

Plan

Large-Scale GAN Training

Quality Metrics for Generative Models

Generative Texture Models

Neural Network architecture

Generator and discriminator networks can have various layers:

- Fully connected (FC) layers
- Upsampling (interpolation) or Subsampling (max/average pooling) layers
- Convolution/Transposed convolution (with stride)
- Activation functions: RELU, leakyRELU, sigmoid, tanh, etc
- BatchNorm
- ...

Input noise Z has often uniform distribution $\mathcal{U}([0, 1]^p)$ or Gaussian distribution $\mathcal{N}(0, \text{Id})$.

Convolution

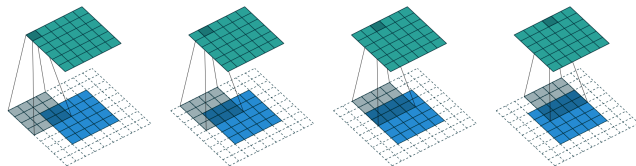
Let $u : \Omega \rightarrow \mathbf{R}^C$ be defined on $\Omega = [0 : M - 1] \times [0 : N - 1]$.

Let $w : \omega \rightarrow \mathbf{R}^{C' \times C}$ be defined on a small $\omega \subset \mathbb{Z}^2$. (Often, $\omega = [-k, k]^2$)

Definition

The convolution $w * u$ of the image u with kernel w is defined by

$$w * u(x) = \sum_{y \in \omega} w(y)u(x - y) = \sum_{z \in -\omega} \tilde{w}(z)u(x + z) \quad \text{where} \quad \tilde{w}(z) = w(-z).$$



NB: There are several possible border conditions (restriction, constant padding, periodic, ...)

Convolution and Transposed convolution

Notice that

- The transpose of a convolution with a $k \times k$ kernel is a convolution with a $k \times k$ kernel
- The transpose of a border crop is zero-padding the borders.
- The transpose of a crude subsampling is zero-inserting.

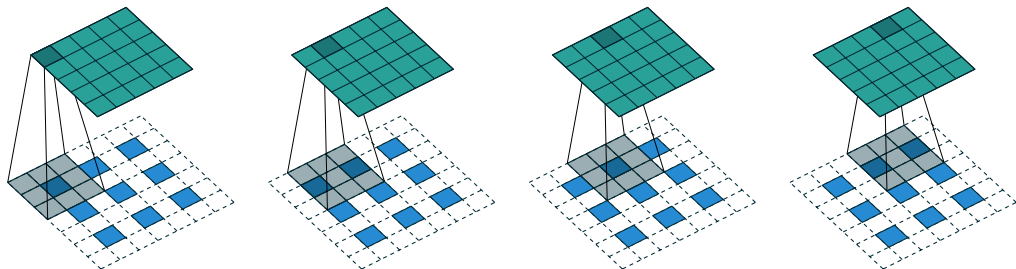
Strided convolutions:

- A “convolution with stride” is a convolution followed by subsampling.
- Called `Conv2d` in PyTorch

Fractionally strided convolutions:

- This is the transpose operator of convolution with stride.
- Called `ConvTranspose2d` in PyTorch

One Example from [Dumoulin and Visin, 2016]



“The transpose of convolving a 3×3 kernel over a 5×5 input padded with a 1×1 border of zeros using 2×2 strides (i.e., $i = 5$, $k = 3$, $s = 2$ and $p = 1$). It is equivalent to convolving a 3×3 kernel over a 3×3 input (with 1 zero inserted between inputs) padded with a 1×1 border of zeros using unit strides (i.e., $i' = 3$, $\tilde{i}' = 5$, $k' = k$, $s' = 1$ and $p' = 1$).”

See also <https://madebyollin.github.io/convnet-calculator/>

BatchNorm layer

Principle of BatchNormalization:

- Consider a batch $(x_n)_{1 \leq n \leq N}$ of N responses to a neural layer with C features.
- For each n , $x_{n,i} \in \mathbf{R}^{W \times H}$ is the i -th feature map of the n -th image.
- Batch normalization consists in computing for any n, i

$$y_{n,i} = \gamma_i z_{n,i} + \beta_i \quad \text{with} \quad z_{n,i} = \frac{x_{n,i} - m_i}{\sqrt{\sigma_i^2 + \epsilon}}$$

where m_i, σ_i are the mean and std of the gathered feature maps $(x_{n,i})_{1 \leq n \leq N}$.
(In other words, m_i, σ_i contains averages over N and spatial dimensions H, W .)

