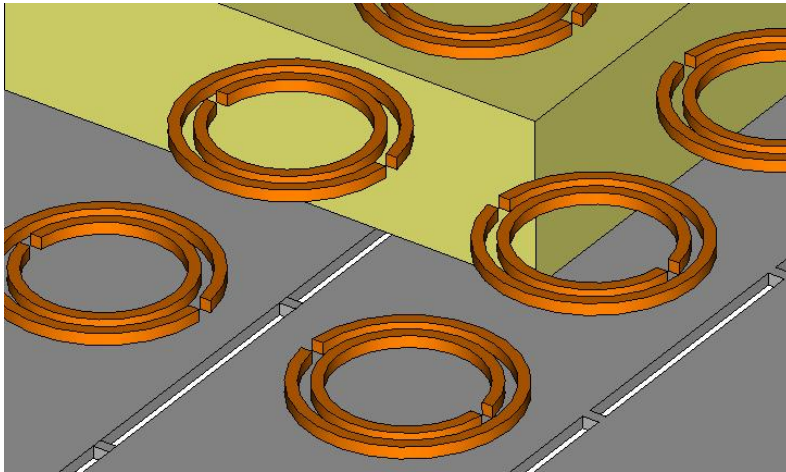


# CST STUDIO SUITE™ 2006B

## Application Note

# Periodic Arrays : FSS / PBG / ...



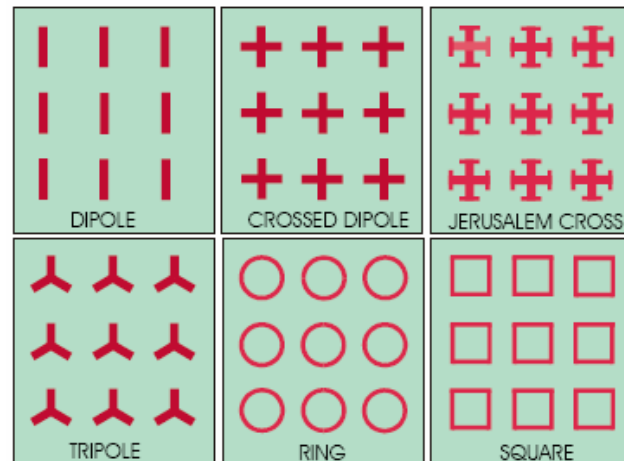
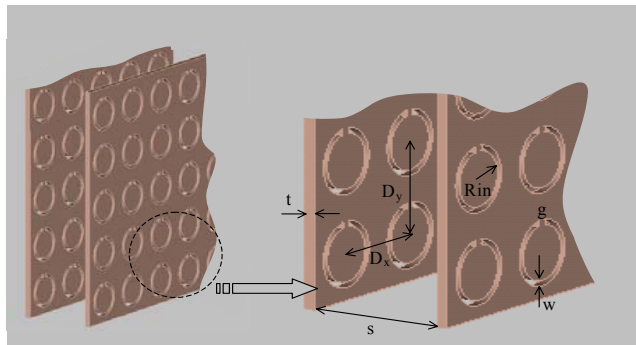
Frequency Selective Surfaces  
Unit Cell  
Complimentary Arrays  
Tips + Tricks  
Metamaterials  
Dispersion Diagrams

# Periodic Arrays

## *Frequency Selective Surfaces (FSS)?*

Periodic assemblies of identical elements arranged in a one- or two-dimensional array.

These periodic structures are either an array of apertures in a thin metallic sheet or metallic patches on a dielectric substrate



# Applications



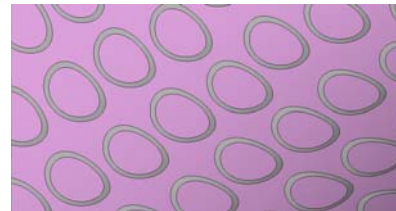
(Photo by Kockums AB).

Ghost ships

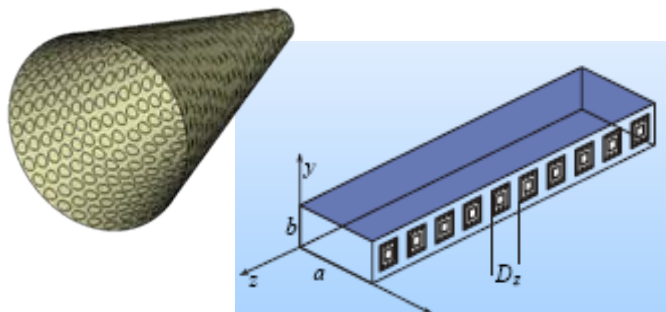
Rapidly retractable antennas, some of which are concealed behind frequency selective surfaces (FSS)



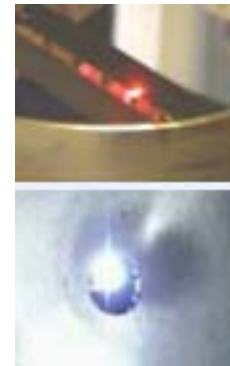
FSS Radomes



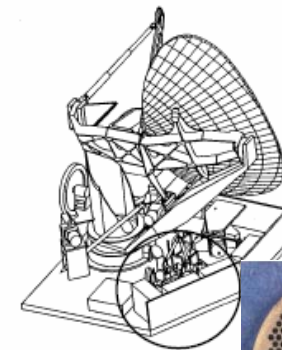
Stealthy wallpaper to block Wi-Fi signals



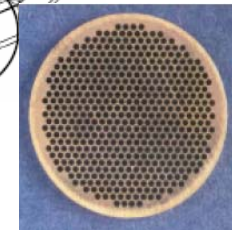
FSS horns and waveguides and reflector antennas



Optically tunable FSS arrays on Si



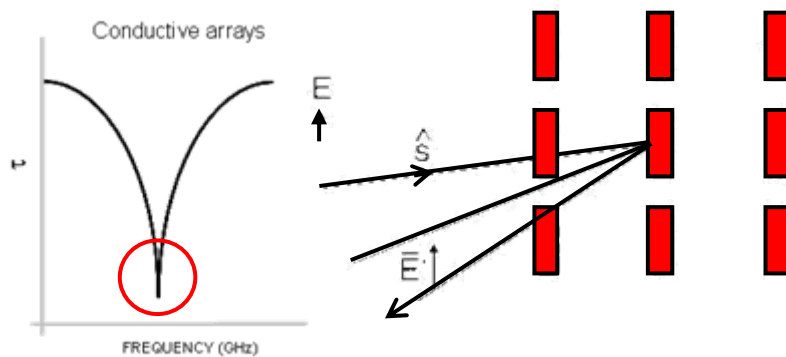
Multi-channel radiometer filters



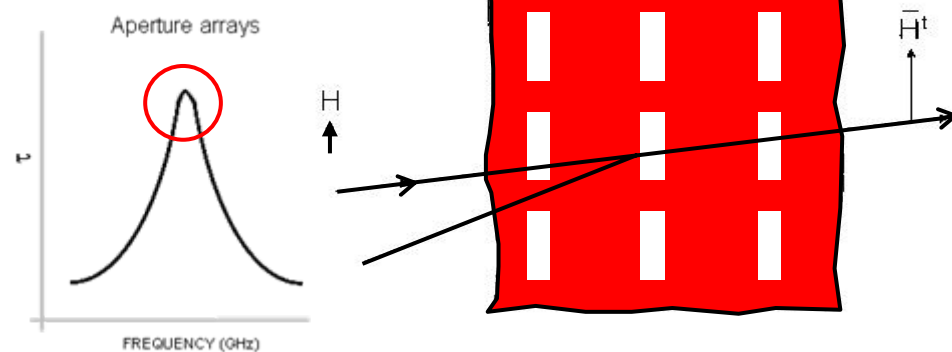
# Conducting and Aperture Arrays

## Complimentary Arrays

Combination of conducting and aperture arrays of similar shape when put one on top of each other forms a “complete” perfectly conducting plane



