

Cognitive Radio: an information theoretic perspective

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in collaboration with:

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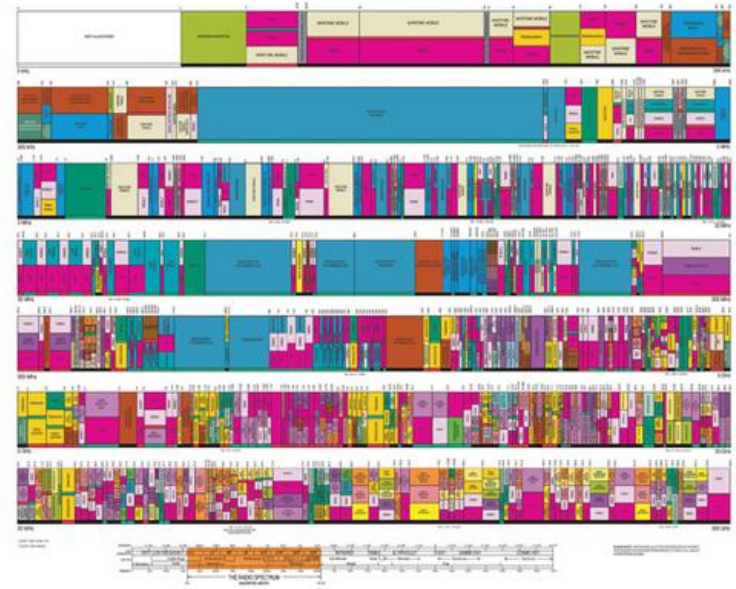
Diana Maamari, Ph.D. candidate @ UIC, and

Natasha Devroye, prof. @ UIC.

Motivations

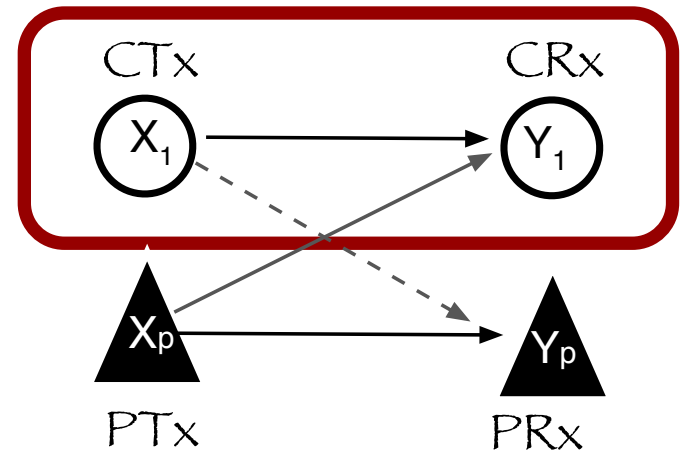
- Coexisting devices on a radio channel interfere with one another.
- Prime frequency bands all licensed with almost no free band for new services.

UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM



Motivations

- Is it possible to coexist in overcrowded spectrum without degrading existing users/services?
- Idea: use smart devices with advanced sensing/processing capabilities.



Motivations

- Major problems: not technical but regulatory
- Currently, divide-and-set-aside:
 - spectrum divided into distinct bands;
 - regulated communication uses in each band;
 - license each band for exclusive use (ex, cellular, TV, radio, navigation, emergency, defense, etc).
- This approach has pros and cons ...

Motivations

- Some bands are shared/unlicensed to encourage innovation and reduce cost to purchase licensed spectrum (ex, 2.4GHz: Bluetooth, 802.11b/g/n WiFi, etc.).
- Killed by their own success? too much interference.

Motivations

- Cognitive radio aims to bring the advantages of unlicensed bands to licensed bands without disrupting existing services.
- But how?

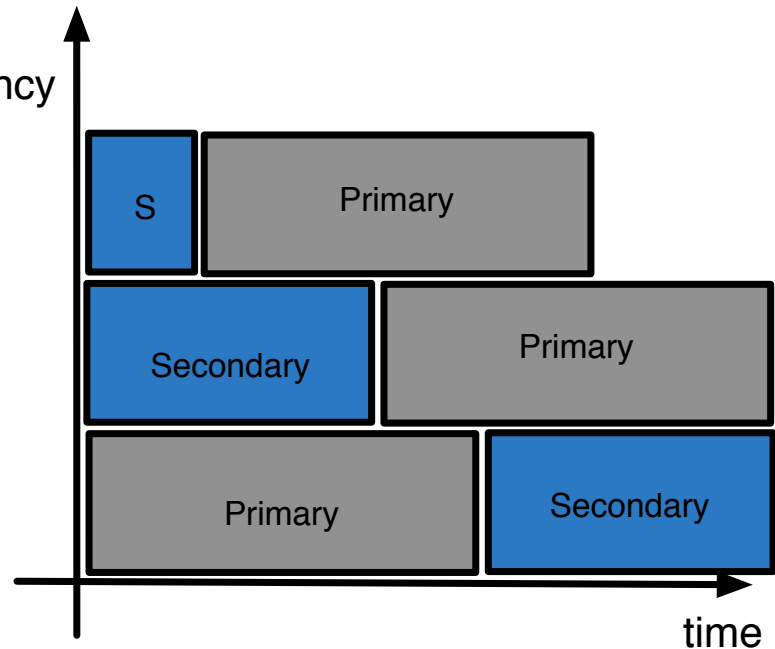
Cognitive Radio (CR)

- CR is a wireless communication system with side information about:
 - the channel activity,
 - channel conditions,
 - user' codebooks/messages.
- CR devices seek to **interweave**, **underlay** or **overlay** their signals with those of existing users without impacting their QoS.

Breaking Spectrum Gridlock with Cognitive Radios: An Information Theoretic Perspective, Goldsmith et al, *Proceedings of IEEE*, 2009.

Interweave CR

- CR opportunistically exploits spectral holes to communicate without disrupting primary transmissions.
- Needs knowledge about channel activity (extensively studied in CommTh and SigProc).

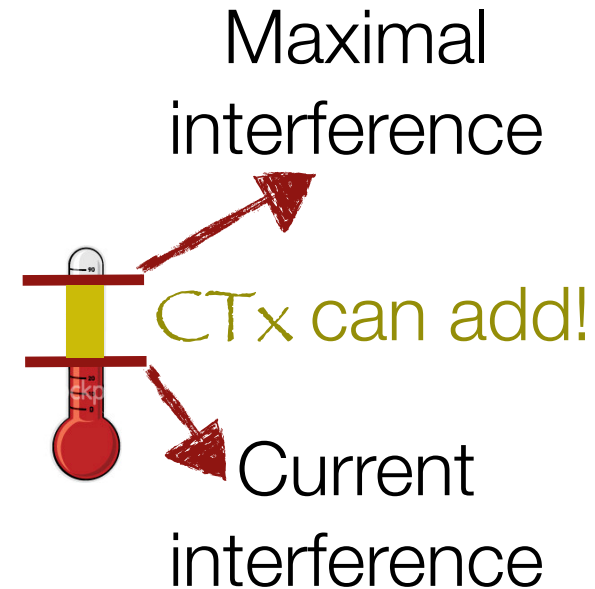
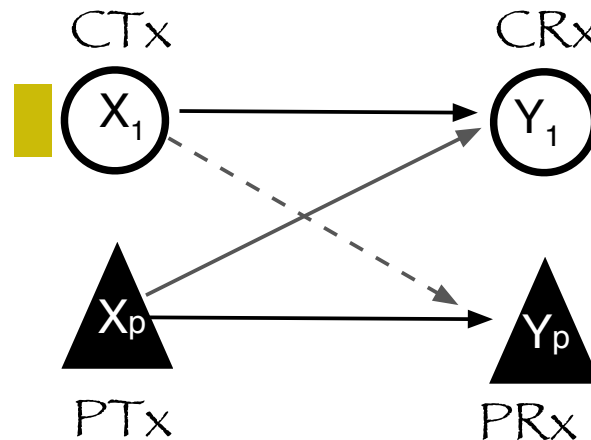


Joseph Mitola, "Cognitive Radio: An Integrated Agent Architecture for Software Defined Radio," PhD Dissertation, KTH, Sweden, December 2000

Underlay CR

- CR sends if interference at PRx is below a fixed interference margin (MIMO or UWU)
 - Pros: primary users are protected
 - Cons: short range communication