- γ_i, β_i are trainable parameters.
- Implemented in `BatchNorm2d` in PyTorch.

At inference: normalization is done with $m_i, \sigma_i, \gamma_i, \beta_i$ learned during training.

Switch to inference mode with `model.eval()`.

Different Kinds of Normalization

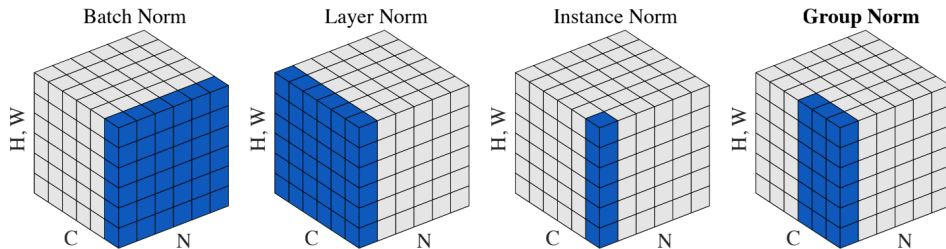


Diagram from [Wu and He, 2018]

- H, W : spatial dimensions
- C : channel dimension
- N : batch dimension

(See the formula for InstanceNorm in [Ulyanov et al., 2017])

Convolutional GAN

[Radford et al., 2016]

Important principles of the construction:

- “All convolutional”: remove max pooling layers, and learn downsampling instead
- Eliminate Fully-Connected Layers
- Batch Normalization to stabilize learning (except on generator output, and discriminator input)
- ReLU activations for the generator
- LeakyReLU activations for the discriminator

Generator: upsampling network with **fractionally strided convolutions**

Discriminator: convolutional network with **strided convolutions**

DCGAN Architecture

[Radford et al., 2016]

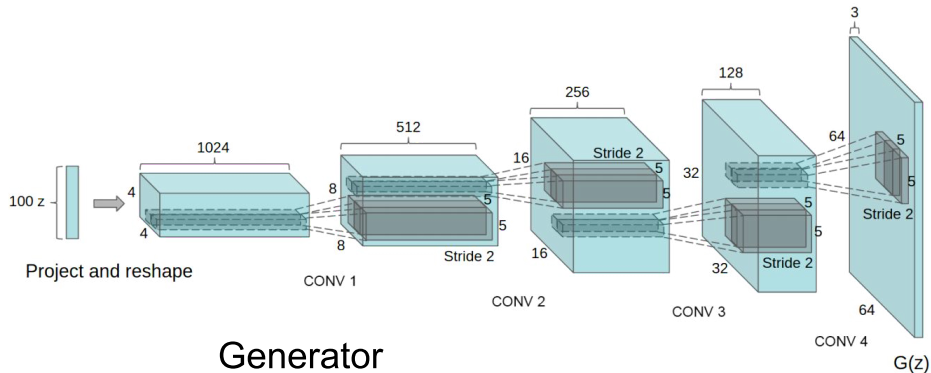
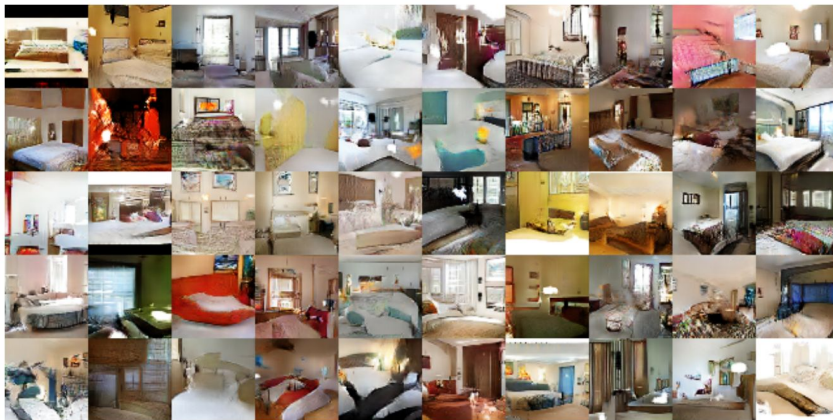