Band Stop



Band Pass

# Typical FSS Elements



Single polar elements

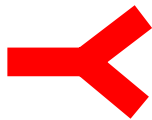
Resonant wavelength  $\lambda_r$  for a conducting element without substrate

Dipoles =  $l/2$

Rings =  $2\pi(R_{in} + 0.5w)$

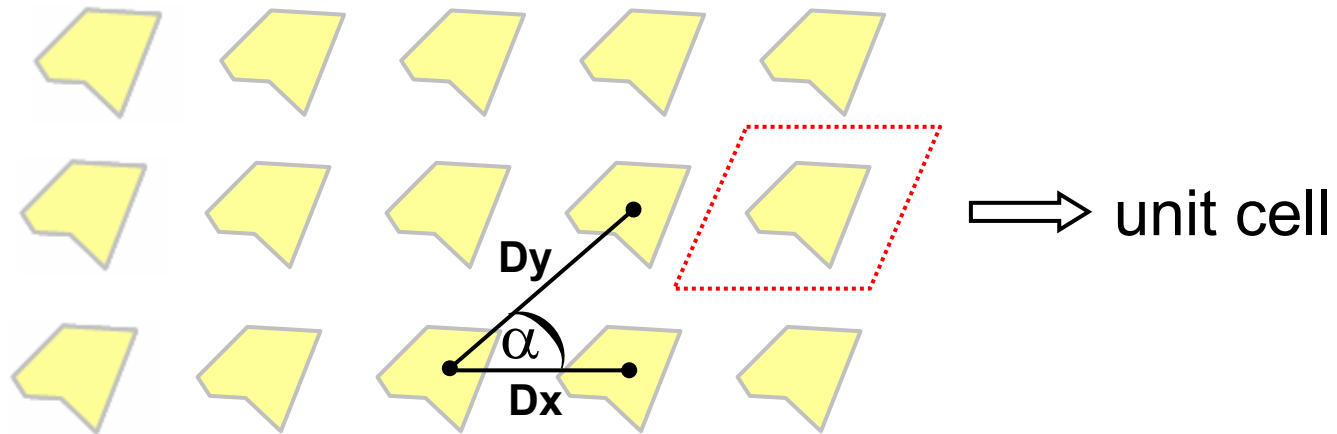
With a substrate the resonant wavelength

$$\lambda_\varepsilon = \frac{\lambda_r}{\sqrt{\varepsilon_r}}$$



Dual polar elements

# The Unit Cell



The unit cell can be defined as the basic building block (can be an arbitrary resonant shape) of the array that repeats itself infinitely defined by the periodicity  $Dx$ ,  $Dy$  and the angle in-between  $\alpha$

# Passive and Active Arrays

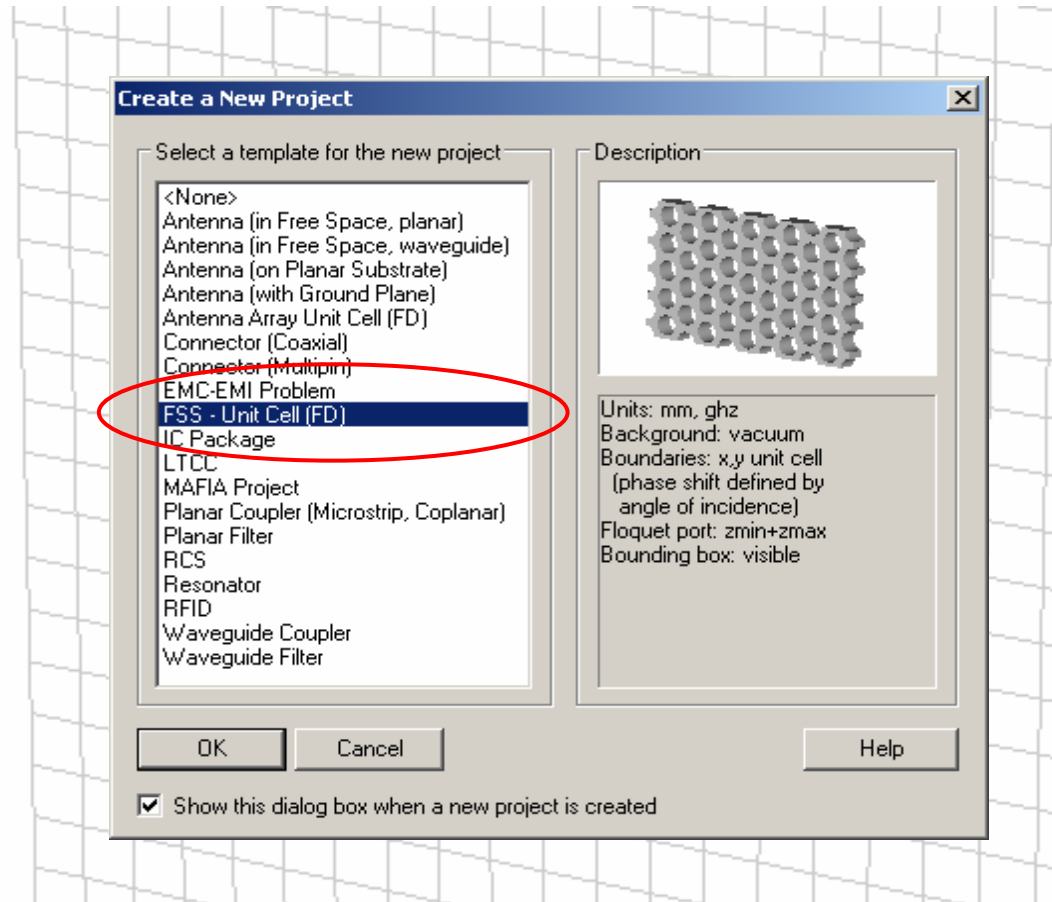
## Methods of Excitation

Fundamentally any periodic array can be excited in two ways:

- Incident Plane wave  $\vec{E}_i$  (*passive array*)
- Individual Generators connected to each elements (*active array*)

