

# Static Scheduling for Time-Predictable Networks-on-Chip

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This work is partially supported by the EC project T-CREST.



# The T-CREST Platform

Design of a time-predictable multi-core platform

- Simplify calculation of WCET bounds
- Explore WCET-driven system design and optimization

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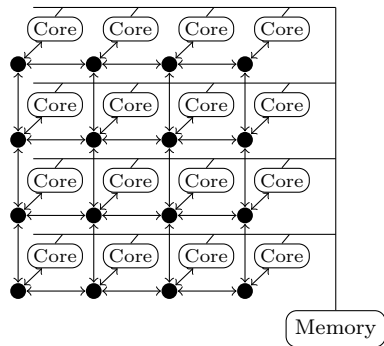
- Simplify calculation of WCET bounds
- Explore WCET-driven system design and optimization
- Project scope
  - Processor / Chip-multi-processor (DTU)
  - Memory hierarchy (U. York, TU/e)
  - **Network-on-Chip (DTU)**
  - Compiler (DTU, Vienna UT)
  - WCET analysis (Absint)
  - Use cases (GMV, Intecs)

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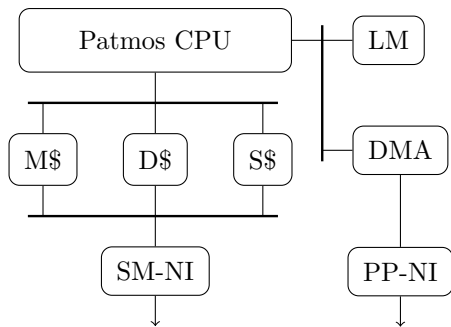
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- Project mantra  
Evaluate everything with regard to WCET analyzability.

# Platform Overview

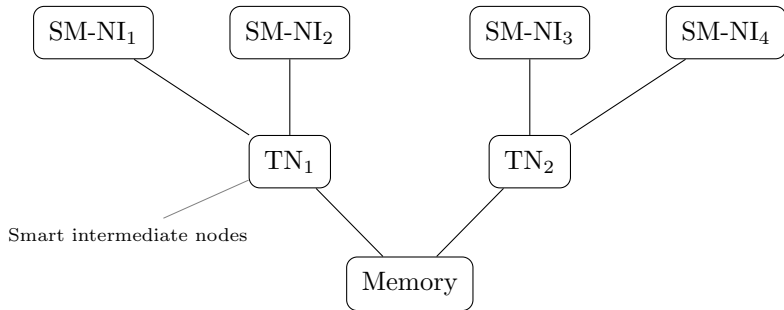


(a) Overall Platform



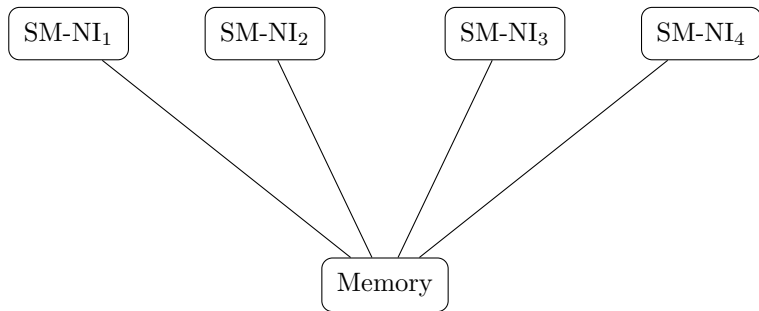
(b) Processing Core

## Shared Memory – Tree



Work-preserving tree

## Shared Memory – Serial Lines



Point-to-point serial lines

# Point-to-Point Communication

Realized using a Network-on-Chip (NoC)

- Consisting of several Patmos cores
- Each core is connected to a router
- Routers interconnected by links
- DMA-based point-to-point exchange of messages



# Time-predictable Networks-on-Chip

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# Time-predictable Networks-on-Chip

Why is there a problem in real-time systems?