Image Generation with DCGAN [Radford et al., 2016]



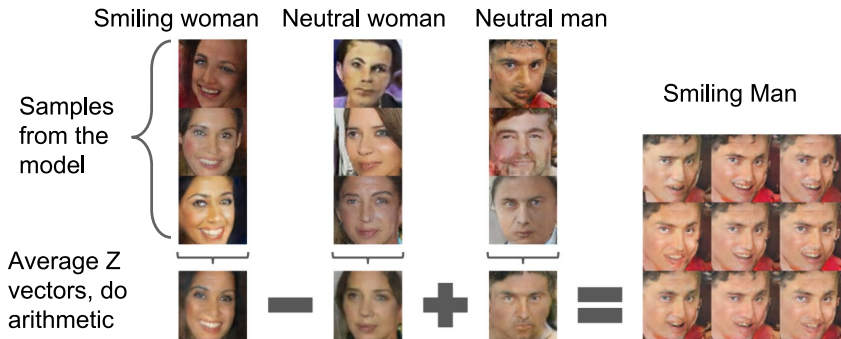
Generations of realistic bedrooms pictures, from randomly generated latent variables.

Image Interpolation with DCGAN [Radford et al., 2016]



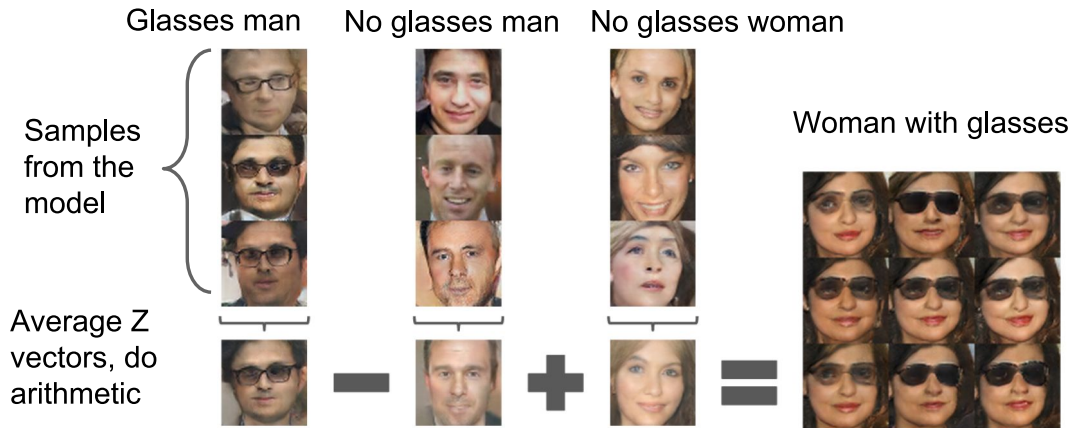
Interpolation in between points in latent space.

Arithmetic with DCGAN [Radford et al., 2016]



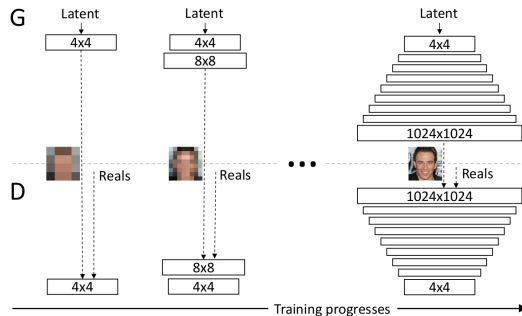
- Average latent vector of several samples
- After arithmetic, add a small random perturbation to get similar samples

Arithmetic with DCGAN [Radford et al., 2016]



Progressive Growing of GANs [Karras et al., 2018]

- Progressive Multiresolution Training
- Mirror architectures for G and D
- Simple upsampling/downsampling
nearest neighbor upsampling;
average pooling downsampling
- Minibatch statistics layer at the end of D
- Pixelwise feature normalization
- Training with WGAN-GP



StyleGAN [Karras et al., 2019]