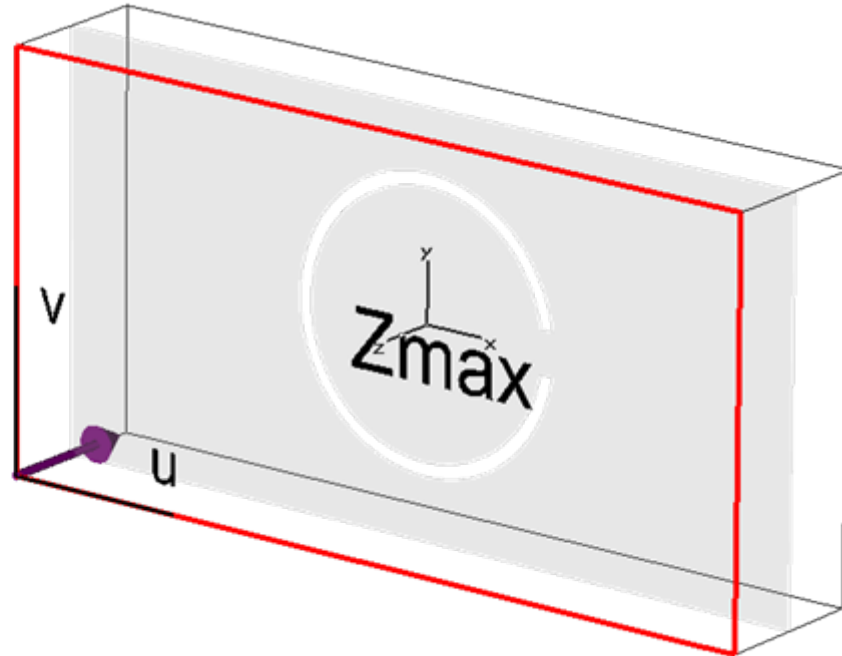
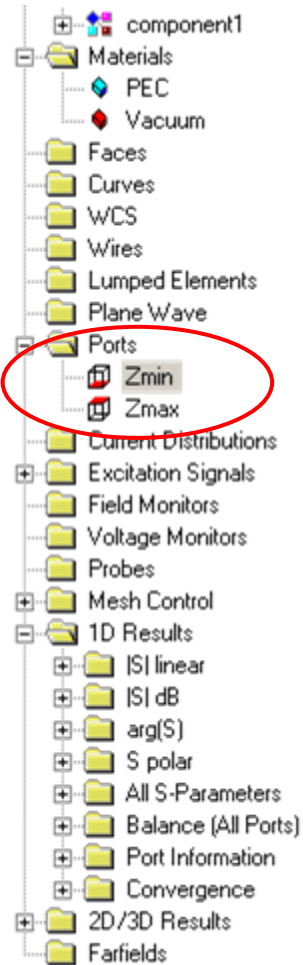
For an active array the voltage generators must have the same amplitude and a linear phase variation across the active array in order to qualify as a periodic array

# CST MWS Example (F Solver)

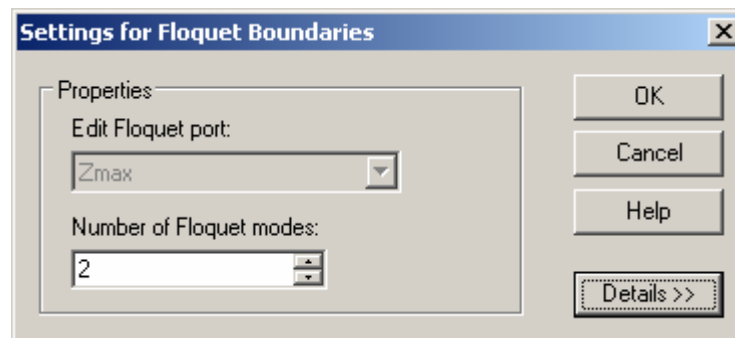




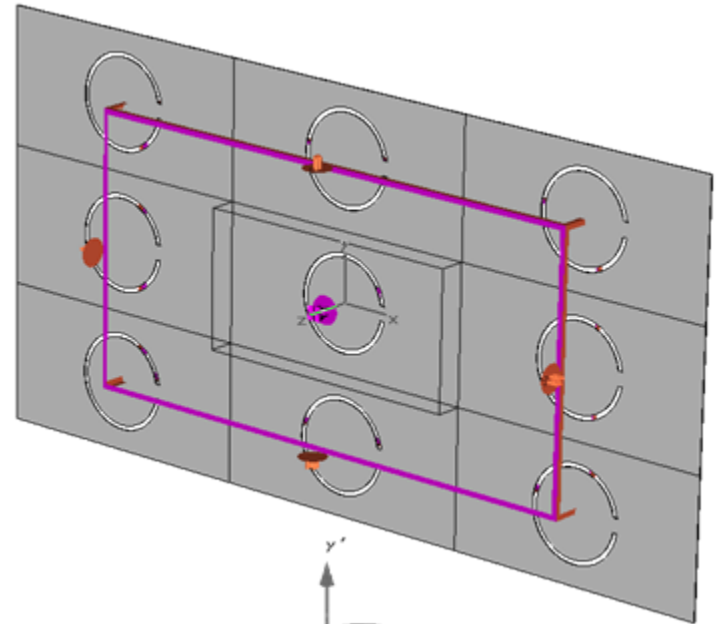
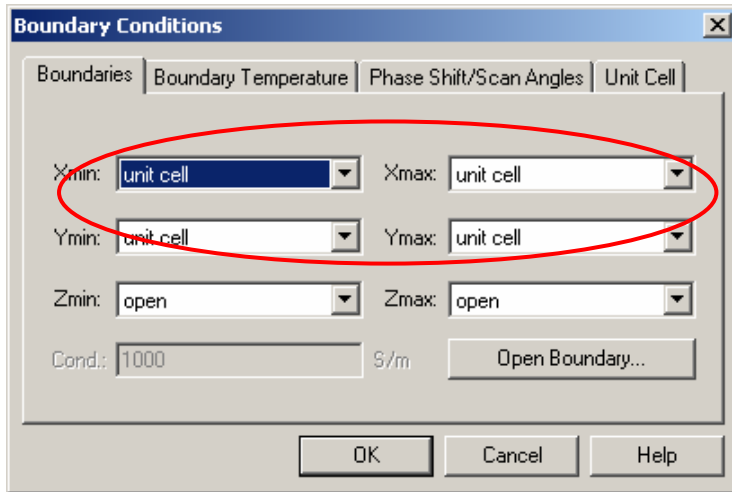
# Floquet Ports