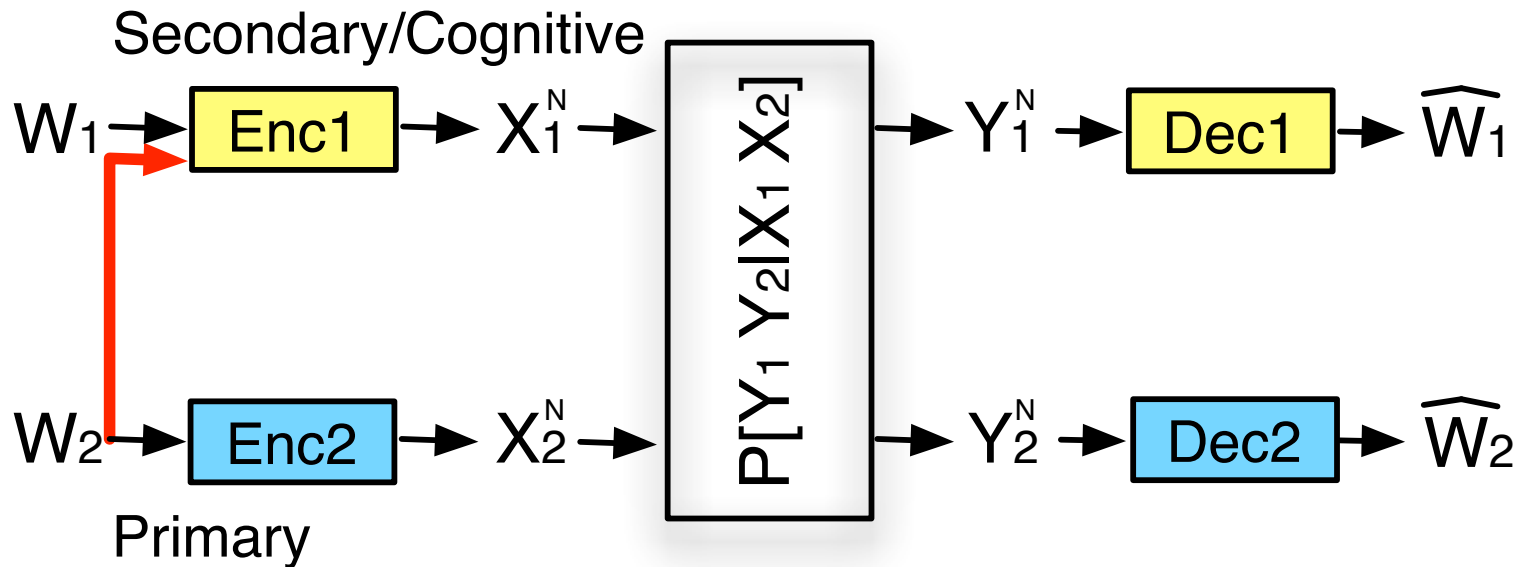
Determines power level



Overlay CR

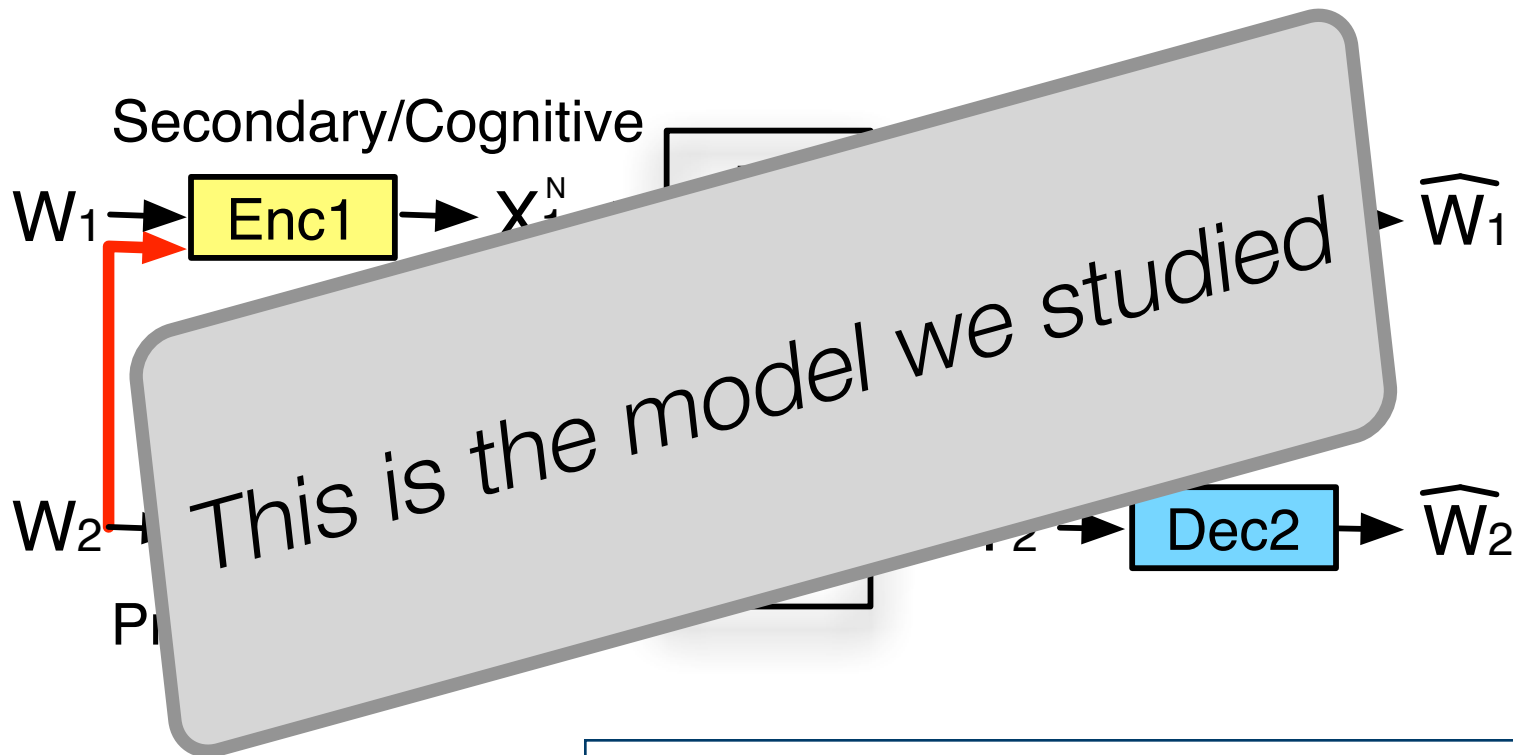
- CR uses sophisticated signal processing and coding to maintain or improve the communication of PR while achieving its own communication goals.
- Needs knowledge of primary codebooks (ex from standards) and possibly primary messages (ex after first transmission).

IT overlay CR



N. Devroye, P. Mitran, V. Tarokh, Achievable Rates in Cognitive Radio Channels," IEEE Transactions on Information Theory, vol. 52, pp. 1813–1827, May 2006

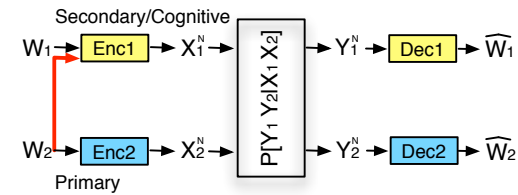
IT overlay CR



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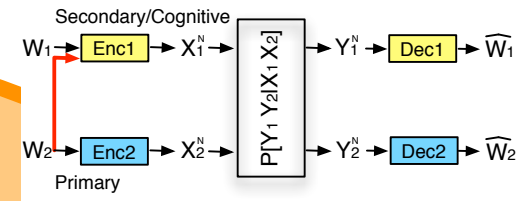
Past Work - outer bounds

the smaller,
the better



Past Work - outer bounds

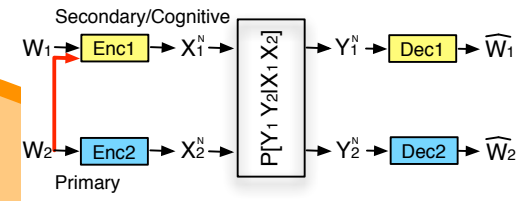
the smaller,
the better



Devroye *et al* IT06
(Broadcast Channel)

Past Work - outer bounds

the smaller,
the better

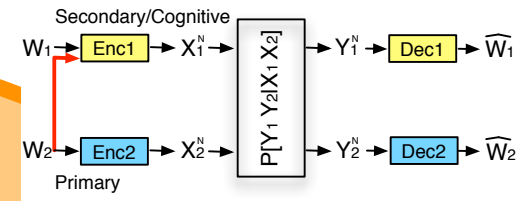


Wu et al IT07
(1 aux.RVs)

Devroye et al IT06
(Broadcast Channel)

Past Work - outer bounds

the smaller,
the better



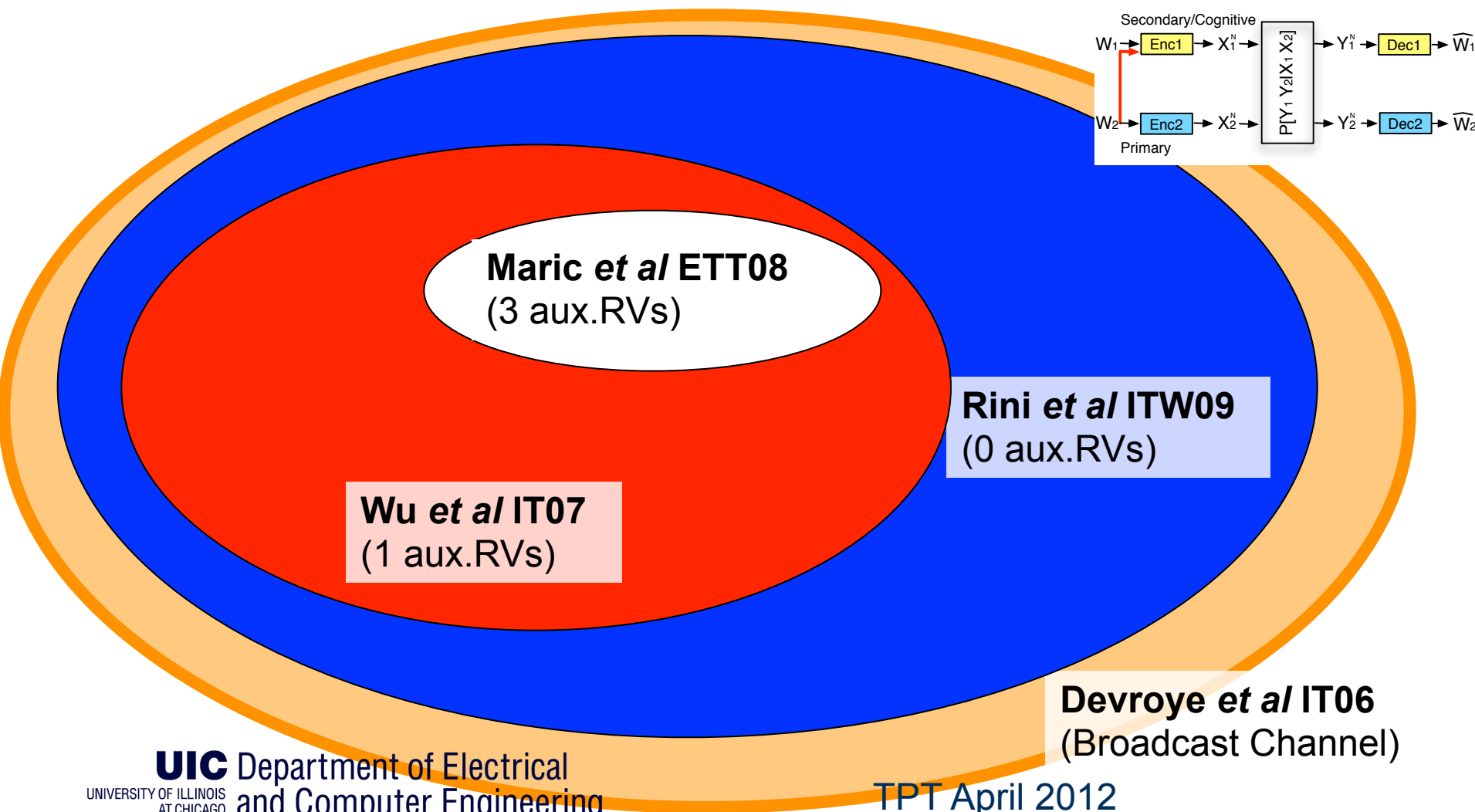
Maric *et al* ETT08
(3 aux.RVs)

Wu *et al* IT07
(1 aux.RVs)

Devroye *et al* IT06
(Broadcast Channel)

