



# Radio channel modeling: from GSM to LTE *and beyond...*

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- ❑ **Introduction: why do we need channel models ?**
- ❑ **Basics**
- ❑ **Narrow band channels**
- ❑ **Wideband channels**
- ❑ **MIMO channels**
- ❑ **Multi-link channels**
- ❑ **Perspectives & conclusion**

# Introduction: why do we need channel models ?

## □ From the operator's point of view

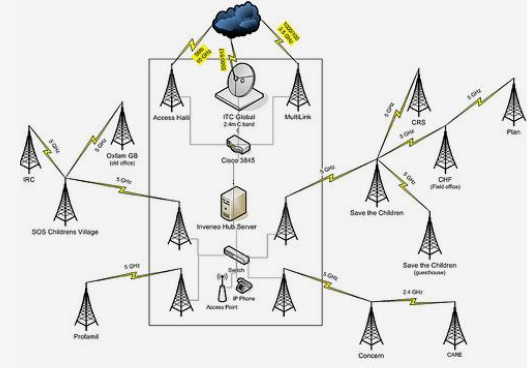
- For network planning, BST deployment
- As inputs to engineering rules & tools

## □ From the manufacturer's point of view

- For performance evaluation
- For device/equipment design optimization

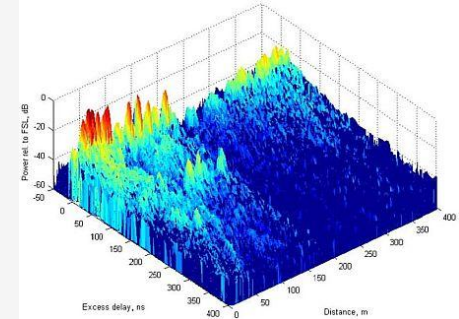
## □ From the researcher's point of view

- For trying novel network architectures
- For evaluating novel antenna technologies