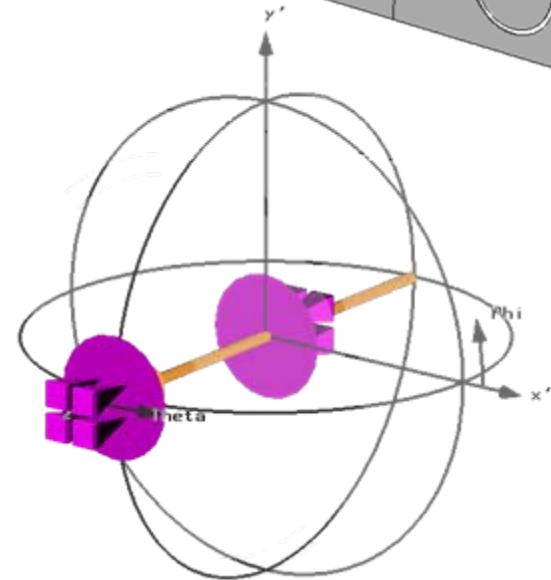
Number of modes = 2



# Unit Cell Boundaries

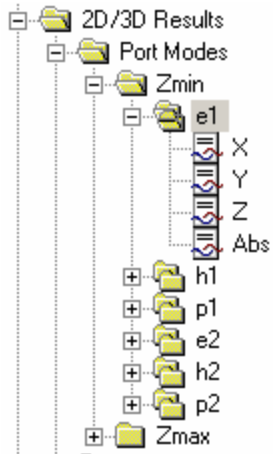


Name	Value	Description	Type
phi	0	spherical angle of incident plane wave	None
theta	45	spherical angle of incident plane wave	None
			Undefined



**Unit cell boundaries allow plane waves at arbitrary angles**

# Plane Wave Incidence at arbitrary Angles



Type = E-Field (peak)

Mode type = Plane wave

Accuracy = 1.52537e-007

Normal Beta = 14.8201 1/m

Wave Imp. = 376.732 Ohms

Plane at z = -3

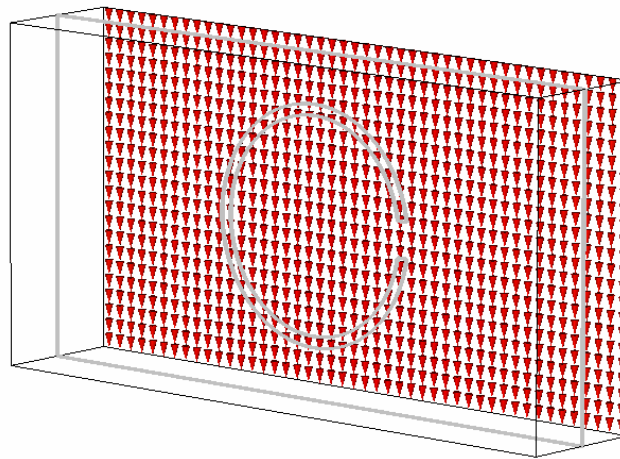
Frequency = 1

Phi = 0 degrees

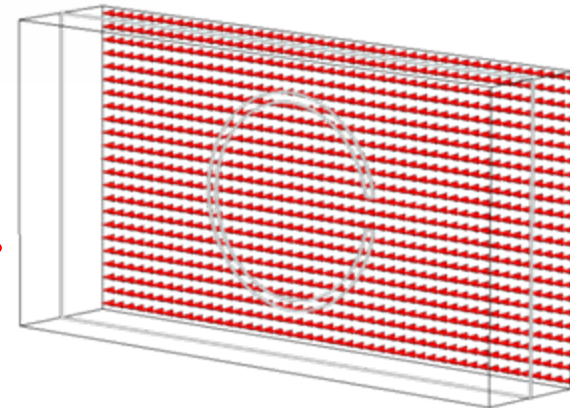
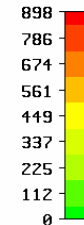
Theta = 45 degrees

Phase = 0 degrees

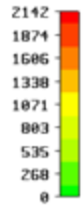
Maximum-Zd = 898.22 V/m at 1.91748 / -7.68 / -3



V/m



VA/m<sup>2</sup>



Type = Power flow (peak)

Mode type = Plane wave

Accuracy = 1.52537e-007

Normal Beta = 14.8201 1/m

Wave Imp. = 376.732 Ohms

Plane at z = -3

Frequency = 1

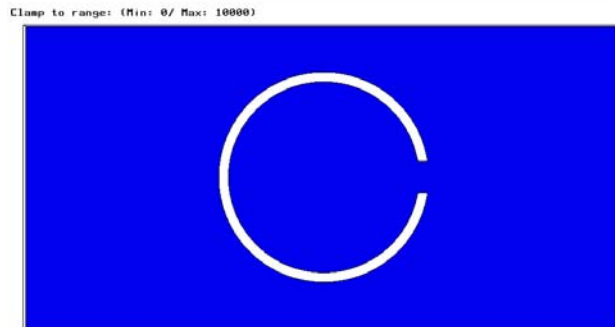
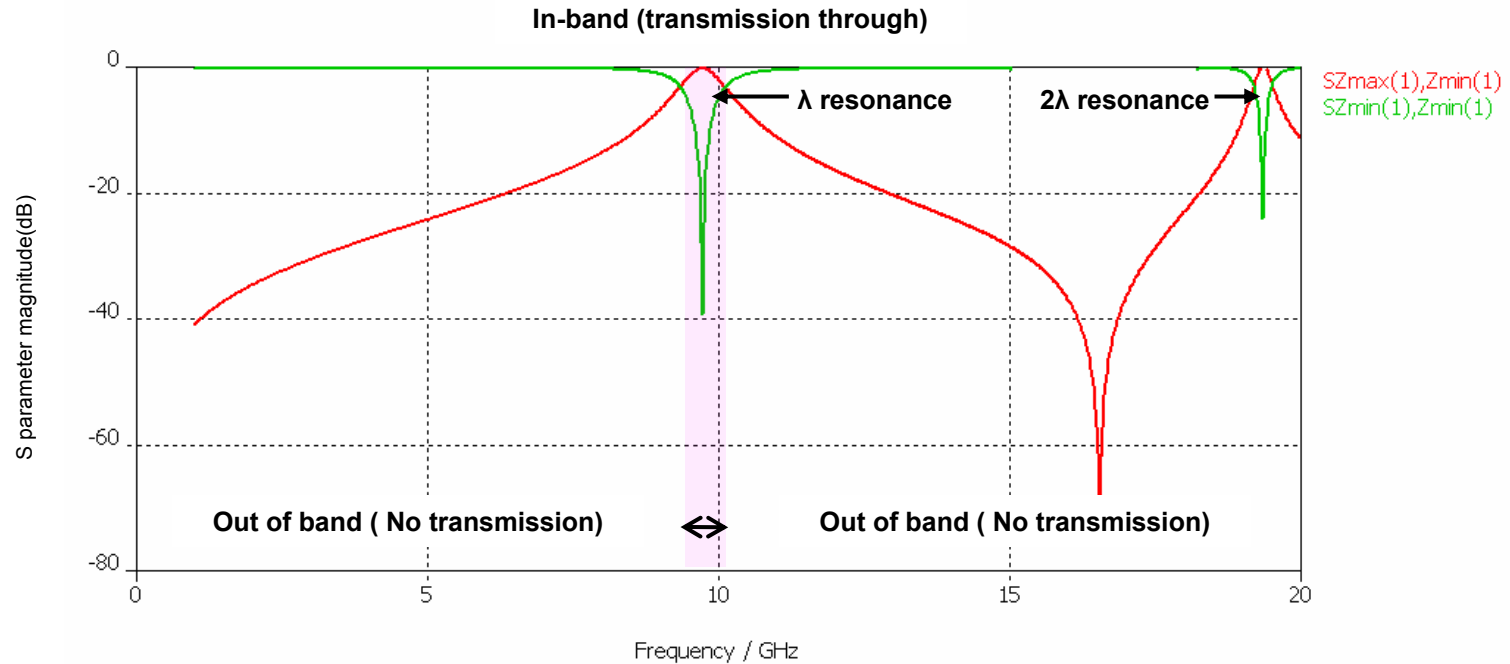
Phi = 0 degrees