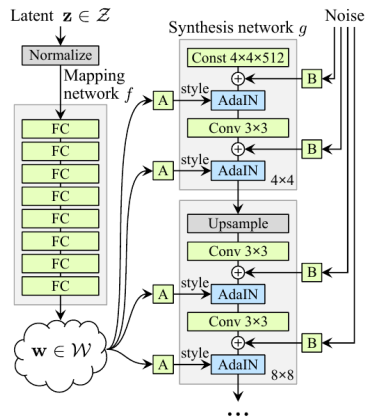
- “Separation of high-level features (pose, identity) from stochastic variation (freckles, hair)”
- Embed latent code z into an intermediate latent space w with a multilayer perceptron (8 FC layers)
- Spatially invariant style vector $y = (y_s, y_b)$ for each feature map, obtained from w
- AdaIN: Adaptive Instance Normalization

$$\text{AdaIN}(x_i, y) = y_{s,i} \frac{x_i - \mu(x_i)}{\sigma(x_i)} + y_{b,i}$$

where the feature map x_i is normalized separately.
(No learned parameters γ, β here.)

$$\text{AdaIN}(x_{n,i}, y) = y_{s,i} \frac{x_{n,i} - \mu(x_{n,i})}{\sigma(x_{n,i})} + y_{b,i}$$

- Style mixing (playing with two latent codes w_1, w_2)



(b) Style-based generator

StyleGAN [Karras et al., 2019]

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- Style mixing (playing with two latent codes w_1, w_2)



StyleGAN [Karras et al., 2019]

StyleGAN allows for style mixing at different scales (by using the corresponding subparts of w).



StyleGAN2 [Karras et al., 2020]

- AdaIN causes droplet artifacts in StyleGAN
→ Weight modulation/demodulation instead of AdaIN
- Path length regularization: fixed-norm steps in w
results in fixed-norm changes in image space
- Residual connections with downsampling in D
- Skip connections in G
- No progressive growing
(which leads to *phase artifacts*)



Face Generation with StyleGAN2 [Karras et al., 2020]



<https://thispersondoesnotexist.com/>

Face Generation with StyleGAN2 [Karras et al., 2020]



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StyleGAN vs StyleGAN2



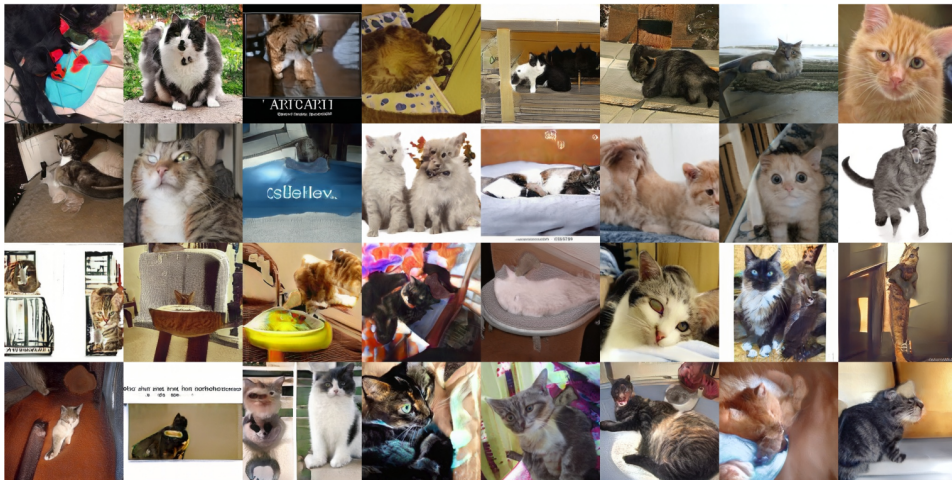
First row: real images
Second row: samples of StyleGAN after projection on the latent code