- The NoC is shared by **all** nodes
- Plenty of interaction between nodes through the network
- WCET analysis for one task depends on
  - Nodes involved in the completion of the task
  - Message delivery times between involved nodes

**All nodes of the NoC have to be analyzed**

## Make it time-predictable ...

Two options

1. Guarantee throughput by buffering
2. Guarantee exclusive access by arbitration

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Buffers:

- Incur hardware overhead
- How determine buffer sizes?
- How determine bandwidth per router/link?
- Requirements are application-specific
- Not suited for a generic, cost-effective platform

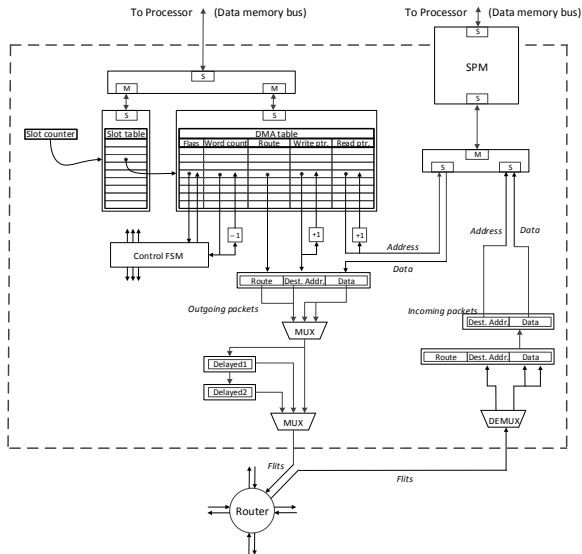
# The T-CREST NoCs

- S4
  - Simple, Stupid, Small, ...
  - Minimal NoC aiming at all-to-all communication
  - Fully synchronous design
- Argo
  - Globally asynchronous locally synchronous (GALS) design
  - Asynchronous handshaking at link-level
  - Implicit *clock* driven by message injection

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  - Implicit *clock* driven by message injection
- Common ideas
  - Time-division multiplexing at all levels of the NoC
  - TDM at Network Interfaces (NI)
  - TDM on NoC links and routers

# The T-CREST Network Interface



# The S4 Design

## Minimalistic time-multiplexed NoC

- Fixed, static schedules  
providing periodic, all-to-all communication



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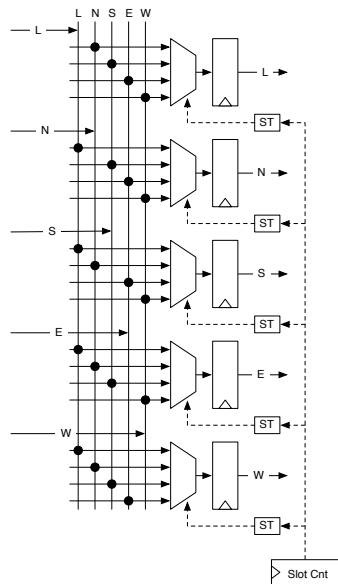
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- Guarantees
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  - Separation of independent tasks
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- Time-multiplexing of routers and links
- Guarantees
  - Fixed, well-known timing
  - Separation of independent tasks
  - Analyzability of worst-case behavior
- Minimal hardware requirements
  - Routers are simple multiplexers
  - Static schedule tables at routers

# The S4 Router



- A multiplexer and a register per out-going link
  - L connects the router to its node
  - N to the *north* neighbor
  - ...
- One in-coming/out-going link per direction
- Word-sized link width (e.g., 16 bits)
- Schedule table (ST) controls multiplexers

# Schedule Construction

## Some assumptions

- Every node sends one message to every other node
- Every node receives one message from every other node
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- Message = packet = flit = phit = 1 data word
- A hop from one router to the next takes one cycle
- Network given as a graph  $G = (N \cup R, E)$   
 $N$  ... nodes,  $R$  ... router,  $E$  ... links



## Schedule Construction (2)

Solve a multi-commodity flow problem over time:

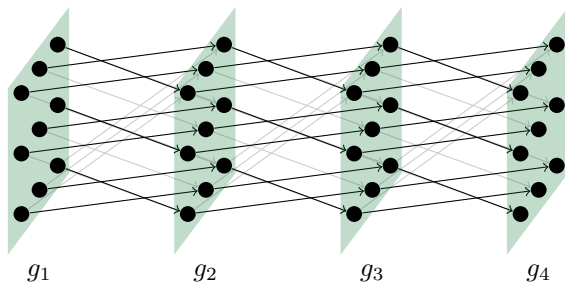
- Commodities correspond to messages
- Minimize time to deliver all commodities/messages

## Schedule Construction (2)

Solve a multi-commodity flow problem over time:

- Commodities correspond to messages
- Minimize time to deliver all commodities/messages
- Modeled as Integer Linear Program (ILP)
  - Given a network  $G$  construct a time-expanded network  $G^T$
  - $G^T$  consists of copies of  $G$ :  $g_1, \dots, g_T$
  - Edges lead from some copy  $g_i$  to  $g_{i+1}$
  - Solve a standard flow problem on  $G^T$

## Example: Time-Expanded $3 \times 3$ Torus



The time-expanded network represents the state of the NoC on all time instants during the schedule construction.