Theta = 45 degrees

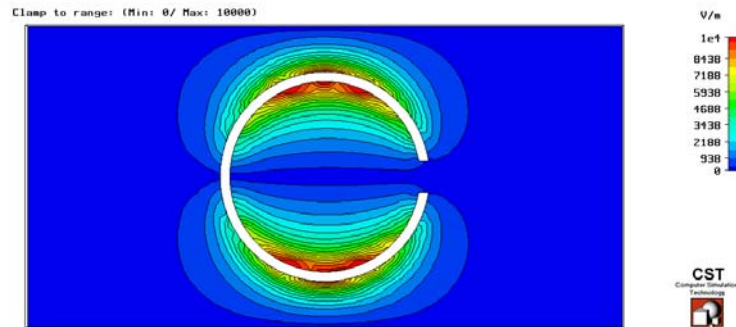
Maximum-Zd = 2141.57 VA/m<sup>2</sup> at -4.374 / -7.68 / -3



# Transmission Coefficient



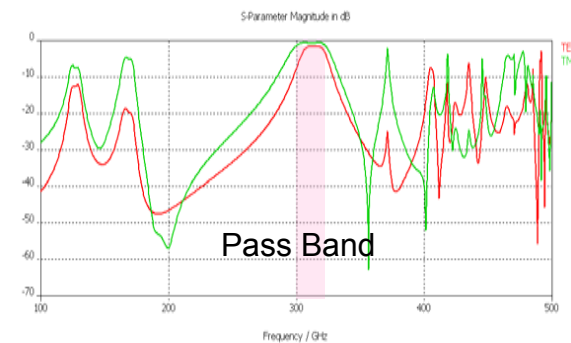
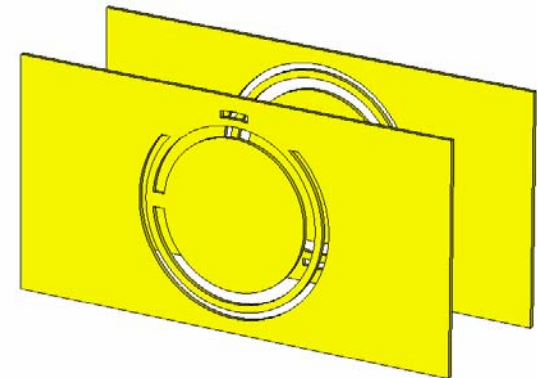
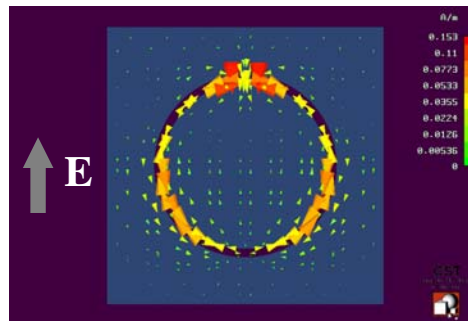
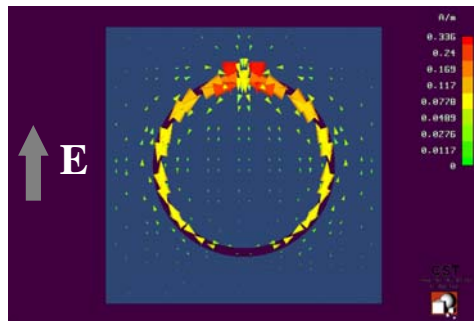
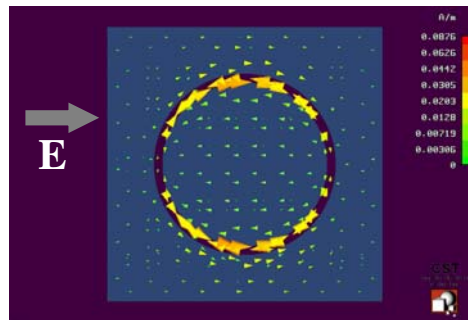
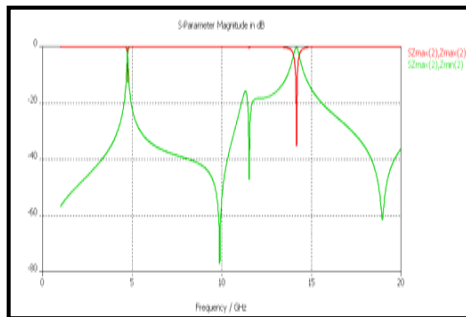
E field animation at 1GHz



E field animation at 10GHz



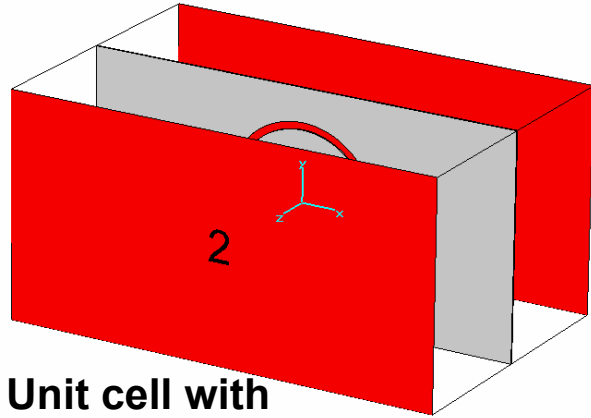
# Coupling Modes & Cascaded Arrays



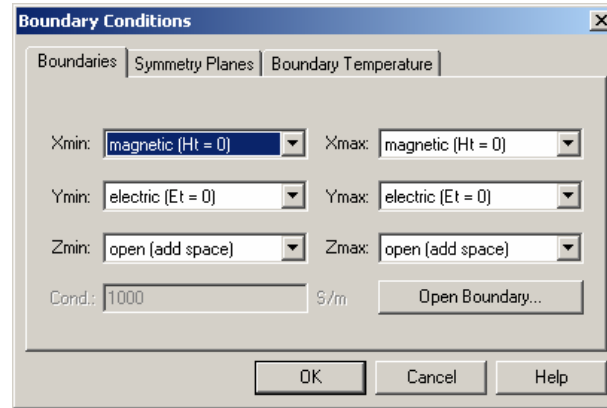
Coupling TE and TM modes by nesting rings allow for dual polar dual frequency filters to be designed

Cascaded arrays give higher BW and the separation allows to control the roll-off rate