StyleGAN vs StyleGAN2



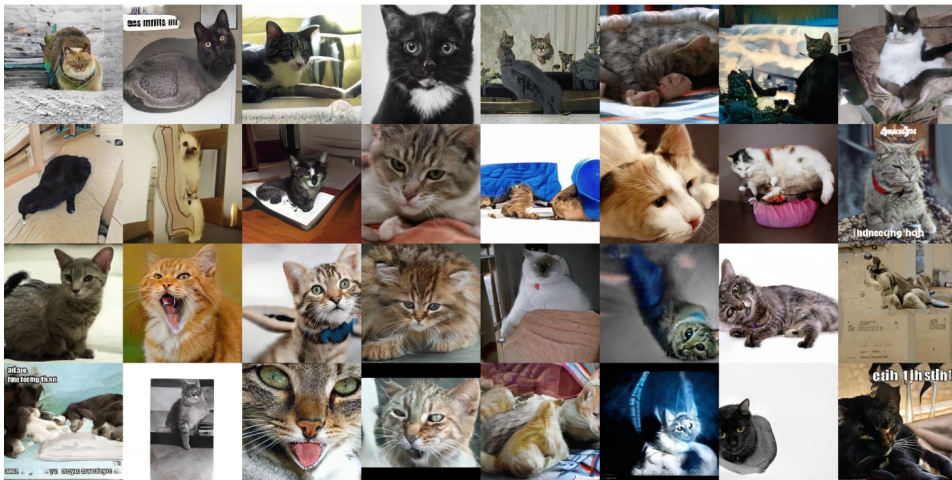
First row: real images
Second row: samples of StyleGAN2 after projection on the latent code

The Cat Challenge...



Samples of StyleGAN2-Model1 trained on LSUN Cat

The Cat Challenge...

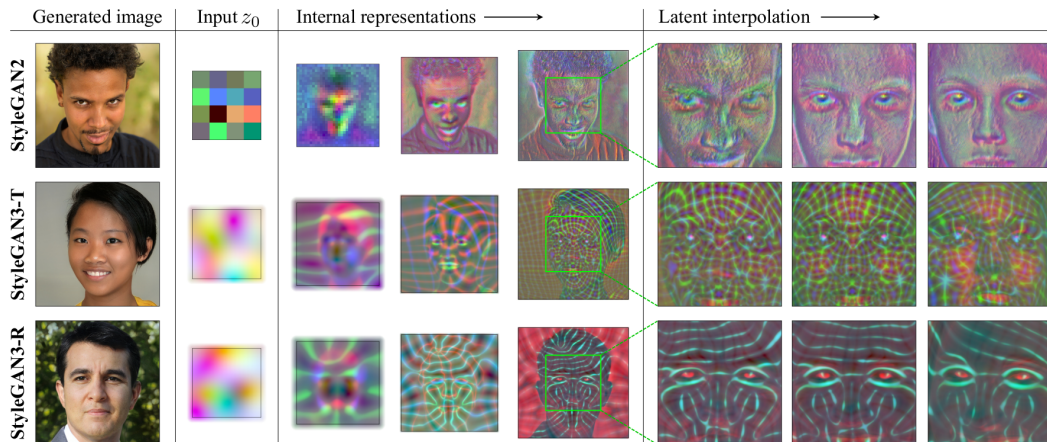


Samples of StyleGAN2-Model2 trained on LSUN Cat

StyleGAN3 aka Alias-free GANs

- Aliasing artifacts present in some GANs results due to:
 - non-ideal upsampling
 - pointwise activations
- Enforce continuous equivariance to sub-pixel translation (Shannon is back...)
- Also, ensure that no aliasing appears through the network:
 - use band-limited filters
 - use low-pass filters when needed

StyleGAN3 aka Alias-free GANs



Conditional GANs

Conditional GANs: Train the generator and the discriminator by passing a class information:

- **Generator:** Generate a fake “3”.
- **Discriminator:** Is it a real or a fake “3”?

Class conditional training:

$$\min_{\theta_G} \max_{\theta_D} \sum_{(x, \mathbf{c}) \in \mathcal{D}_{\text{real}}} \log D_{\theta_D}(x, \mathbf{c}) + \sum_{(z, \mathbf{c}) \in \mathcal{D}_{\text{rand}}} \log(1 - D_{\theta_D}(\underbrace{G_{\theta_G}(z, \mathbf{c})}_{\text{fake}}, \mathbf{c}))$$

where

- $\mathcal{D}_{\text{real}}$ is a collection of real labeled data.
- $\mathcal{D}_{\text{rand}}$ is a collection of synthetic latent code and labels.