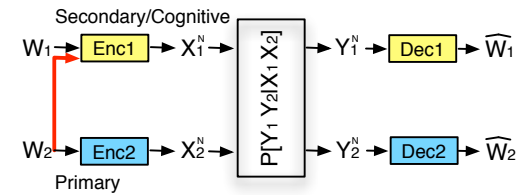
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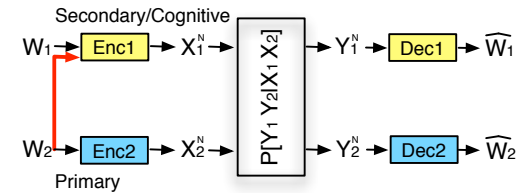
Past Work - inner bounds

the larger,
the better



Past Work - inner bounds

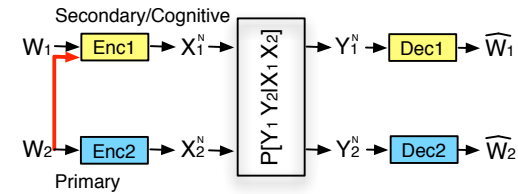
the larger,
the better



Maric *et al* ETT08

Past Work - inner bounds

the larger,
the better

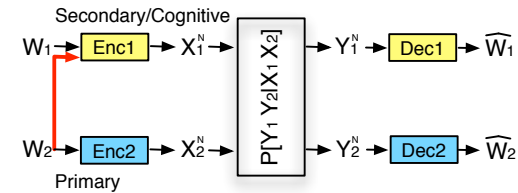
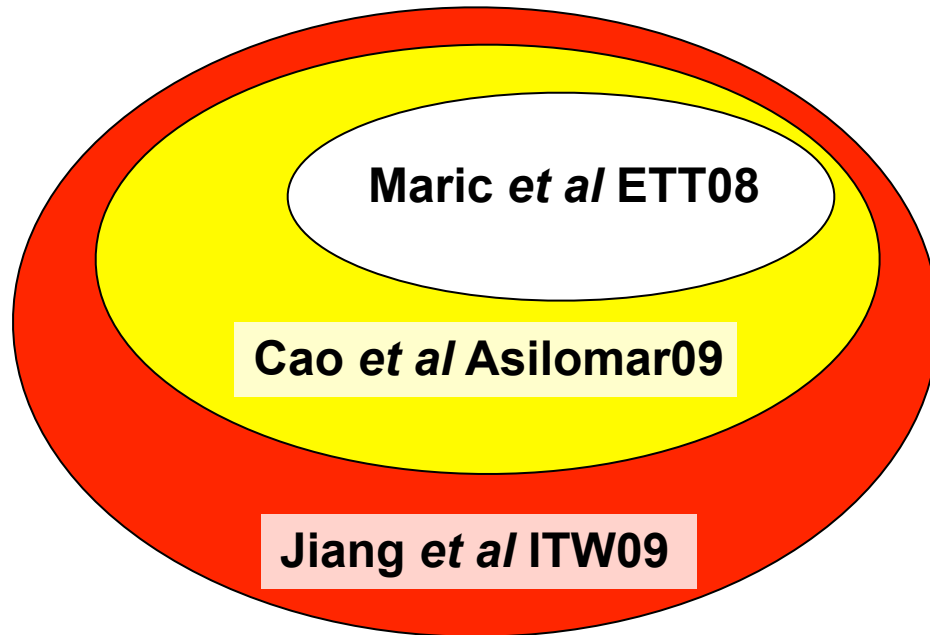


Maric *et al* / ETT08

Cao *et al* / Asilomar09

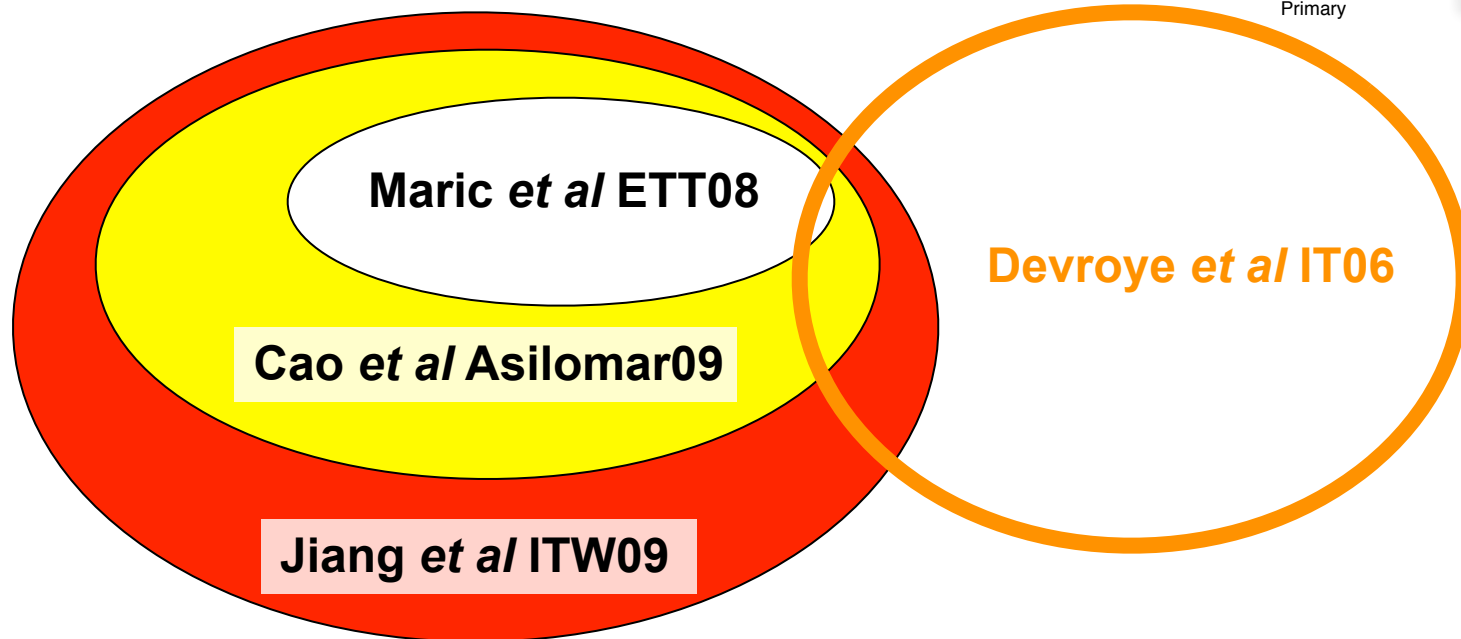
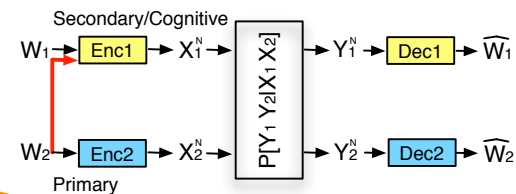
Past Work - inner bounds

the larger,
the better



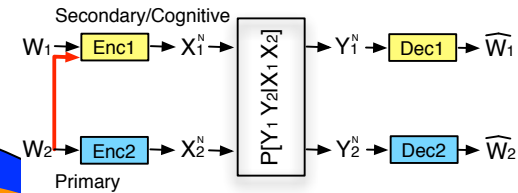
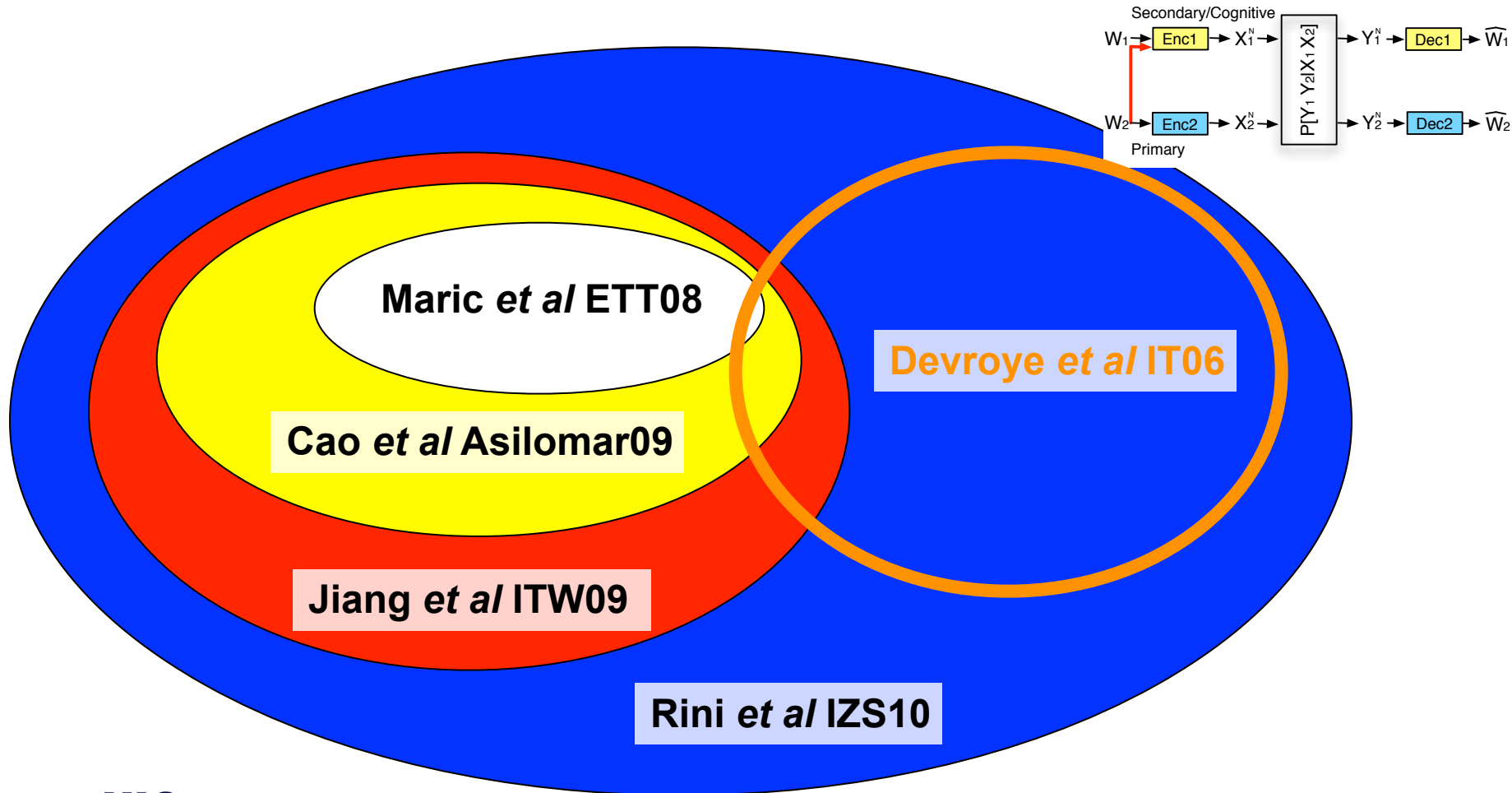
Past Work - inner bounds

the larger,
the better



Past Work - inner bounds

the larger,
the better



Past Work - capacity

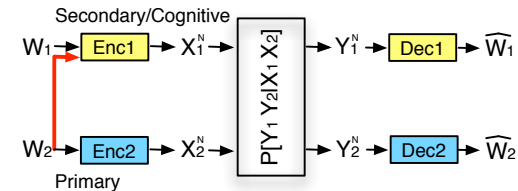
- **Weak interference** [W. Wu et al IT 2007,

Jovicic et al IT 2006 for AWGN]

- **(Very) strong interference** [I. Maric et al IT 2007]

- **Some semi-deterministic** [Y. Cao et al Asilomar 2009]

- **Some Z-channel** [N. Liu et al ISIT 2009]



Contributions: general CIFC

- Computable outer bound (the tightest is still by Maric et al at ETT 2008)
- Largest inner bound
- Capacity in “better cognitive decoding”
- Capacity for semi-deterministic channels