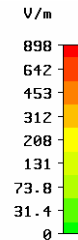
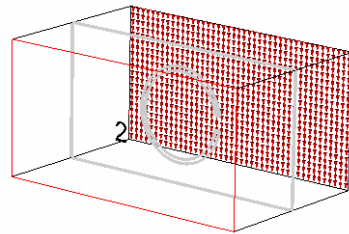
# Unit Cell (T Solver)



Unit cell with waveguide ports

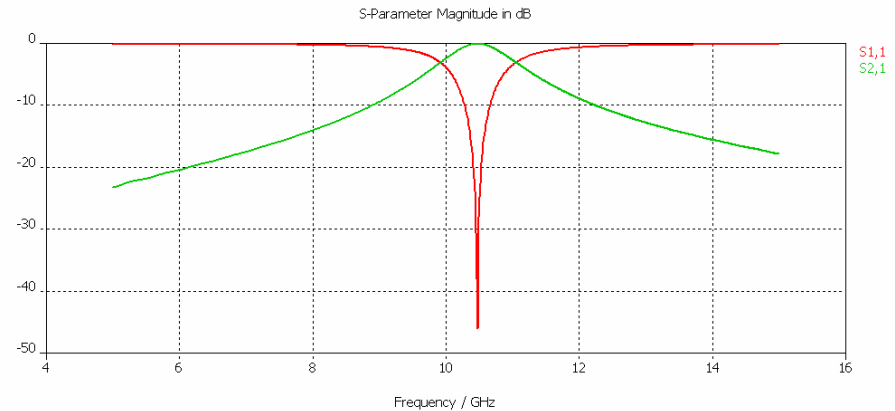


Only valid for normal incidence (theta and phi = 0)



Type = E-Field (peak)  
 Mode type = TEM  
 Accuracy = 5.64781e-013  
 Beta = 209.585 1/m  
 Wave Imp. = 376.73 Ohms  
 Line Imp. = 188.318 ohms

Plane at z = -10  
 Frequency = 10  
 Phase = 180 degrees  
 Maximum-2d = 898.22 V/m at -8.33258 / -0.8 / -10



# Metamaterials

**AMC**

(Artificial Magnetic  
Conductor)

**DNG**

(Double Negative)

**EBG**

Electromagnetic Bandgap

**LHM**

(Left Handed Materials)

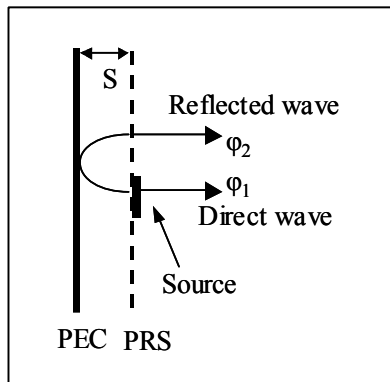
**PBG**

(Photonic Bandgap)



# AMC

- PEC: reflect incident waves with 180° phase shift
- PMC : Would reflect waves with 0° (dual)



- Direct wave  $\varphi_1$

- Reflected wave  $\varphi_2 = 2\varphi_T - \frac{2\pi 2S}{\lambda} - \pi + \varphi_1$

Transmission phase of the FSS  $\varphi_T$

Phase delay along  $S$   $\frac{2\pi 2S}{\lambda}$

Reflection phase at PEC  $-\pi$

Direct wave phase  $\varphi_1$

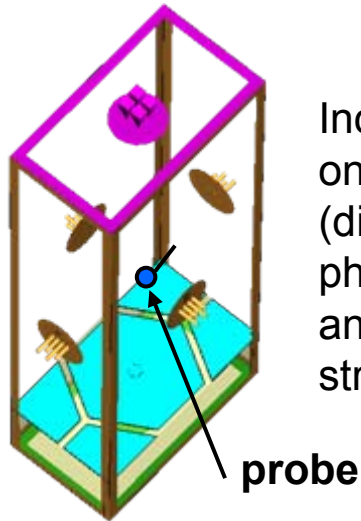
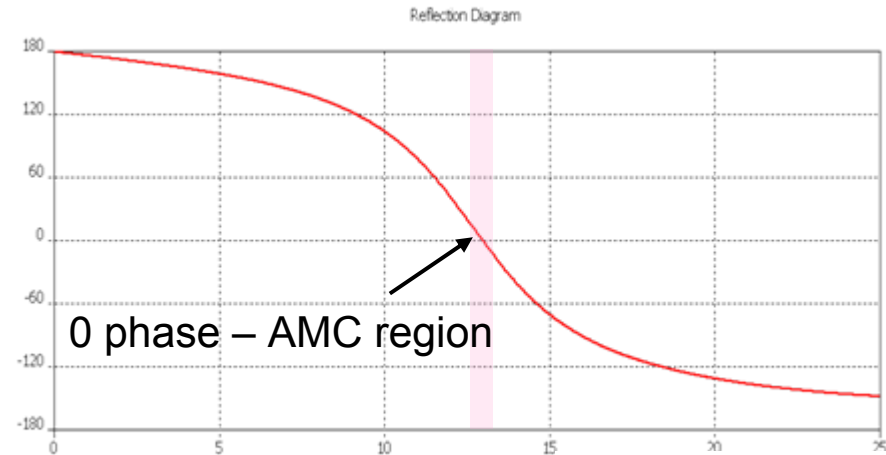
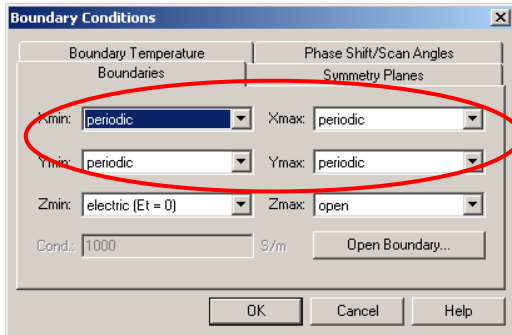
Resonance Condition:

$$\varphi_2 - \varphi_1 = 2\varphi_T - \frac{2\pi 2S}{\lambda} - \pi = 2N\pi$$

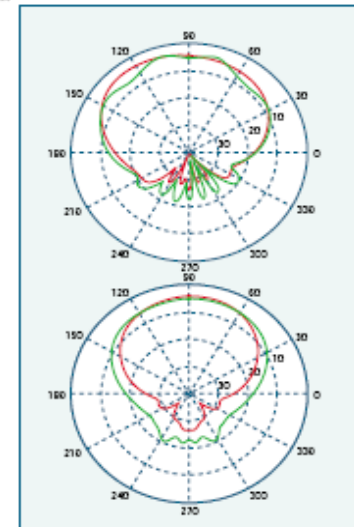
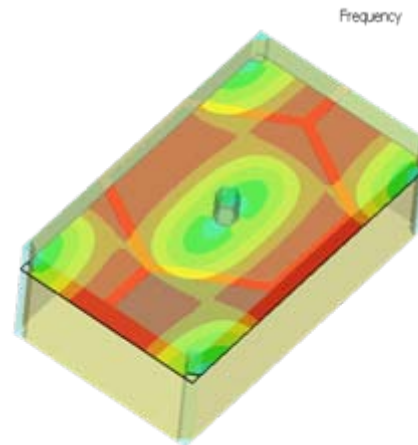
An AMC can be generated by having a ground plane at close proximity to the FSS. The combination provides a 0° phase shift from the reflected wave