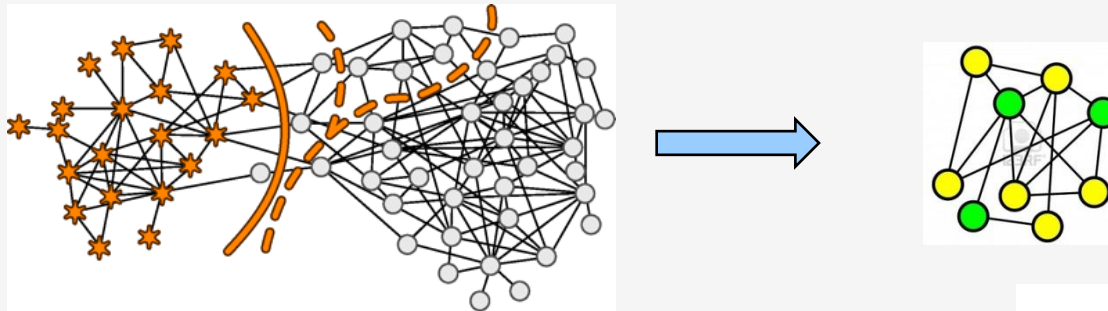


## □ How to proceed ?

1. Propagation research done by researchers



2. Extract the substance of the channel physics into something tractable

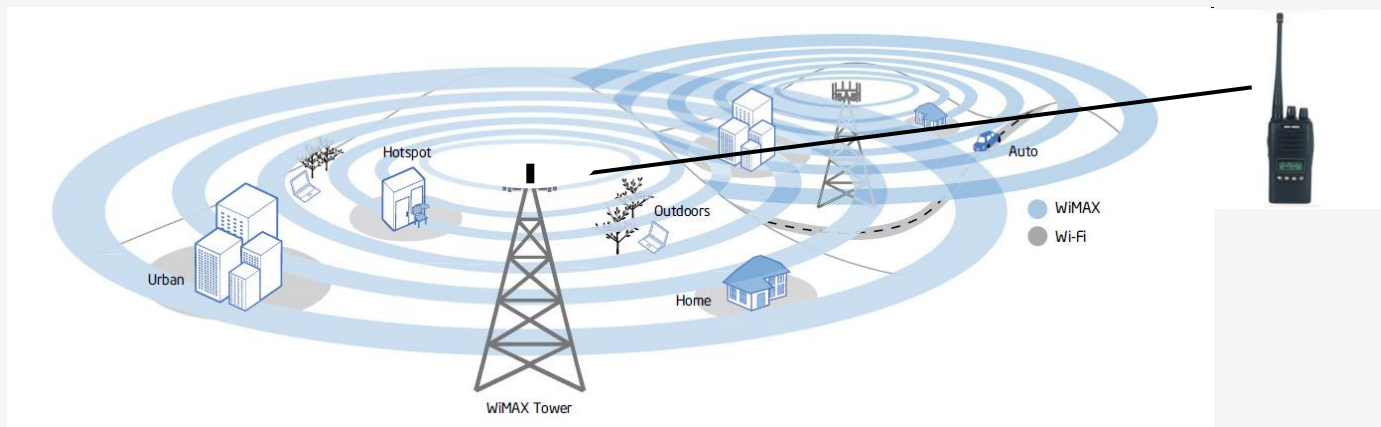


3. Standardize channel models *de-facto* or through official bodies: COST, IEEE, ETSI, 3GPP...



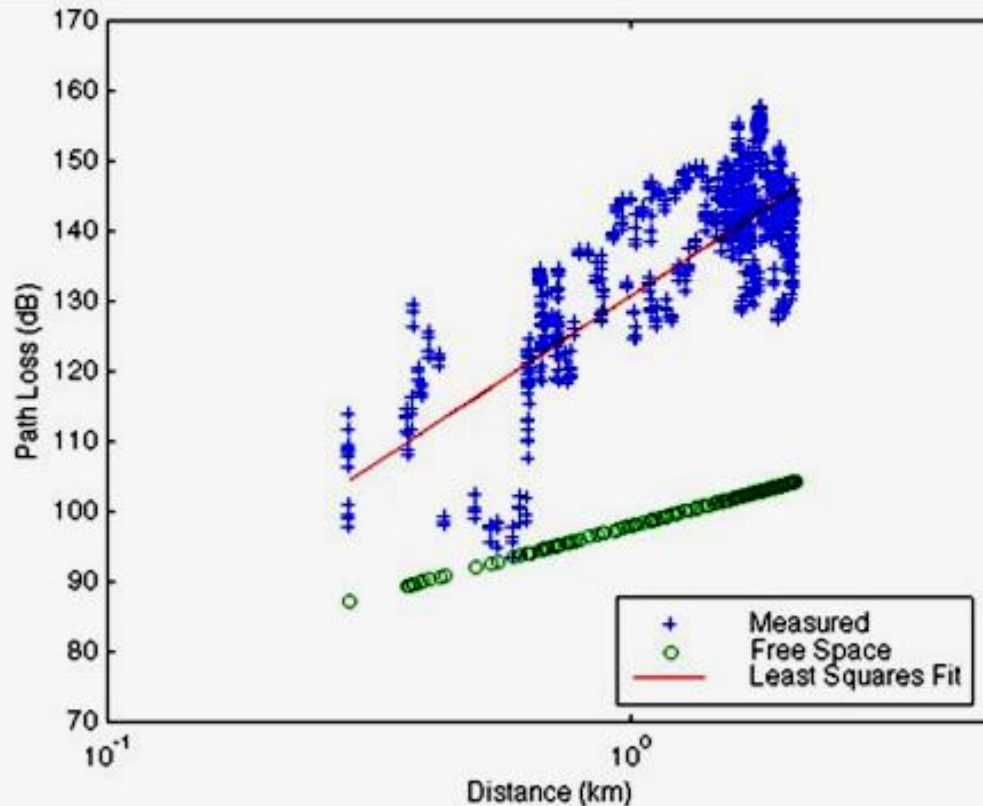
## □ Example - back to basics: GSM (operator's need)

- The main need: to model the attenuation (path loss) vs. distance, for « typical » environments and varying BST height



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## □ Example - back to basics: GSM (operator's need)

- The main need: to model the mean attenuation (path loss) vs. distance, for « typical » environments and varying BST height