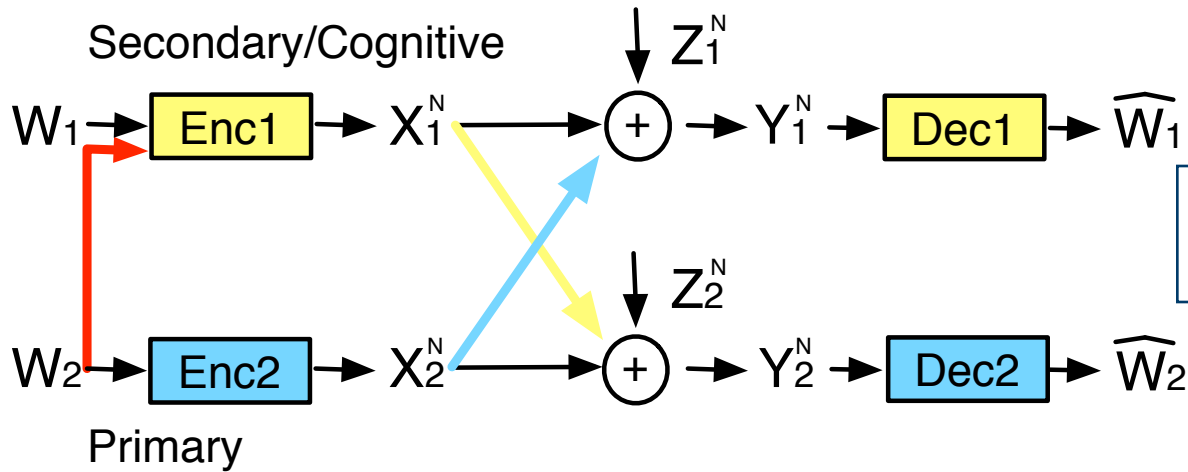
S. Rini et al, “New Inner and Outer Bounds for the Memoryless Cognitive Interference Channel and some Capacity Result”, IT 2011

Contributions: AWGN CIFC

- Unifying outer bound (for weak and strong interference)
- “BC with degraded message set” outer bound for strong interference
- Capacity in “primary decodes cognitive”
[subset also presented by J. Jiang et al ICC 2011]
- Capacity for some Z-channels
[extension claimed by M. Vaezi et al CWIT 2011]
- Capacity to within 1 bit
or a factor 2

S. Rini et al, “Inner and Outer Bounds for the Gaussian Cognitive Interference Channel and New Capacity Results”, IT 2012

AWGN CIFIC

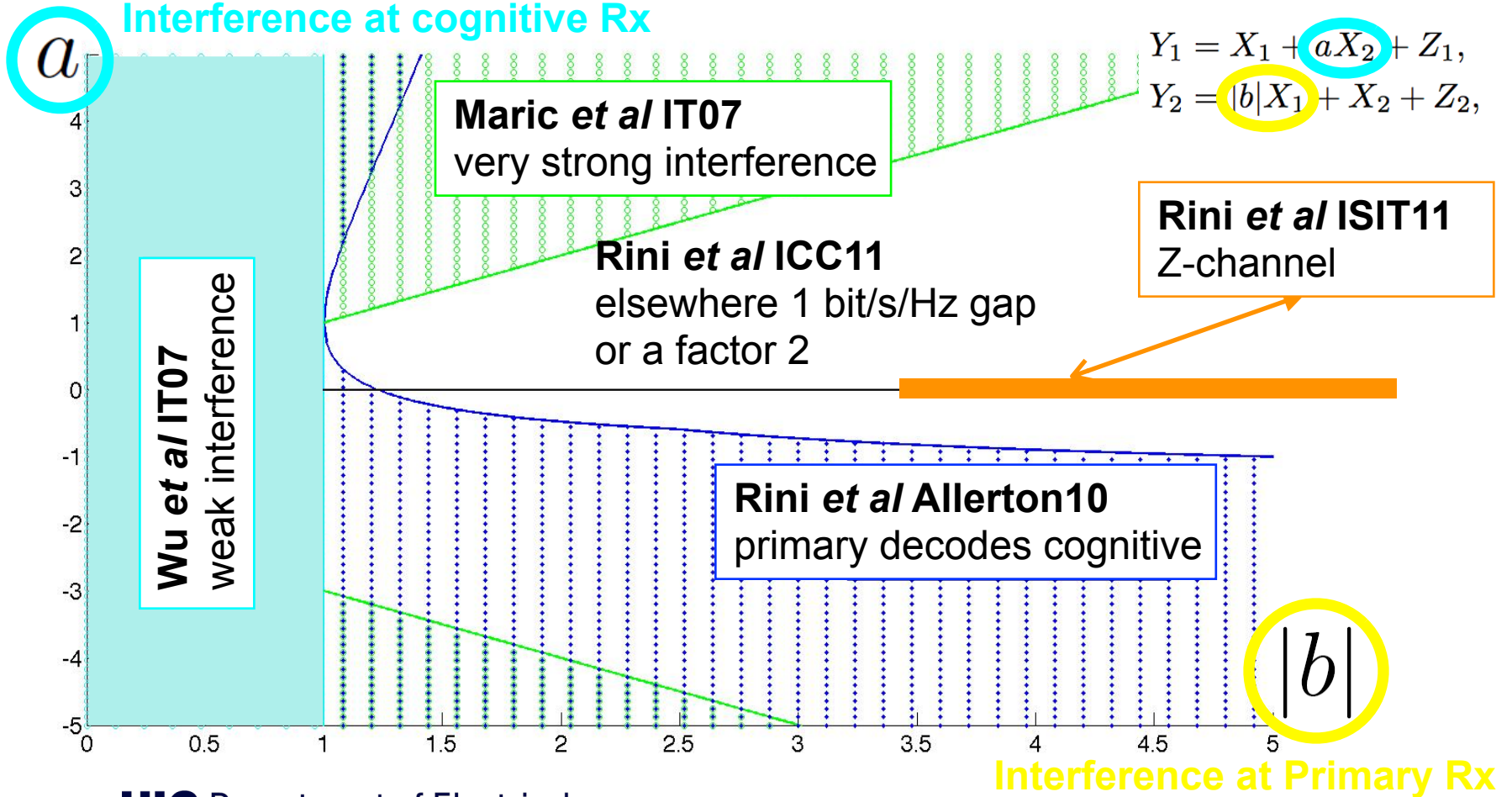


Most results extend to a general memoryless CIFIC

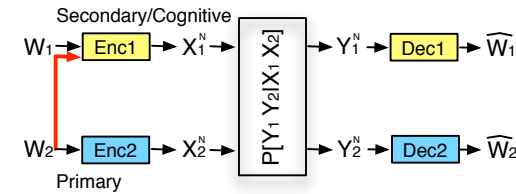
$$\begin{aligned}
 Y_1 &= X_1 + aX_2 + Z_1, \\
 Y_2 &= |b|X_1 + X_2 + Z_2,
 \end{aligned}$$

$$\begin{aligned}
 X_1^N &= f_1(W_1, W_2) : \frac{1}{N} \sum_{t=1}^N \mathbb{E}[|X_{1,t}|^2] \leq P_1, \\
 X_2^N &= f_2(W_2) : \frac{1}{N} \sum_{t=1}^N \mathbb{E}[|X_{2,t}|^2] \leq P_2, \\
 Z_j &\sim \mathcal{N}(0, 1), \quad j = 1, 2.
 \end{aligned}$$

Contributions: AWGN CIFC



Outer Bound



- Wu et al IT 07 (BC argument; not the tightest)

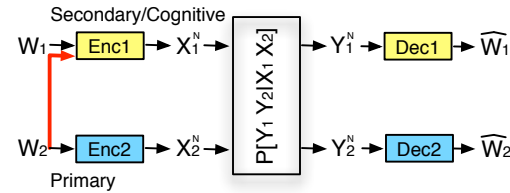
$$R_1 \leq I(Y_1; X_1 | X_2),$$

$$R_2 \leq I(U, X_2; Y_2),$$

$$R_1 + R_2 \leq I(U, X_2; Y_2) + I(Y_1; X_1 | U, X_2),$$

- U: help from the cognitive to the primary
- [Rini et al IT11] tight for “semi-deterministic” channels and for “better cognitive decoding”

Outer Bound



- Rini et al IT 11 (IFC argument)

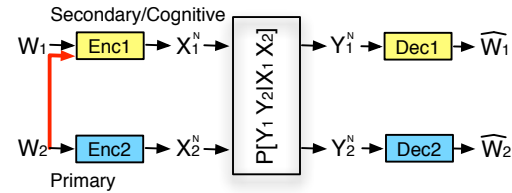
$$R_1 \leq I(Y_1; X_1 | X_2),$$

$$R_2 \leq I(X_1, X_2; Y_2),$$

$$R_1 + R_2 \leq I(X_1, X_2; Y_2) + I(Y_1; X_1 | Y_2', X_2),$$

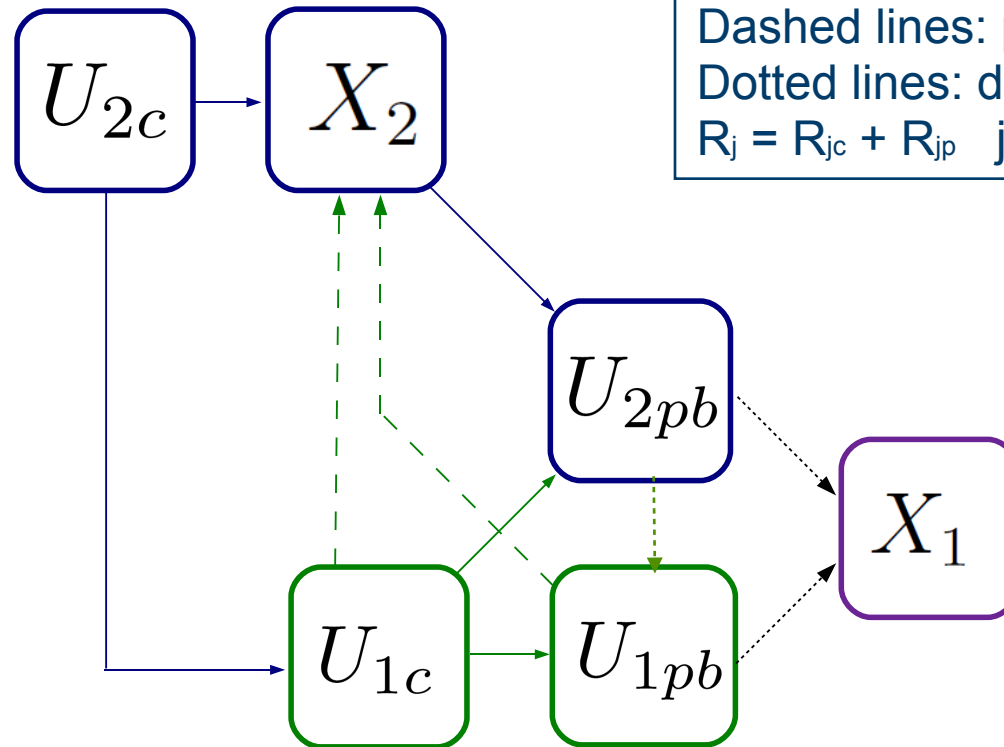
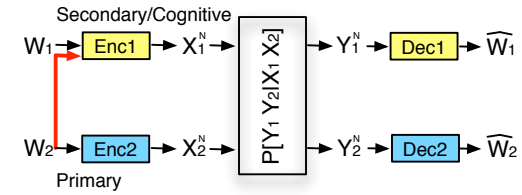
- does not contain auxiliary RVs, hence it is computable
- [Rini et al IT12]: it unifies weak and strong interference outer bounds for AWGN

Inner Bound



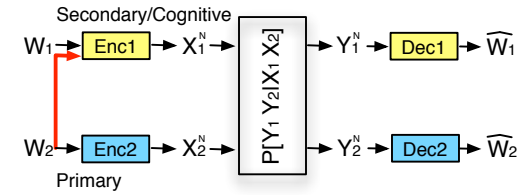
- Rate splitting:
 - common message (decoded @ non intended destination)
 - private message (treated as noise @ non intended destination)
- Superposition coding/nesting: start with primary-common end with cognitive-private
- Interference pre-coding/binning: remove effect of interf. non-causally known at CTx