# Structure of the Linear Program

## Variables

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All messages flowing into a router have to flow out again.

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All messages flowing into a router have to flow out again.
- $\sum_{l \in In(n,t)} \ell_{l,n}^t = |N| - 1$   
Receive a message from every other node.
- $\sum_{l \in Out(s,t)} \ell_{l,d}^t = 1$   
Send once from source node  $s$  to destination node  $d$ .



# Solving the Linear Program

Using a generic ILP solver

- CPLEX 12.3 academic
- DTU's hms2 server  
8 Quad-Core AMD Opteron 8356 (32 cores), 256 GB RAM

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(no initial solution, generous upper bound for schedule length)
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- Network sizes of up to 25 nodes feasible  
(no initial solution, generous upper bound for schedule length)
  - Topologies: mesh, torus, bidir. torus (also: tree, fat-tree)
- Considerable improvements possible

## Some results

Topology	Nodes	Routers	Links	Schedule Length
Mesh	4	4	8+8	5
	9	9	24+18	10
	16	16	48+32	18
	25	25	80+50	34
Torus	4	4	8+8	5
	9	9	18+18	11
	16	16	32+32	26
	25	25	50+50	54*
Bidir. Torus	4	4	16+8	4
	9	9	36+18	10
	16	16	64+32	18
	25	25	100+50	27

\* DNF ... (lower bound from CPLEX: 52)

# Dealing with Larger Networks

## Observations from ILP solutions

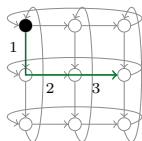
- Paths taken for message routes
  - One straight horizontal or vertical segment, or
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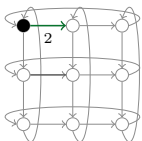
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- Paths taken for message routes
  - One straight horizontal or vertical segment, or
  - One horizontal and one vertical segment (X-Y, Y-X)
  - No detours, shortest routes only
- We can exploit regularities of network topologies
  - Construct symmetric schedules
  - Synchronize all routers
  - Use the same schedule table everywhere

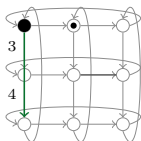
# Example: Partial, Optimal Solution for the $3 \times 3$ -Torus



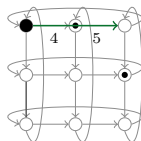
Step 1



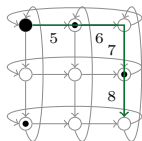
Step 2



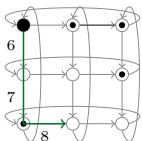
Step 3



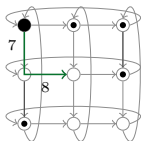
Step 4



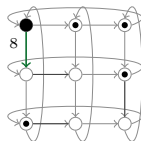
Step 5



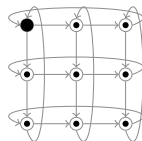
Step 6



Step 7



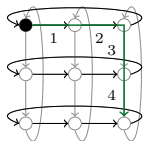
Step 8



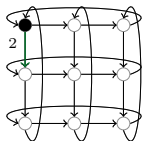
Step 9

This schedule cannot be replicated everywhere,  
due to conflicts, e.g., at cycle 2.