COST-Hata model for suburban or rural environments:

$$L = 46.3 + 33.9 \log f - 13.82 \log h_B - a(h_R) + [44.9 - 6.55 \log h_B] \log d + C \quad (\text{dB})$$

$$a(h_R) = (1.1 \log f - 0.7)h_R - (1.56 \log f - 0.8)$$

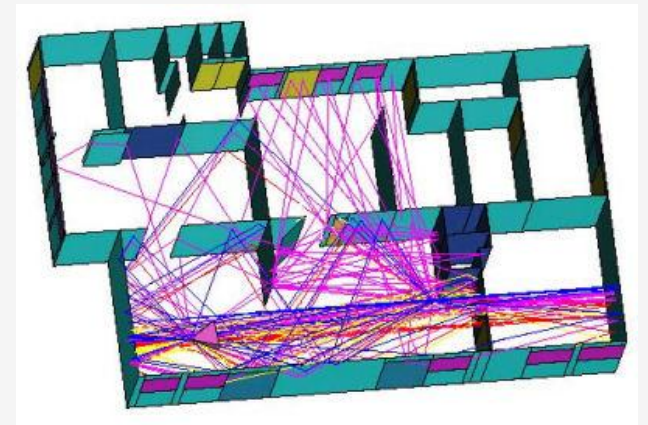
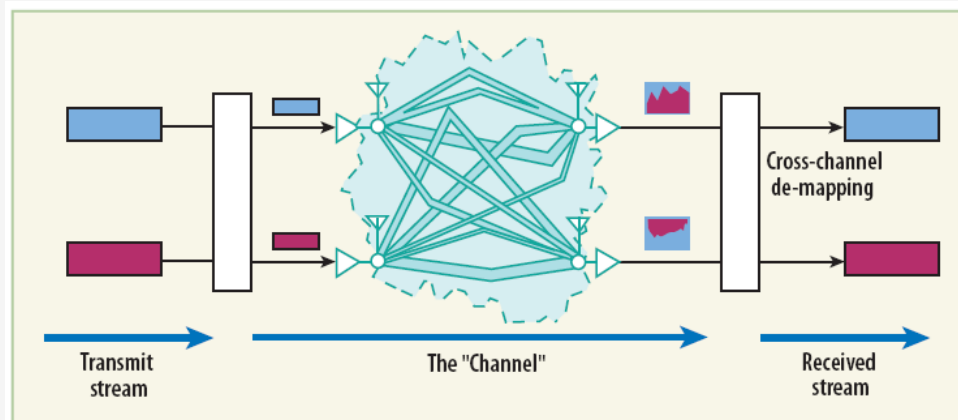
$$C = \begin{cases} 0 \text{ dB} & \text{for medium cities and suburban areas} \\ 3 \text{ dB} & \text{for metropolitan areas} \end{cases}$$

(1500-2000 MHz, 1-20 km)

This is typical of an “empirical” path loss model



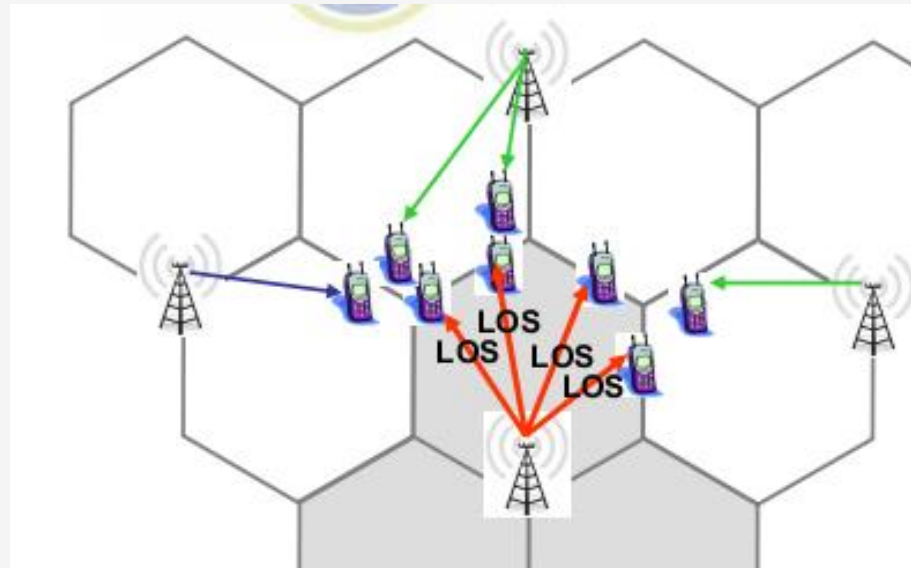
- **Example: MIMO WLAN - IEEE 802.11n (manufacturer's need)**
  - MIMO channels deeply involve the « space variant » characteristics of the channel (and the multi-antenna system)