# Plane Wave Incidence (T Solver)



Incident plane wave onto a unit cell (difference between phase diagram with and without AMC structure)



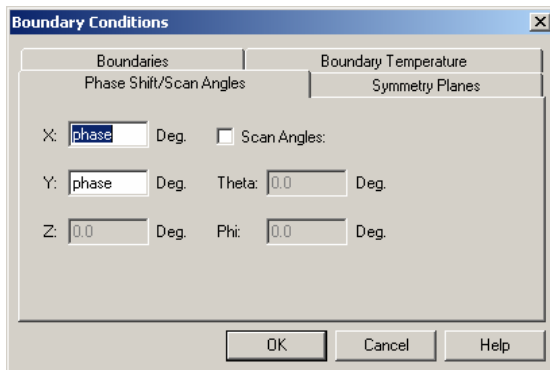
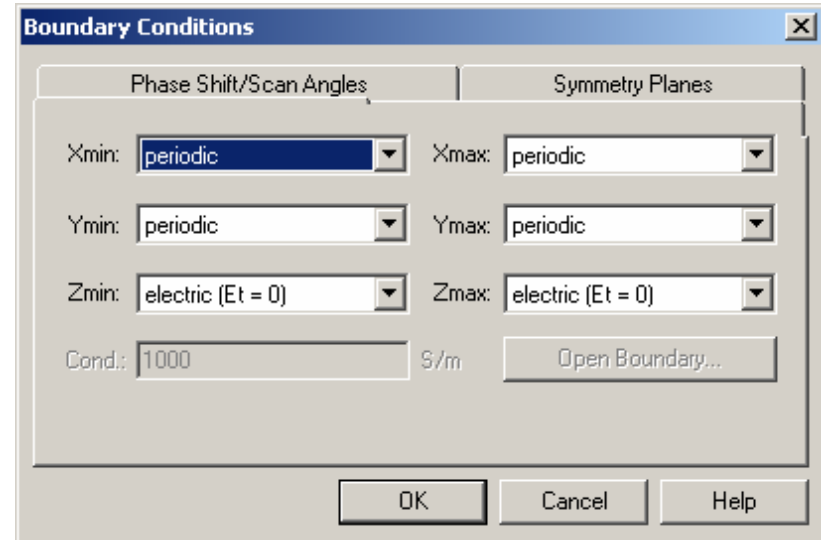
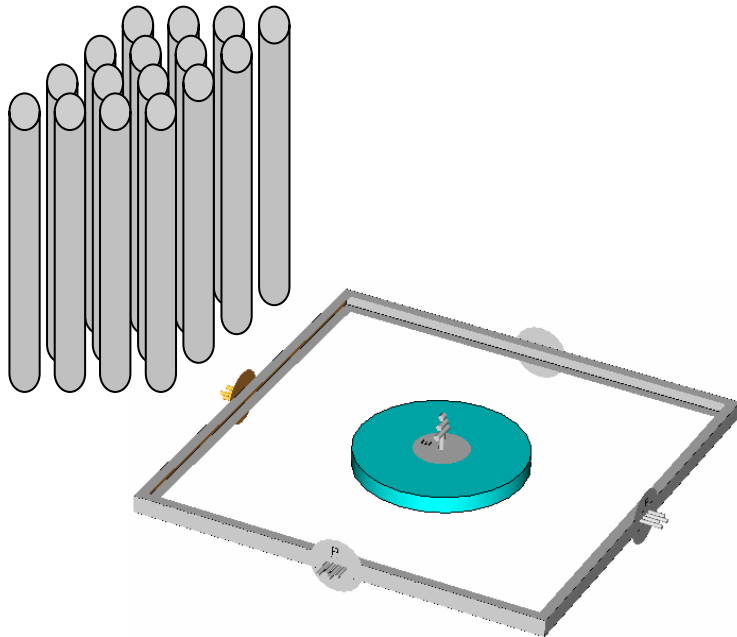
# EBG and PBG

EBG are the Electromagnetic equivalent of Photonic Band Gaps (PBG). PBG are dielectric structures with a forbidden gap for electromagnetic waves.

Surface waves on a periodic array are suppressed from propagating at the band gap frequency

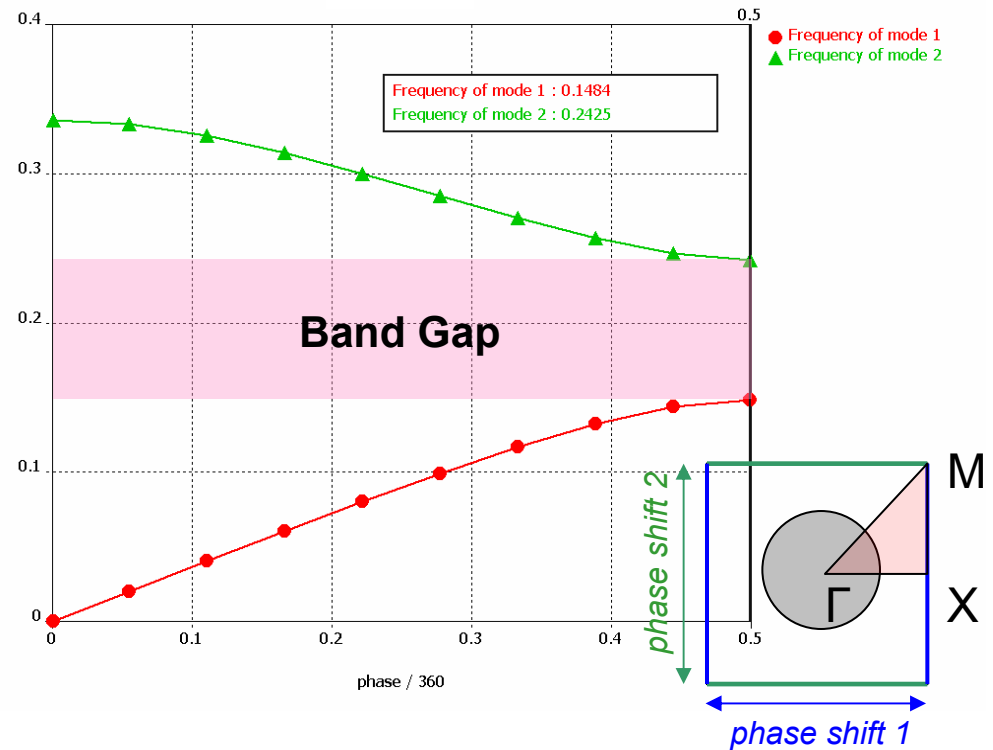
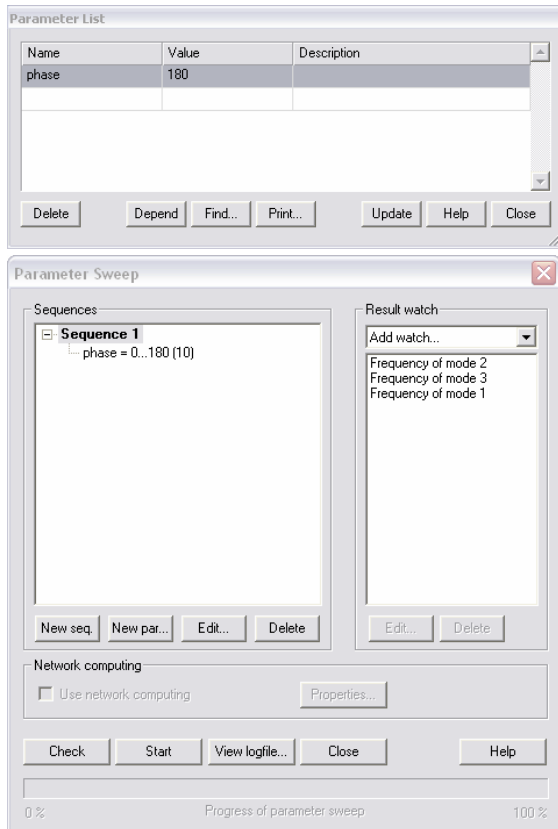
Dispersion diagrams can be used to identify EBG/PBG regions