Inner Bound

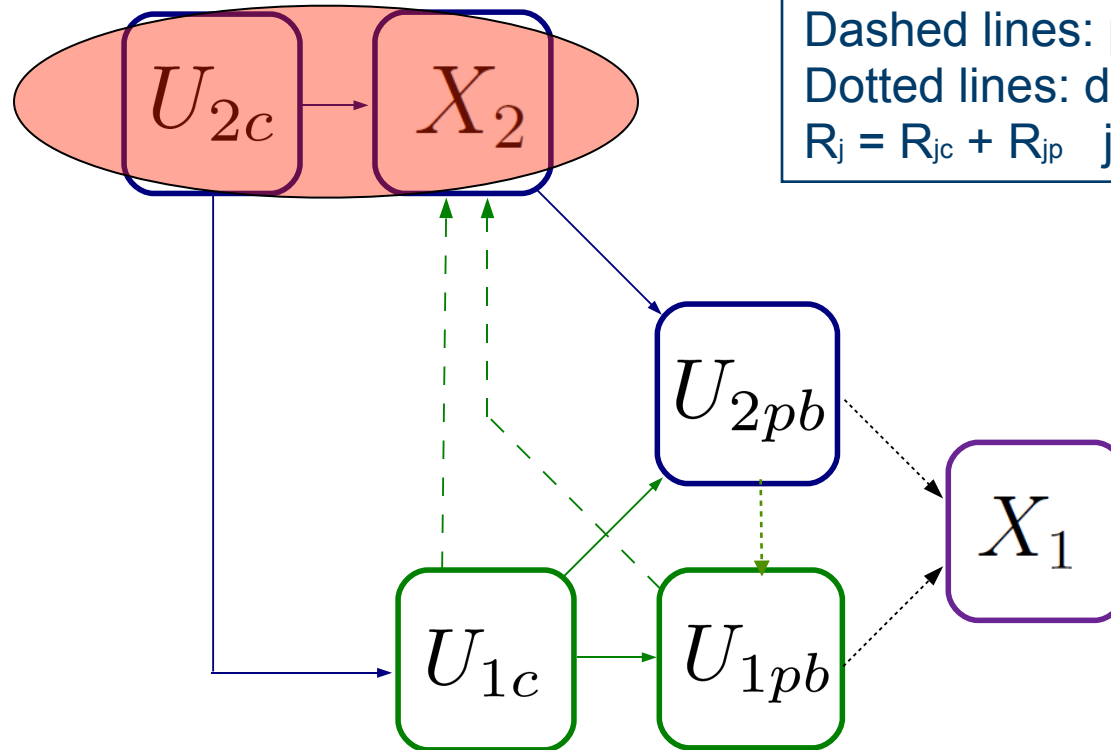


Thick lines: superposition
 Dashed lines: pre-coding
 Dotted lines: deterministic function
 $R_j = R_{jc} + R_{jp} \quad j=1,2$

Inner Bound

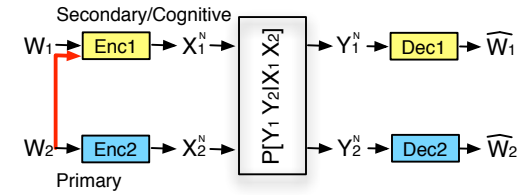


@ primary Tx: common/private split

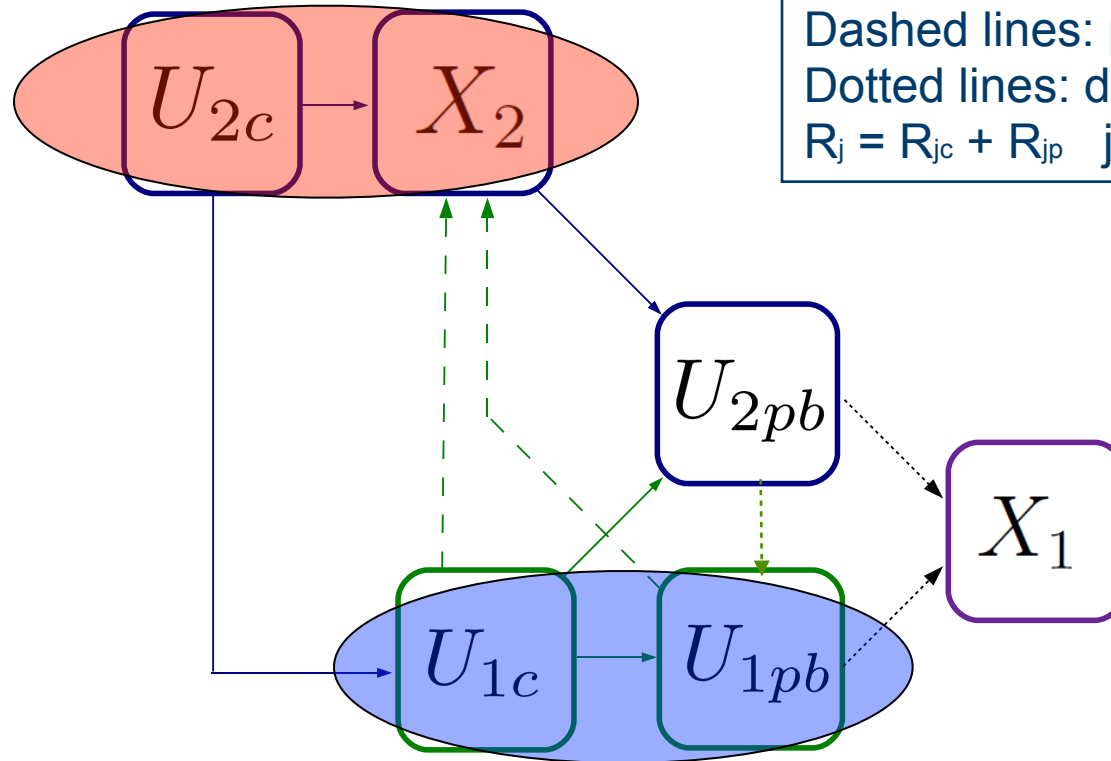


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Inner Bound

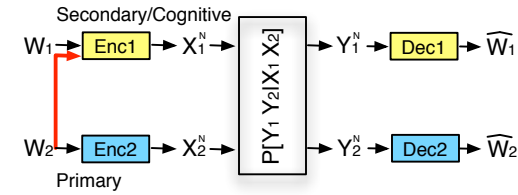


@ primary Tx: common/private split

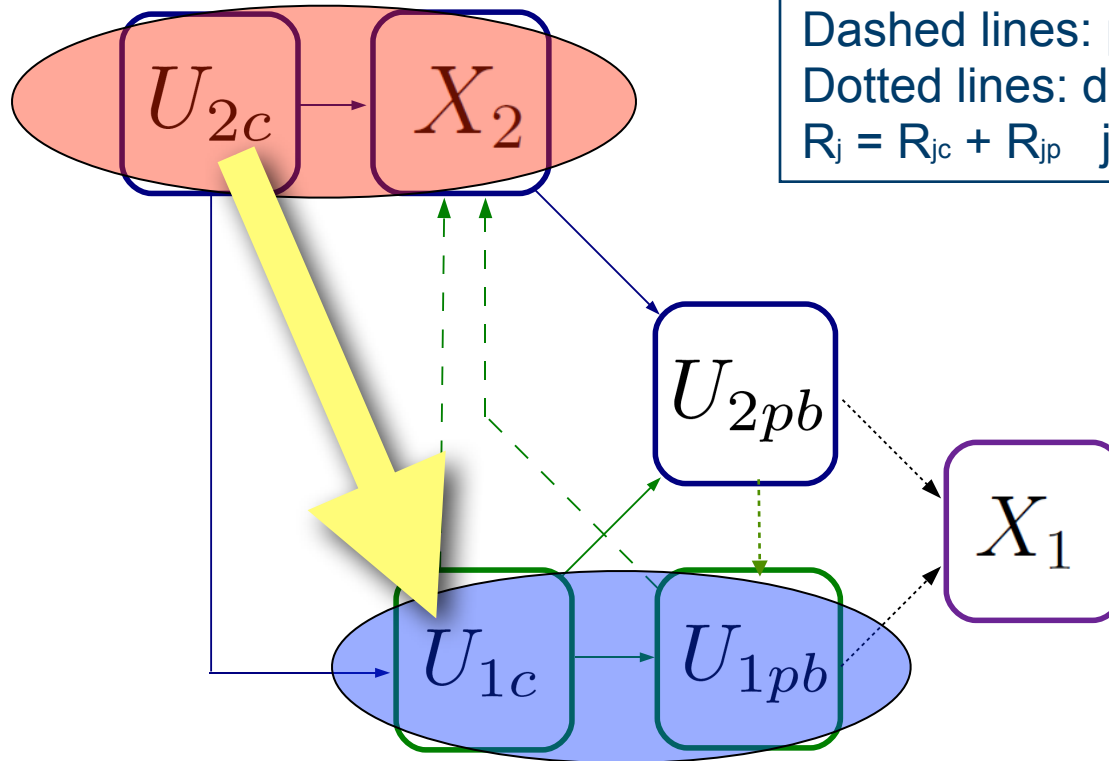


@ cognitive: common/private split

Inner Bound



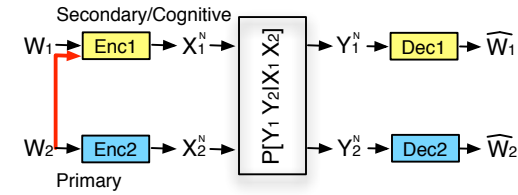
@ primary Tx: common/private split



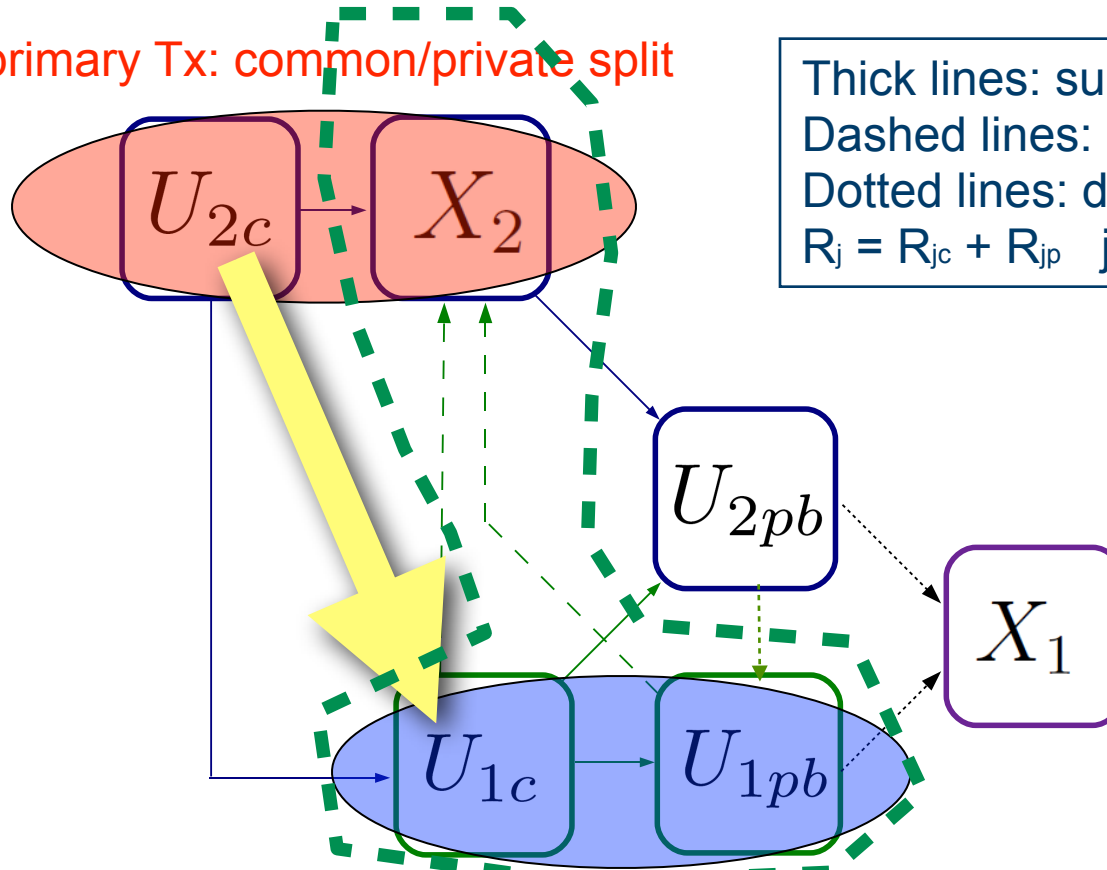
Thick lines: superposition
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 $R_j = R_{jc} + R_{jp} \quad j=1,2$