## □ Example: LTE / LTE-A (manufacturer & operator's need)

- A more complicated networking scheme, implying a sophistication of channel models

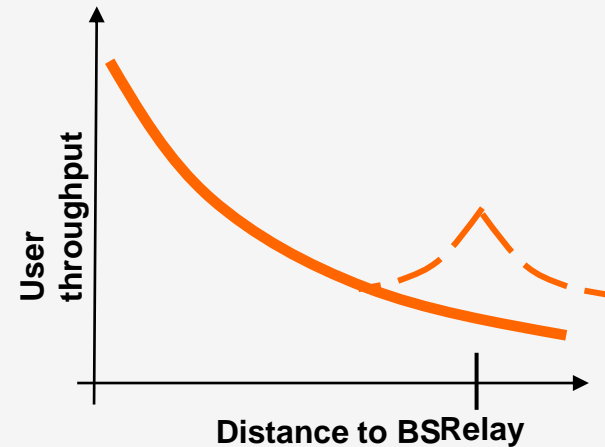
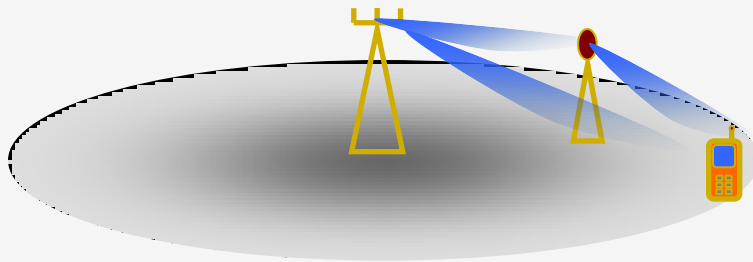
### Cell-Edge Beamforming



## □ Example: LTE / LTE-A (manufacturer & operator's need)

- A more complicated networking scheme, implying a sophistication of channel models