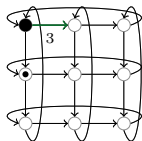
# Example: Symmetric Solution for the $3 \times 3$ -Torus



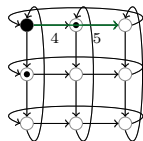
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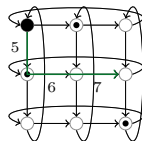
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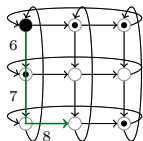
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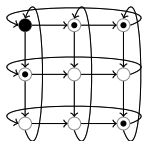
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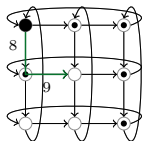
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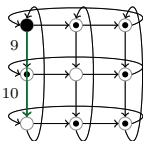
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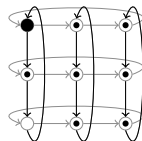
Step 7



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Step 10

**This schedule can be replicated everywhere.**



# A Heuristic Algorithm

Some assumptions

- Schedule relative to **one** reference node, then replicate
  - Restrict paths considered as routes
  - Only shortest routes from reference node
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  - **Yes**: torus, bidirectional torus, ...
  - So-so: 2D-mesh
  - **No**: tree, fat-tree, star, ...
- As before
  - all-to-all communication
  - single-cycle hops
  - Message = 1 flit = 1 word

## A Heuristic Algorithm (2)

1. Compute set of candidate routes
  - Set of routes from the reference node to all other nodes
  - Example: shortest, X-Y and Y-X routes
2. Select a *good* candidate
  - Example: a longest remaining route
3. Schedule the candidate route
  - Avoid conflicts with already scheduled routes
  - Example: schedule as early as possible
4. Remove all *equivalent* candidate routes
5. Repeat step 2-4 until no candidate route remains

# Routes and Conflicts

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- Routes are equivalent when they lead to the same target node  
Example: eesss  $\equiv$  sssee

# Experiments

Several heuristic configurations

- Implemented in C++ (relatively untuned)



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- Network size up to 900 nodes
  - Network topologies: torus, bidirectional torus (also: mesh)
- Compare schedule lengths and execution times
  - Theoretical bounds: network capacity, bisection bandwidth
  - Optimal results (as far as available)

# Configurations

## Candidate selection

- Sht: Shortest routes first
- Rnd: Select random route
- Lng: Longest routes first
- Cnfl: Longest routes first, avoid conflict with last candidate

# Configurations

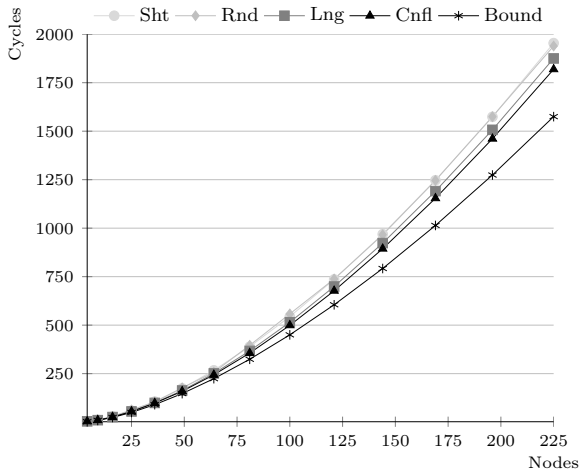
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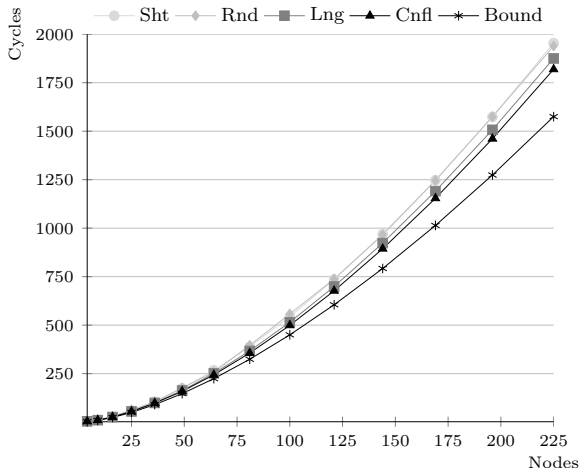
## Scheduling