This requires to choose a distribution on \mathbf{c} to generate the synthetic image $G_{\theta_G}(z, \mathbf{c})$.

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- **Question:** How to measure that the generator covers well the training data?
- **Main idea:** Comparing image distributions is hard...
but comparing measurements from it is easier.
- Classification neural networks provide a set of deep non-linear features.
For example, VGG19 [Simonyan and Zisserman, 2015], or Inception Networks [Szegedy et al., 2016].
- **Measure quality of the generative model by looking at how deep statistics are preserved**
Somehow, this ensures that the database is well-covered.
- **Keep in mind that**
 - The network used to get the features must be relevant w.r.t. the generative task at play.
 - Quantitative results highly depend on the network and implementation details.

Inception Score \uparrow [Salimans et al., 2016]

- The inception score measures if μ generates a diverse collection of meaningful pictures
- For an image x , Inception-v3 gives a label distribution $p(y|x)$ (discrete on $N = 1000$ labels)
- Images containing meaningful objects have $p(y|x)$ with low entropy
- In order to generate various images, $p(y) = \int p(y|x)\mu(dx)$ should have high entropy

The Inception Score then writes as

$$\text{IS}(\mu) = \exp \left(\int \text{KL} \left(p(y|x) | p(y) \right) \mu(dx) \right) \in [1, N]$$

It is 1 iff for a.e. x , $p(\cdot|x) = p(\cdot)$ (label distribution does not depend on x)

It is N iff for a.e. x , $p(\cdot|x)$ is concentrated on one label, and $\forall y, \int p(y|x)\mu(dx) = \frac{1}{N}$

How to compute it in practice:

- Compute an estimate $\hat{p}(y)$ of $p(y) = \int p(y|x)\mu(dx)$ by drawing samples of μ
- Estimate $\int \text{KL}(p(y|x) | \hat{p}(y))\mu(dx)$ by drawing samples of μ

Fréchet Inception Distance (FID) ↓ [Heusel et al., 2017]

The FID measures how close are two image distributions μ, ν in terms of features distributions. It is based on the response of Inception-v3 [Szegedy et al., 2016] before last pooling layer:

$$f : \mathbf{R}^d \rightarrow \mathbf{R}^m$$

that extracts $m = 2048$ features (as a generic image summary)

NB: Images may have to be resized/normalized to fit into this network.

Algorithm to compute the FID score:

1. Draw samples (x_i) and (y_j) of $X \sim \mu$ and $Y \sim \nu$ and compute the features $(f(x_i)), (f(y_j))$
2. Fit Gaussian distributions $\mathcal{N}(m_X, \Sigma_X)$ and $\mathcal{N}(m_Y, \Sigma_Y)$ to $(f(x_i)), (f(y_j))$ (in \mathbf{R}^{2048})
3. Return the 2-Wasserstein distance between the Gaussian distributions, i.e. the Fréchet distance: [Dowson and Landau, 1982]

$$W_2^2\left(\mathcal{N}(m_X, \Sigma_X), \mathcal{N}(m_Y, \Sigma_Y)\right) = \|m_X - m_Y\|_2^2 + \text{Tr}\left(\Sigma_X + \Sigma_Y - 2(\Sigma_X \Sigma_Y)^{\frac{1}{2}}\right)$$

NB: FID can be adapted to the “single-image” case: **SiFID** [Shaham et al., 2019]

SiFID compares distributions of features obtained after a convolution layer (spatially averaged)

Comments on Generative Quality

- Inception Score does not depend on the target distribution ν .
- Need to distinguish “precision/recall” for evaluating quality [Lucic et al., 2018].
“Precision” is the probability that a fake image falls within the distribution of real images.
“Recall” is the probability that a real image falls within the distribution of fake sample.
IS mainly captures precision. FID captures both precision and recall.
- The IS and FID are not enough to measure the fact that samples are photo-realistic.
[Barratt and Sharma, 2018]
- Other measures have been proposed better correlated with Human prediction of quality.
[Kolchinski et al., 2019]

Are GANs created equal?

[Lucic et al., 2018]

Many variants of GAN training exist, with various architectures and more or less stable training.