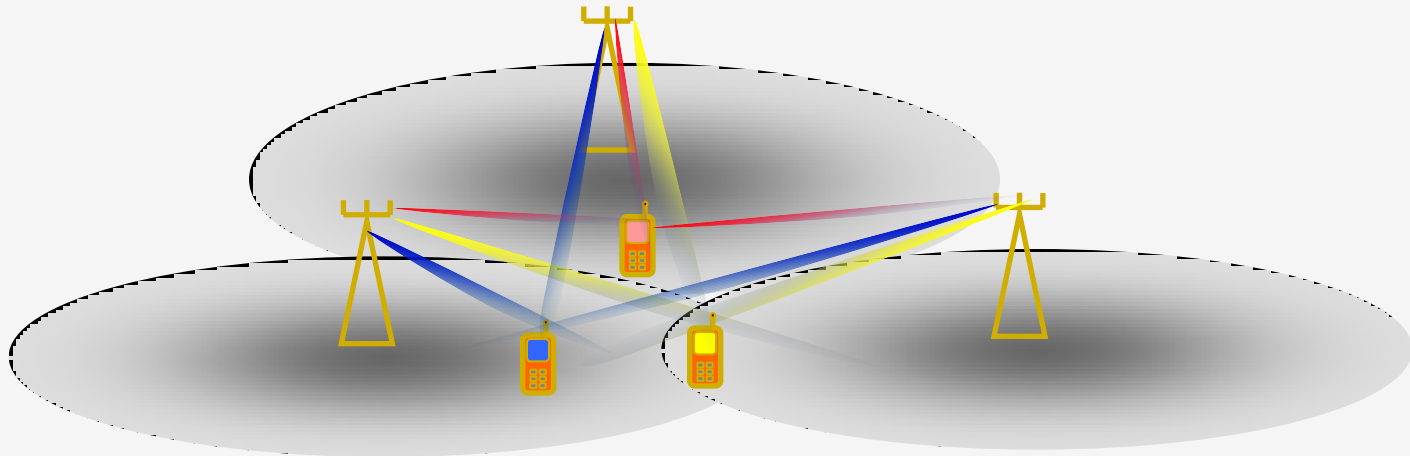
### Relaying



## □ Example: LTE / LTE-A (manufacturer & operator's need)

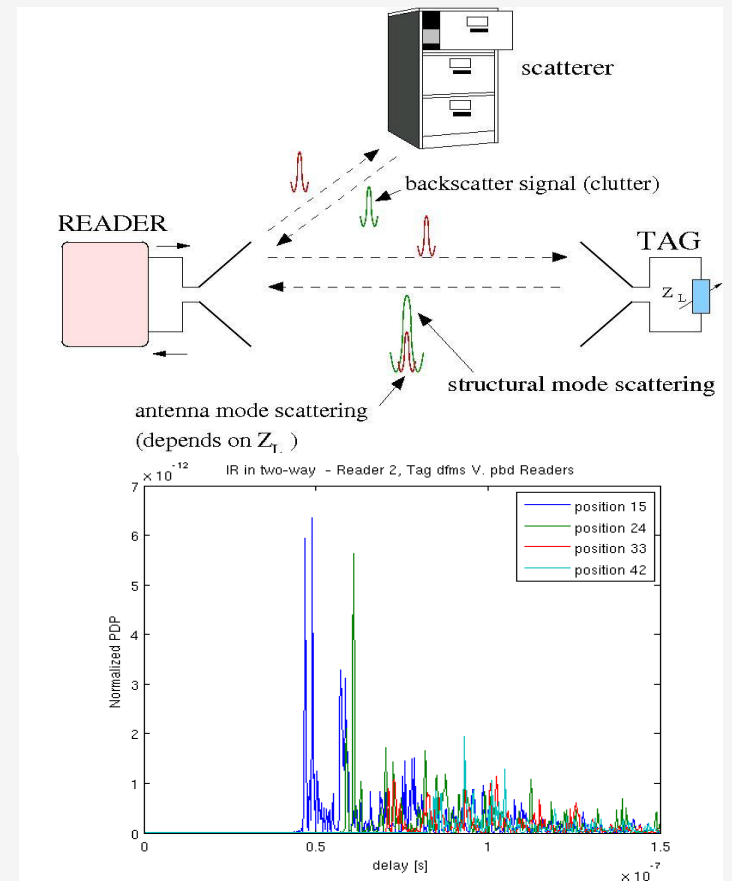
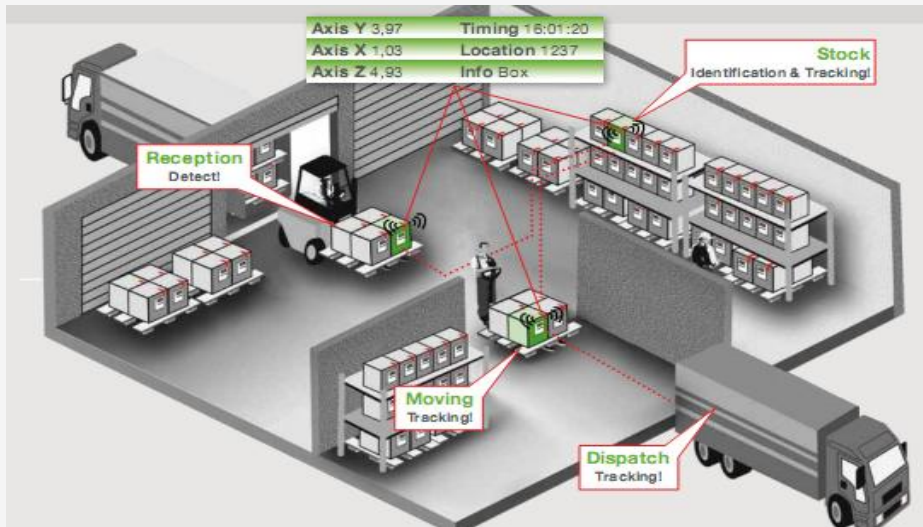
- A more complicated networking scheme, implying a sophistication of channel models