- Schedule as early as possible
- Naive checking for conflicts

# Schedule Lengths – Torus

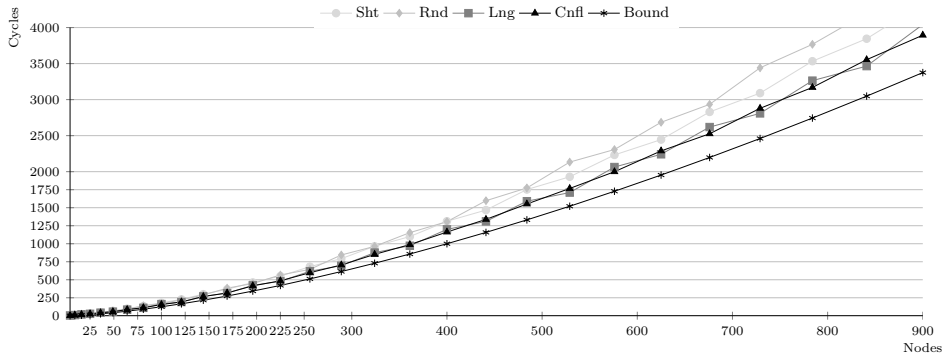


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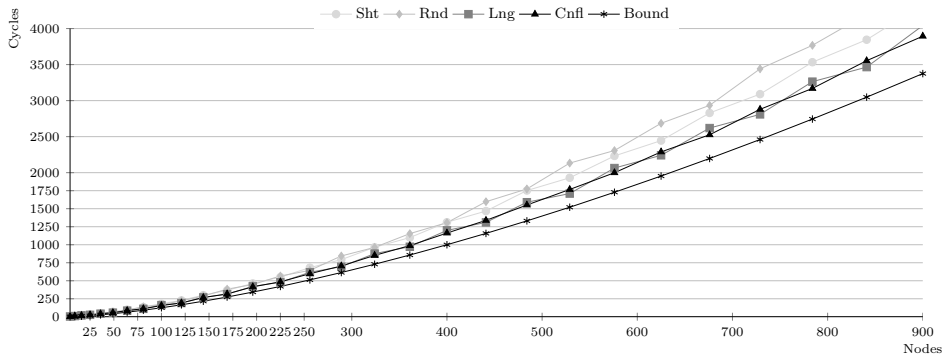
Heuristic is within 15-20% of theoretical lower bound.

# Schedule Lengths – Bidirectional Torus





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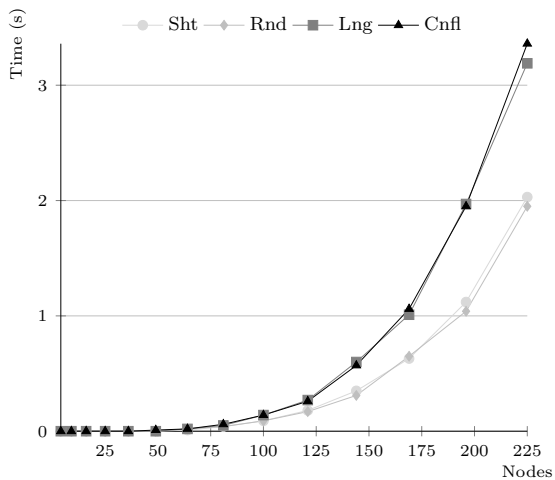
Again within 15-20% of theoretical lower bound.

## Heuristic vs. Optimal Solutions

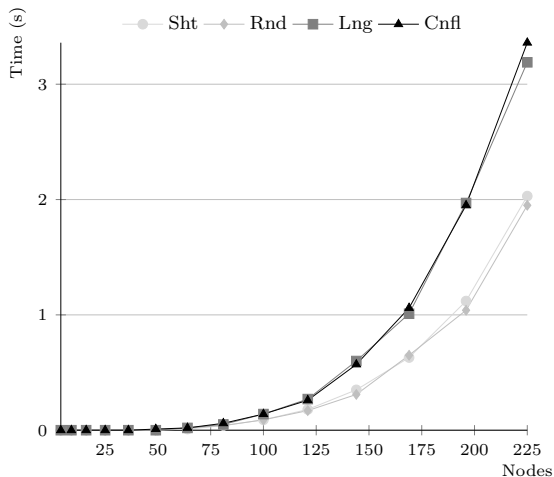
Topology	Nodes	Optimal	Heuristic	Ratio
Torus	4	5	5	1.00
	9	11	11	1.00
	16	26	27	1.04
	25	54*	56	1.04
Bidir. Torus	4	4	5	1.25
	9	10	10	1.00
	16	18	19	1.06
	25	27	28	1.04

\* DNF

# Execution Time – Bidirectional Torus



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Polynomial curve, can clearly be improved by more efficient tracking of conflicts.

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## Heuristic scheduling

- Exploit regularity of NoC topology
- Simple, yet efficient
- 15-20% from lower bounds
- Even closer to optimal solutions