# Unit Cell Modelling (E Solver)



- Periodic boundary conditions are used to model the whole crystal structure
- Z axis boundaries are either E or H walls, in order to obtain TE and TM modes

# Dispersion Diagram



Eigen mode solver parameter sweep is used to step through the phase assigned to the periodic boundaries

Each third of the overall dispersion curve can be reproduced by plotting found Eigen solutions against boundary condition phases

# LHM

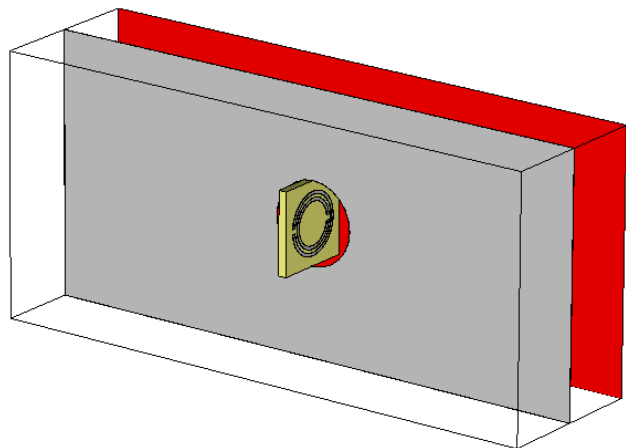
All transparent or translucent materials that we know of possess positive refractive index

Materials with simultaneously negative  $\varepsilon$  and  $\mu$  are frequently referred to as left handed, negative refractive index and double negative materials

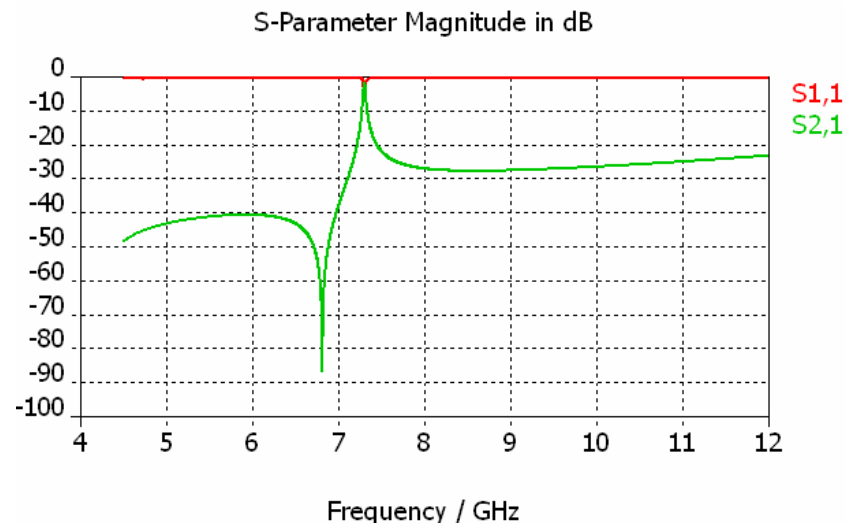
In these materials, the group velocity and phase velocity are anti-parallel

Artificially structured materials mimic the negative  $\mu$  with SRR and the negative  $\varepsilon$  by an array of conducting wires where the unit cell dimensions are  $\ll \lambda$

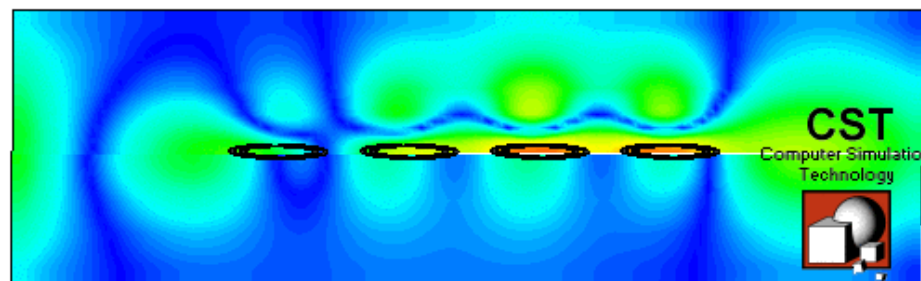
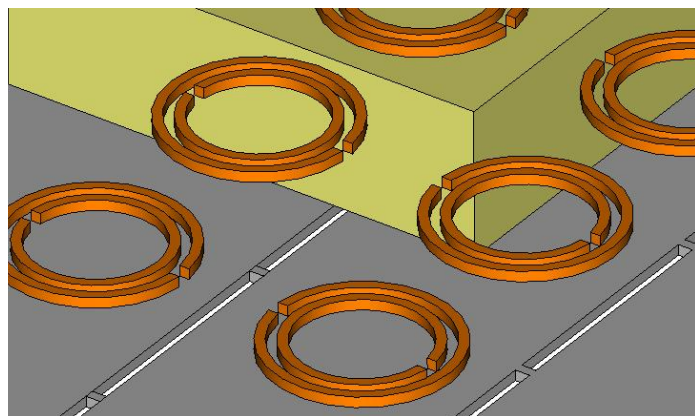
# LHM Split Ring Resonator



An edge-coupled SRR design with waveguide ports



Port excitation from left to right but reversed phase propagation in the SRR region



# Summary

**Passive and Active FSS** arrays exhibit band stop or band pass filter responses

**Unit cell** with appropriate boundary conditions allow to accurately model an infinite periodic array

**T solver** with E and H boundaries (and waveguide ports) can be used to model 0 degree incidence

**F solver** with unit cell boundaries allow arbitrary angles of incidence with Plane wave incidence

**E solver** with periodic boundaries is used to step through the phase assigned to the periodic boundaries to solve for the Eigen modes against phase