### Coordinated Multipoint Tx and Rx



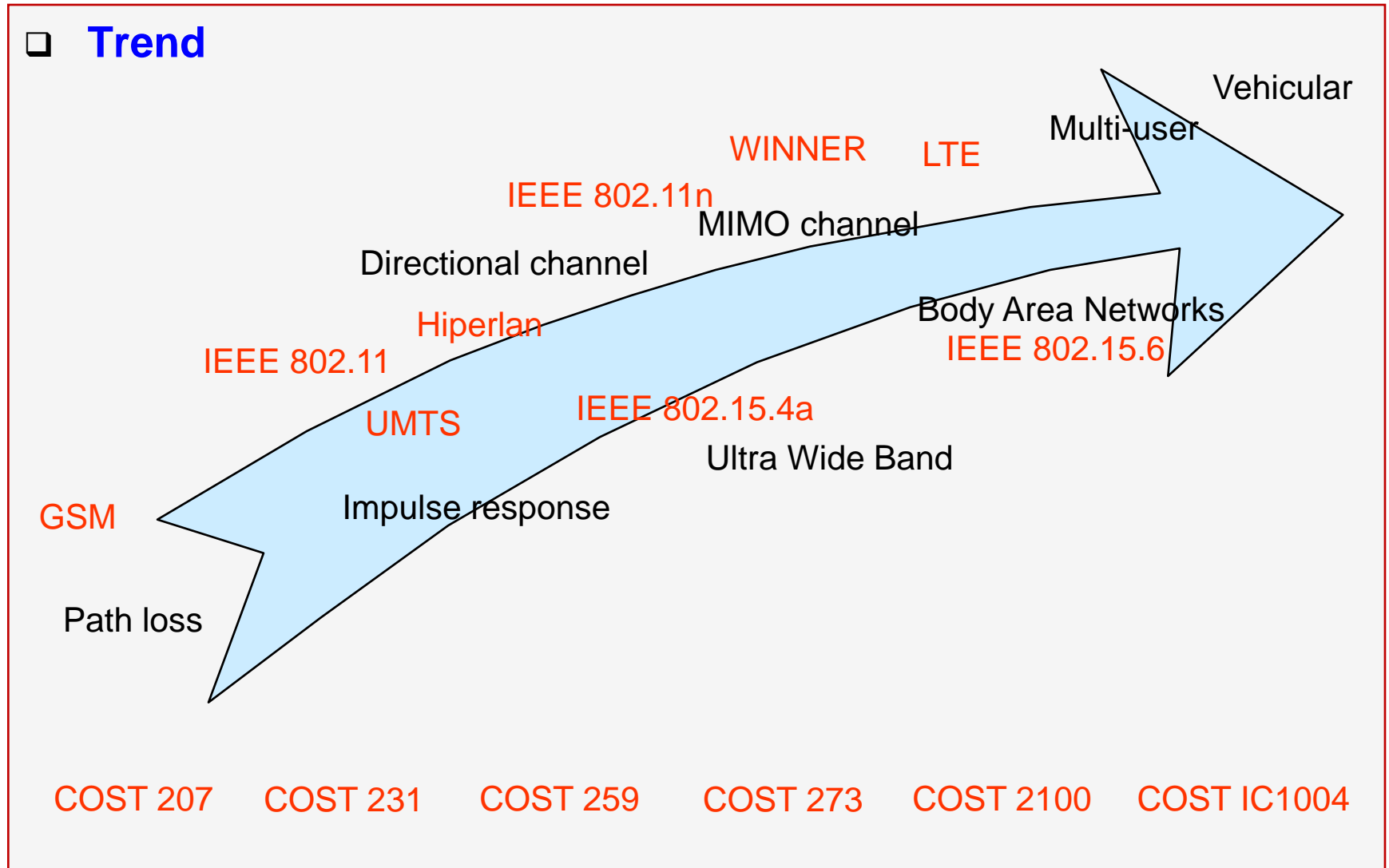
## □ Example: UWB – RFID (researcher’s game: ongoing)

- In every wireless communications research project, one needs to make channel measurement campaigns !