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Inner Bound



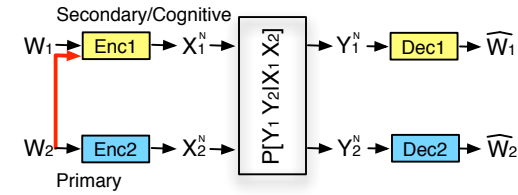
@ primary Tx: common/private split



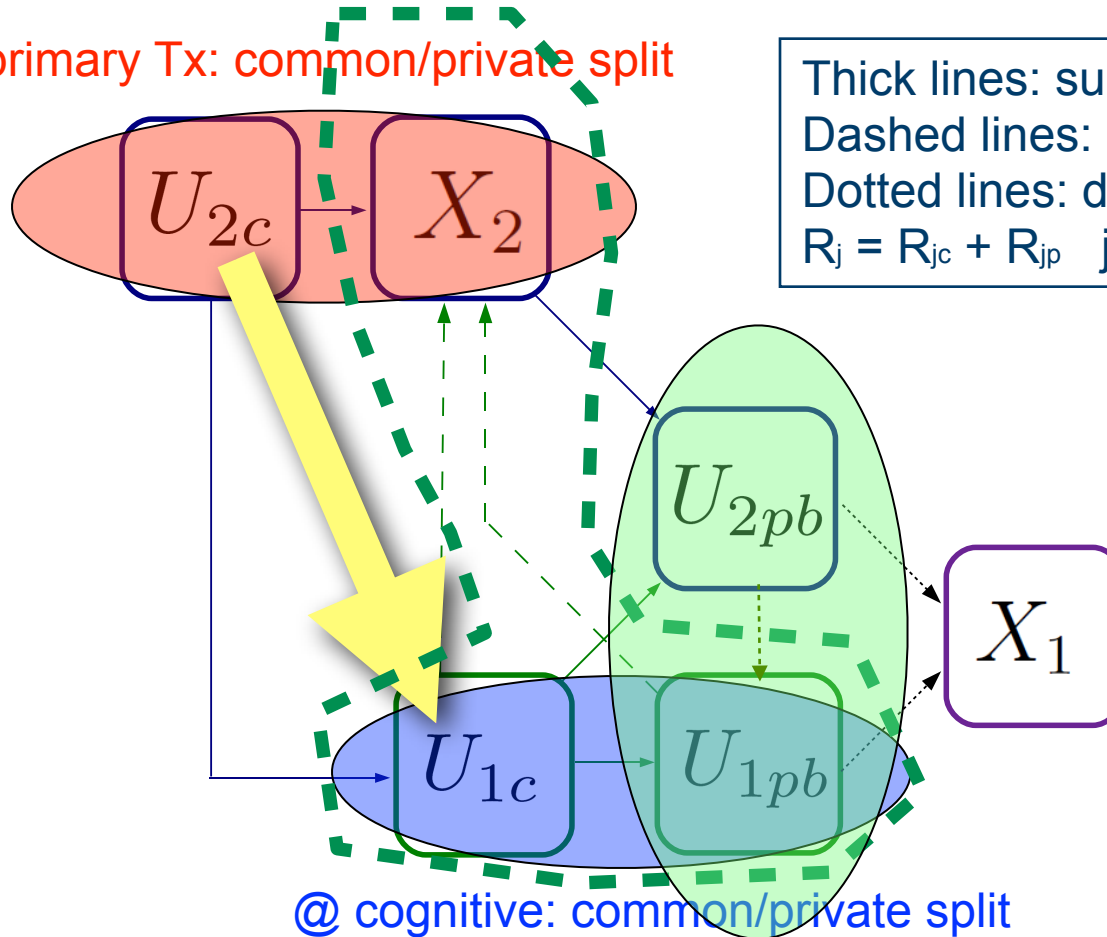
Thick lines: superposition
 Dashed lines: pre-coding
 Dotted lines: deterministic function
 $R_j = R_{jc} + R_{jp} \quad j=1,2$

@ cognitive: common/private split

Inner Bound



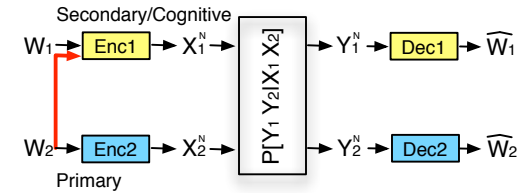
@ primary Tx: common/private split



@ cognitive: common/private split

Thick lines: superposition
 Dashed lines: pre-coding
 Dotted lines: deterministic function
 $R_j = R_{jc} + R_{jpb} \quad j=1,2$

Inner Bound



- Overall region (not that “ugly” ...)

$$R_1 \leq I(Y_1; U_{1pb}, U_{1c} | U_{2c}) - I(U_{1pb}, U_{1c}; X_2 | U_{2c}),$$

$$R_1 \leq I(Y_1; U_{1pb} | U_{1c}, U_{2c}) + I(Y_2; U_{2pb}, U_{1c}, X_2 | U_{2c}) - I(U_{1pb}; X_2 | U_{1c}, U_{2c}),$$

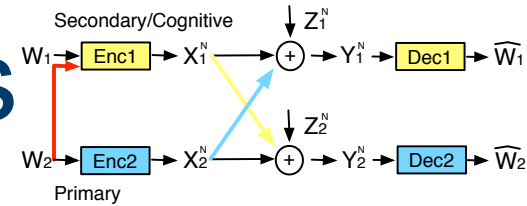
$$R_2 \leq I(Y_2; U_{2pb}, X_2, U_{1c}, U_{2c}) + I(U_{1c}; X_2 | U_{2c}),$$

$$R_1 + R_2 \leq I(Y_1; U_{1pb}, U_{1c}, U_{2c}) + I(Y_2; U_{2pb}, X_2 | U_{1c}, U_{2c}) - I(U_{1pb}; U_{2pb}, X_2 | U_{1c}, U_{2c}),$$

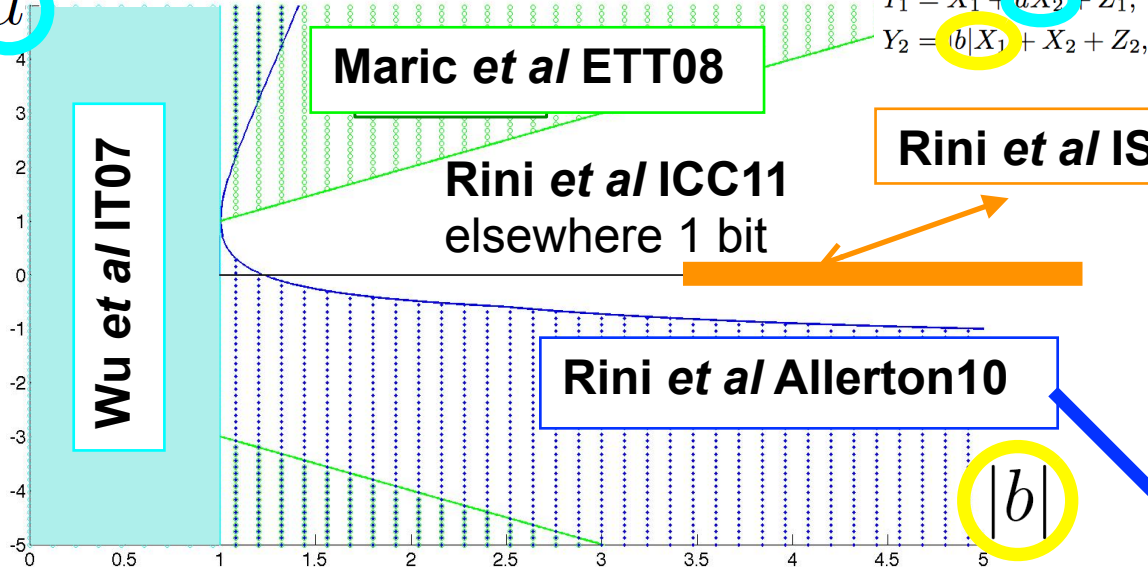
$$R_1 + R_2 \leq I(Y_1; U_{1pb} | U_{1c}, U_{2c}) + I(Y_2; U_{2pb}, X_2, U_{1c}, U_{2c}) - I(U_{1pb}; U_{2pb}, X_2 | U_{1c}, U_{2c}),$$

$$2R_1 + R_2 \leq I(Y_1; U_{1pb}, U_{1c}, U_{2c}) + I(Y_1; U_{1pb} | U_{1c}, U_{2c}) + I(Y_2; U_{2pb}, U_{1c}, X_2 | U_{2c}) \\ - I(U_{1pb}; U_{2pb}, X_2 | U_{1c}, U_{2c}) - I(U_{1pb}, U_{1c}; X_2 | U_{2c}),$$

