX F

PROOF OF LEMMA 6

Let us define k'_m a one-to-one mapping from $\{1, \dots, L\}$ in itself such that $t^T_{k'_1} \leq \cdots \leq t^T_{k'_L}$ where $t^T_{k'_i}$ is defined in (43). To prove Theorem 6, we first observe that the first term in the right hand side (RHS) of $\tilde{\Gamma}(t)$ is continuous and strictly increasing on every open set $(t^T_{k'_i}, t^T_{k'_{i+1}})$. Second, let us prove that the second term is also strictly increasing. To this end, we remind that $\gamma^*_{\ell,2}(t)$ is expressed as

$$\gamma_{\ell,2}^*(t) = \frac{\eta_{\ell}^{(0)}}{\alpha_{\ell}(1 - q_{\ell}(x_{\ell,2}^*(\mathcal{M}_{\ell}^{-1}(t))))}.$$
(75)

Since $\mathcal{M}_{\ell}^{-1}(t)$ is strictly increasing and $x_{\ell,2}^*(\tilde{\omega}_{\ell})$ is strictly decreasing, we infer that $1-q_{\ell}(x_{\ell,2}^*(\mathcal{M}_{\ell}^{-1}(t)))$ is decreasing and as a consequence $\gamma_{\ell,2}^*(t)$ is strictly increasing. Third, it can be checked that $\tilde{\Gamma}(t)$ is continuous in every $t_{k'_{\ell}}^T$ by checking that $\lim_{t \neq t_{k'}^T} \tilde{\Gamma}(t) = \lim_{t \geq t_{k'_{\ell}}} \tilde{\Gamma}(t)$. Finally, by letting \tilde{t} be sufficiently small, one can show that that $\gamma_{\ell,2}^*(t)$ goes to $\eta_{\ell}^{(0)}/\alpha_{\ell}$, and we have $\sum_{\ell=1}^{L} \eta_{\ell}^{(0)}/\alpha_{\ell} \leq 1$ (otherwise the problem would be infeasible). Moreover, when t is sufficiently large, it is clear that $\tilde{\Gamma}(t) > 1$. Hence, there exists t^* such that $\tilde{\Gamma}(t^*) = 1$, which concludes the proof.

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