- Regarding quality of generated images, may GAN variants perform similarly.
[Lucic et al., 2018] proposed a large comparison framework, with a budget for hyperparameter tuning, and by averaging over several random seeds.
- “WGANs work because they fail” [Stanczuk et al., 2021], [Mallasto et al., 2019]
The dual training in WGAN-GP does not approximate the Wasserstein distance correctly.
But estimating it more precisely (e.g. semi-discrete WGAN) often leads to blurrier samples.
→ The quality of a generative network relies on good features learned by the discriminator.

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Exemplar-based Texture Synthesis

- Exemplar texture :

$$u_0 : \Omega \rightarrow \mathbf{R}^d$$

defined on a discrete rectangle $\Omega \subset \mathbb{Z}^2$.

- Texture model: stationary random field

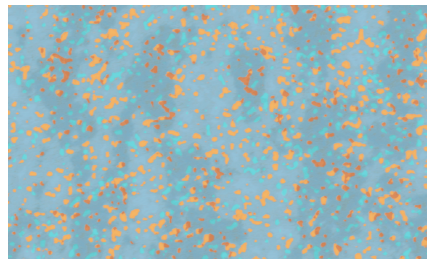
$$V : \mathbb{Z}^2 \rightarrow \mathbf{R}^d$$

The problem can be split into

- Estimate a model V
- Draw one (or several) samples of V



Exemplar u_0



Synthesis v

The Textto Model

Compute exemplar $u^s : \Omega \cap (2^s \mathbb{Z}^2) \rightarrow \mathbf{R}^d$ at different scales $s = 0, \dots, S - 1$
and corresponding patch distributions ν^s

Initialize synthesis with Gaussian field U_{S-1} at the coarse scale

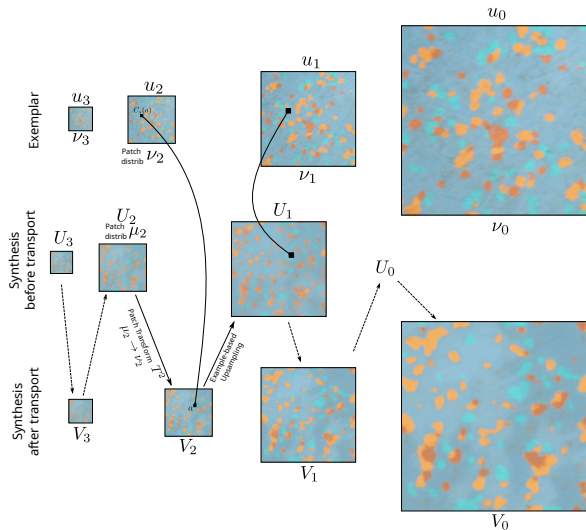
For $s = S - 1, \dots, 0$,

- Estimate the patch distribution μ_s of U_s
- Learn a patch semi-discrete OT map T_s such that $T_s \# \mu_s \approx \nu_s$
(Recall that T_s is a biased nearest neighbor assignment!)
- Apply T_s to all patches of U_s and recompose by averaging to an image V_s
- If $s > 0$, upsample V_s to initialize the next scale U_{s-1}
(For that, use patches at the same positions, but twice larger.)

Output: synthesis at fine scale V_0

Remark: Once the model learnt, one can discard the learning steps ■ to do synthesis on-the-fly