Capacity Results



a



$$Y_1 = X_1 + aX_2 + Z_1,$$

$$Y_2 = b|X_1 + X_2 + Z_2,$$

Maric et al ETT08

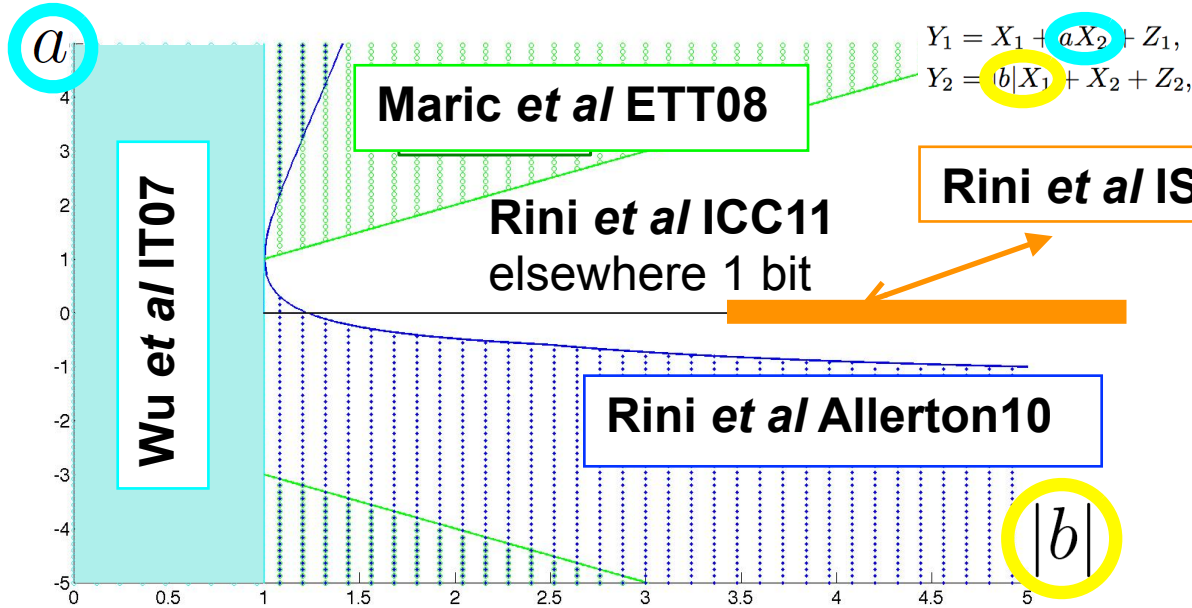
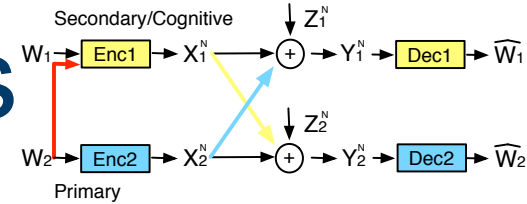
Rini et al ICC11
elsewhere 1 bit

Rini et al ISIT11

Rini et al Allerton10

Primary decodes cognitive: cognitive msg is all common & impose conditions so that the computable outer bound and inner bound match

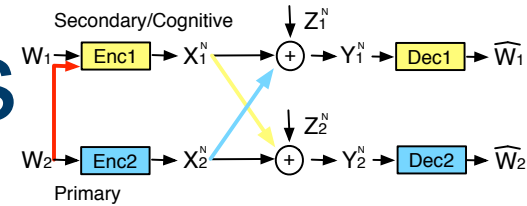
Capacity Results



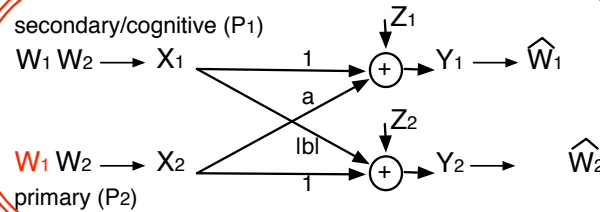
Rini et al ISIT11

Z-channel: need new outer bound!
This new outer bound only holds for AWGN ...

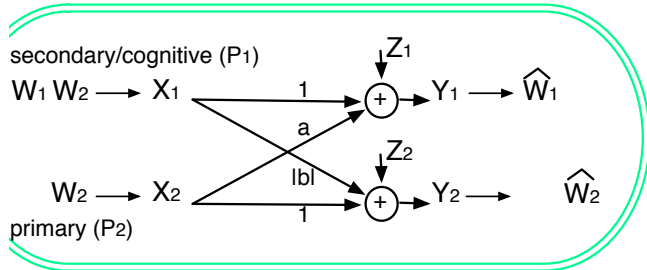
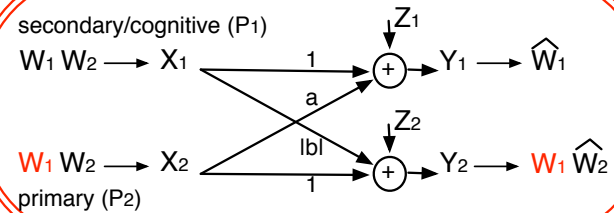
Capacity Results



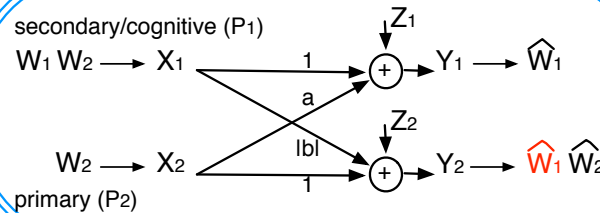
[N. Devroye et al IT 2006]



[H. Weingarten et al ISIT 2006]

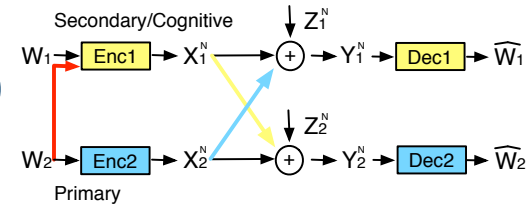


equal
for $|b| > 1$

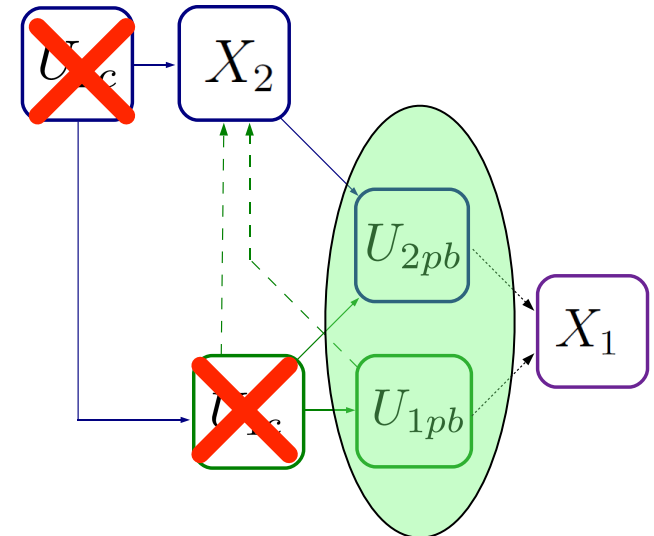
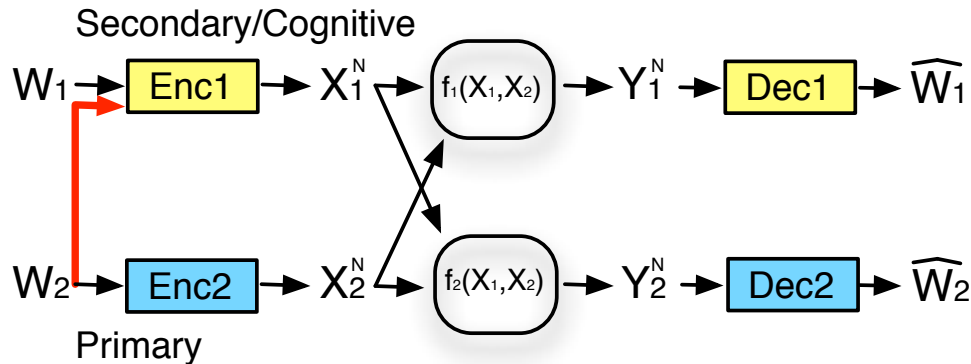


[I. Maric et al IT 2007]

1 bit additive gap



Inspired by the capacity achieving scheme for the deterministic channel: $U_{k,pb} = Y_k$

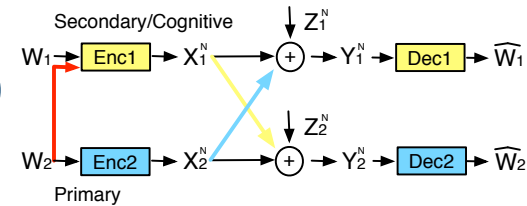


$$R_1 \leq H(Y_1 | X_2)$$

$$R_2 \leq H(Y_2)$$

$$R_1 + R_2 \leq H(Y_2) + H(Y_1 | X_2, Y_2)$$

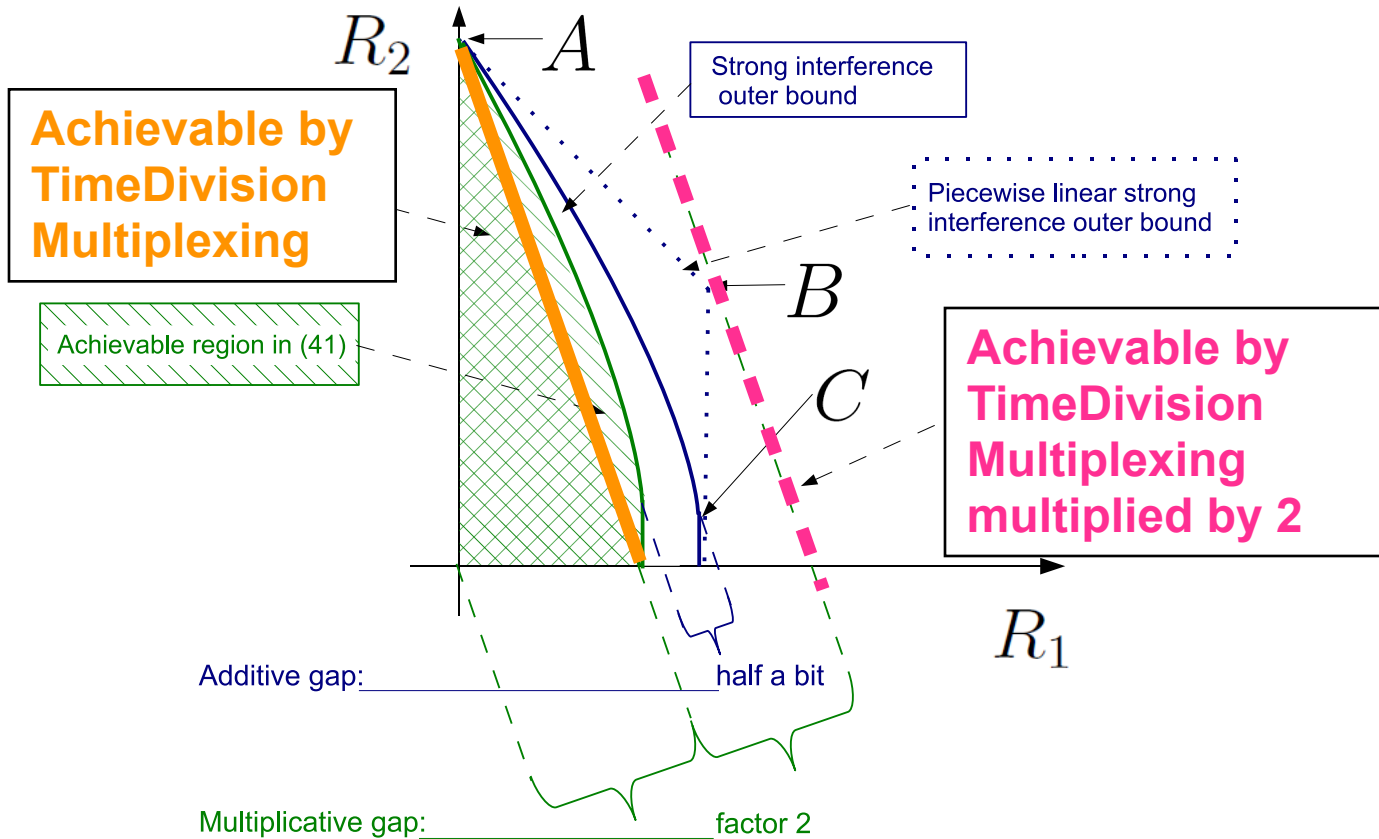
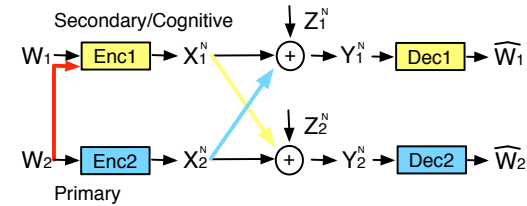
1 bit additive gap