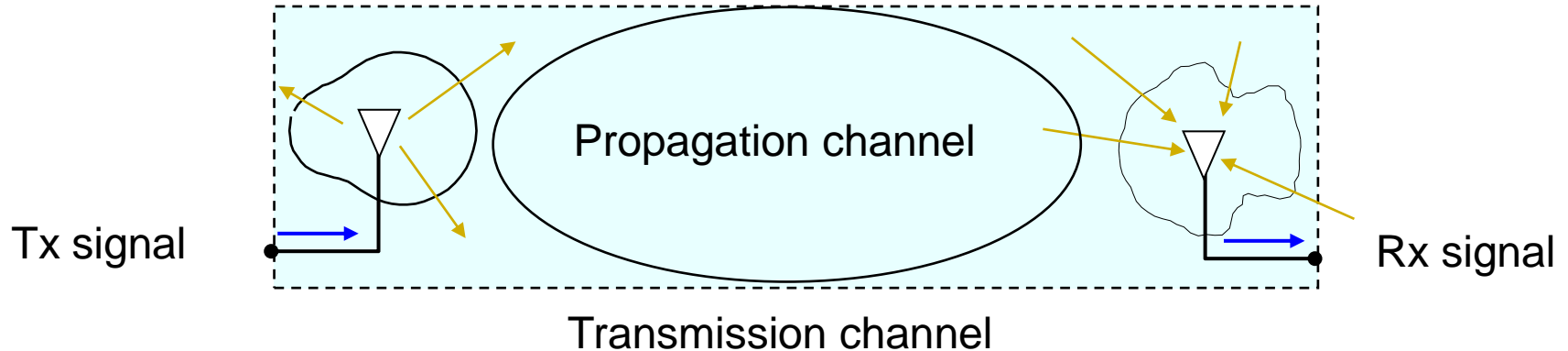
# Why do we need channel models ?

## □ Trend



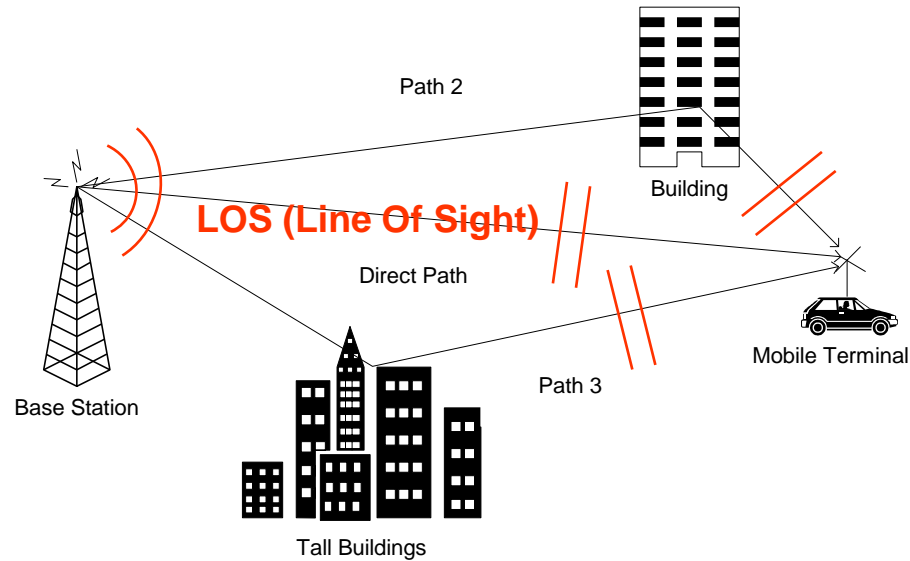


# Basics



- ❑ The **transmission channel** comprises antennas and all objects contributing or hampering propagation between input/output ports
- ❑ The **propagation channel** excludes the antennas and expresses all wave propagation phenomena between Tx and Rx
- ❑ Both channels are considered to be **linear (time variant) filters characterized by their impulse response**