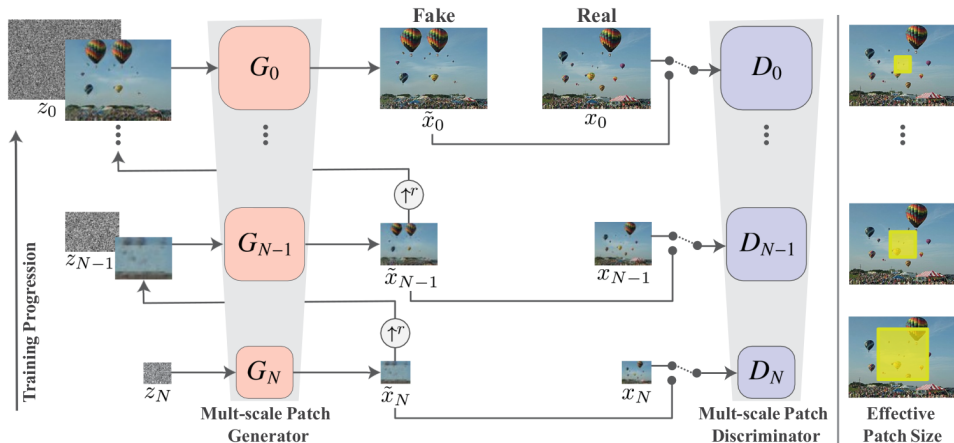
Texto in one diagram



SinGAN: Learning from a Single Image [Shaham et al., 2019]

- Capture the multi-scale patch distributions of an image (possibly non-texture)
- Coarse-to-fine generator
- Patch-based discriminator learned with WGAN-GP loss, at each scale
- Loss defined over all patches of the image, and not randomly selected patches
→ allows the network to learn boundary conditions

SinGAN: Learning from a Single Image [Shaham et al., 2019]



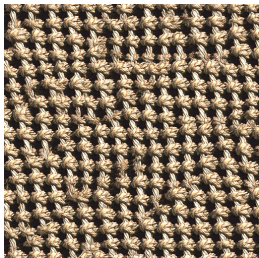
Random samples from a *single* image



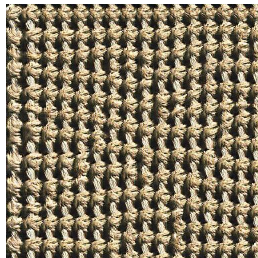
Samples of Texture Networks



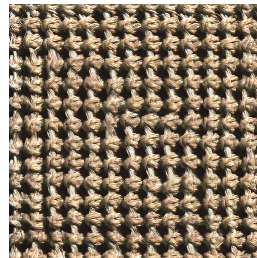
Original



GOTEX
[Houdard et al., 2023]

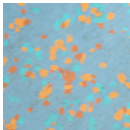


PSGAN
[Bergmann et al., 2017]

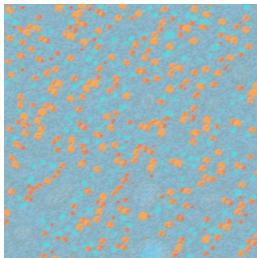


SinGAN
[Shaham et al., 2019]

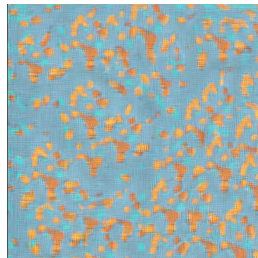
Samples of Texture Networks



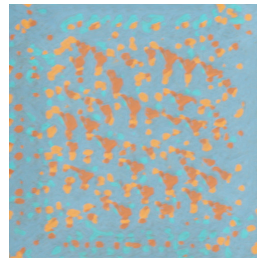
Original



GOTEX
[Houdard et al., 2023]



PSGAN
[Bergmann et al., 2017]

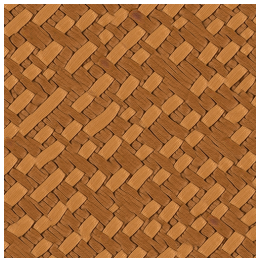


SinGAN
[Shaham et al., 2019]

Samples of Texture Networks



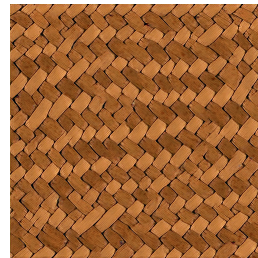
Original



GOTEX
[Houdard et al., 2023]



PSGAN
[Bergmann et al., 2017]








SinGAN
[Shaham et al., 2019]

Take-home Messages





- We discussed several architectures for image generation.
- Large-scale synthesis benefits from architectures adapted for multi-resolution synthesis.
- Recent generative models crucially rely on
 - several tricks for training or designing the architecture
 - very long training of models...
 - with a very large number of parameters
 - and a very large dataset.
- FID score gives a reasonable/simple way to measure the quality of a generative model... but it does not suffice to judge photo-realism of the samples.

THANK YOU FOR YOUR ATTENTION!





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