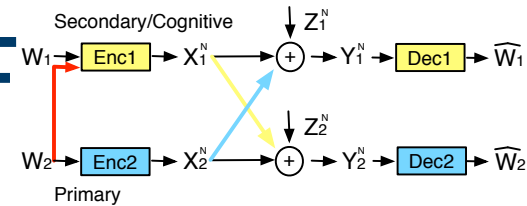
- Impossible to set $U_{k,pb} = Y_k$
- $U_{k,pb} \sim Y_k$ does the trick
- Why does it work?

$$\text{Gap} = \log(1 + \text{Var}[Y_k]/(1 + \text{Var}[U_{k,pb}])) \leq \log(1+1) = 1 \text{ bit}$$

factor 2 gap

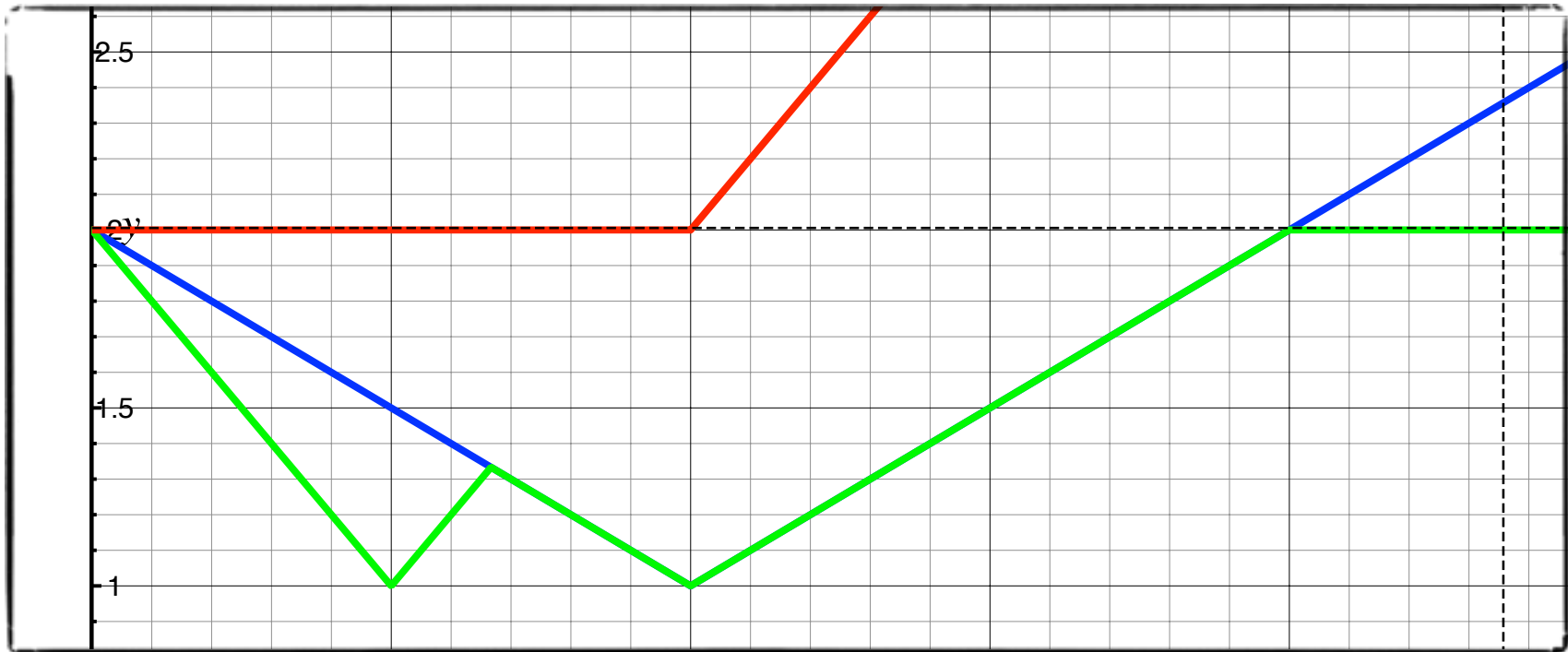
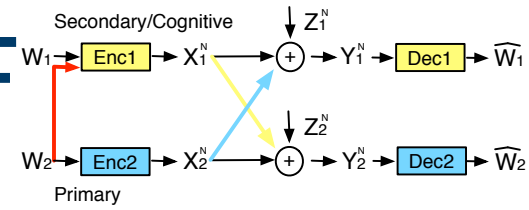


Generalized DoF

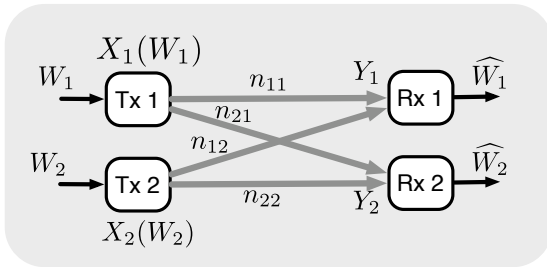


- Useful for gDoF:
 - $P_1 = P_2 := \text{SNR}$,
 - $b^2 P_1 = a^2 P_2 := \text{SNR}, \alpha$
 - $d_{2\text{-CIFC}}(\alpha)$
 $:= \max(R_1 + R_2) / \log(1 + \text{SNR})$
 $= 2\max(1, \alpha) - \alpha := V(\alpha)$

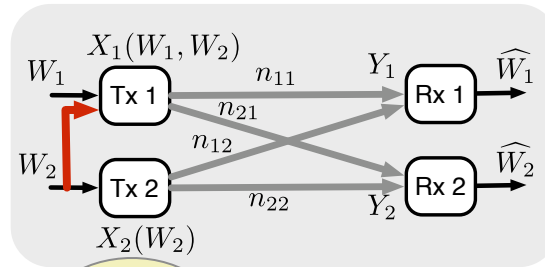
Generalized DoF



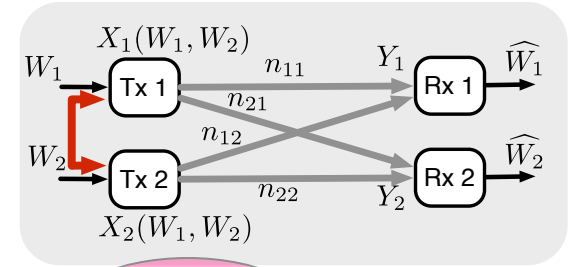
What is the value of cognition?



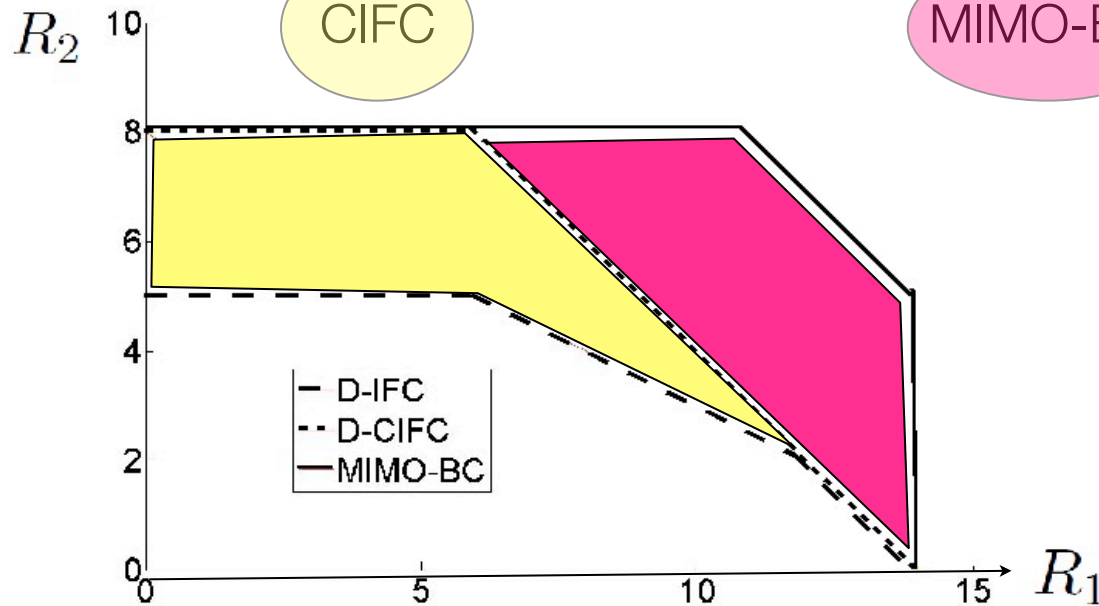
IFC



CIFIC

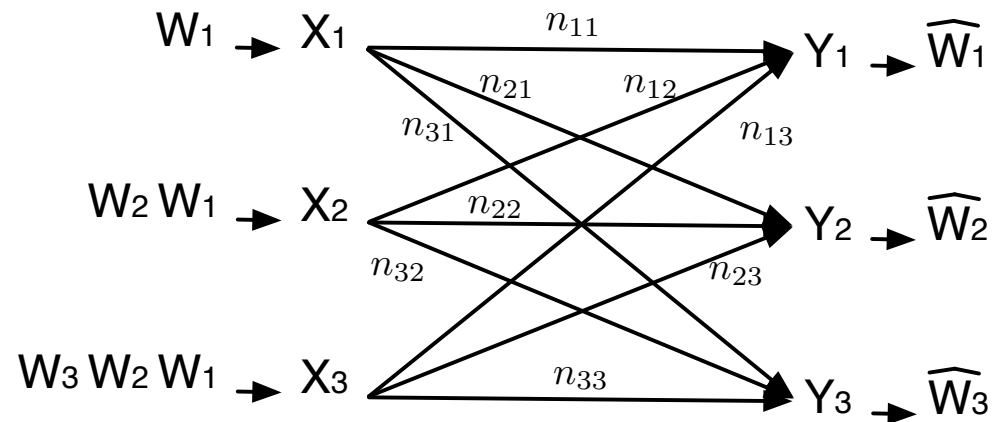


MIMO-BC



More than 2 pairs

- dGoF [Maamari et al, submitted to ISIT 2012]
 - sum-capacity for LDA-AWGN for $K=3$
 - $d_{K\text{-CIFC}}(\alpha) := K \max(1, \alpha) - \alpha$
 - $d_{K\text{-BC}}(\alpha) := K \max(1, \alpha)$



Current Work

- Cognitive channels with nested messages.
- Casal cognition, i.e., secondary users learn the primary message(s) -- a special case of cooperation/generalized feedback.
- Cognitive channels with oblivion constraints, i.e., primary users are unaware of the presence of the secondary users.

Thank you

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