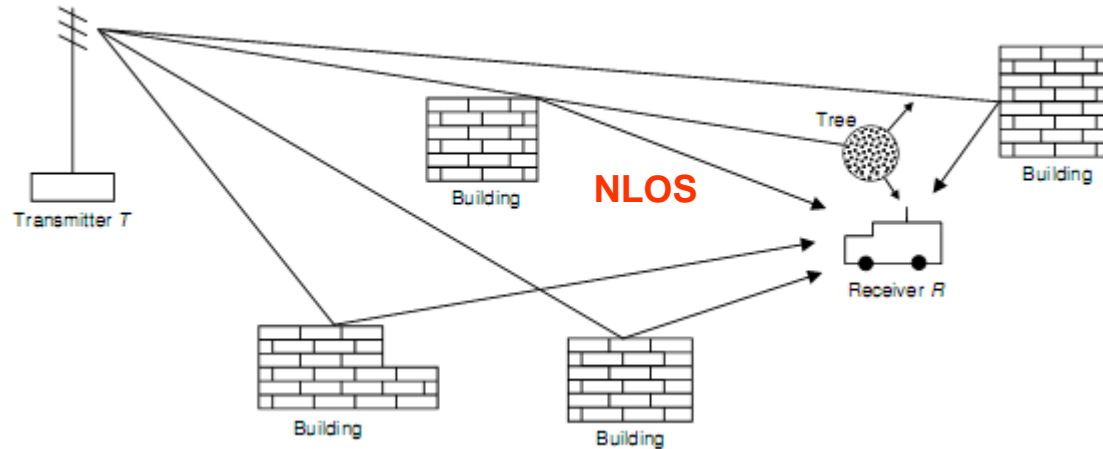




- ❑ **Spherical waves** at Tx
- ❑ **Planar waves** at Rx and in-between

**These are approximations !**

(may not be verified...)



Direct propagation (LOS path)

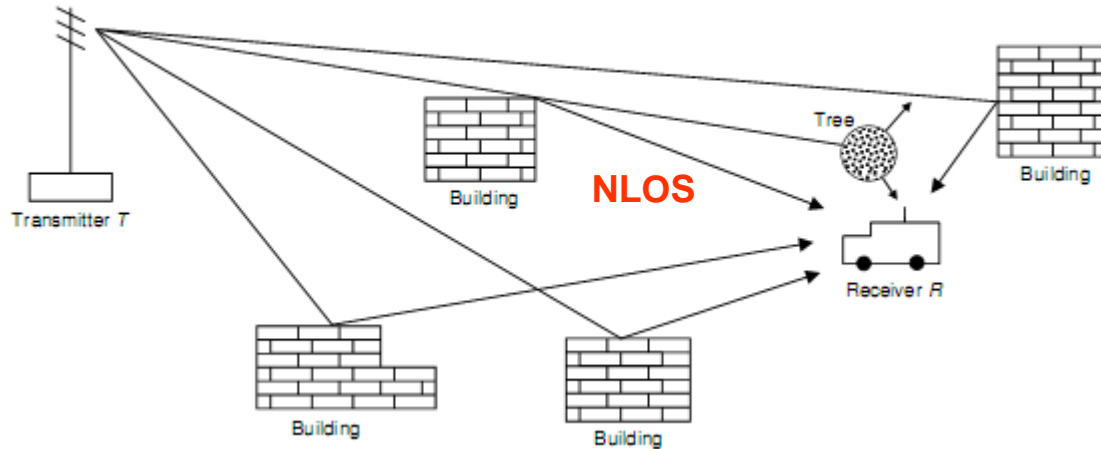
Specular reflection

Diffraction

Diffuse scattering

Refraction/transmission

} scatterers



- **The simple multipath based discrete channel model of the impulse response:**

$$h(t, \tau) = \sum_i A_i(t) \delta(\tau - \tau_i(t))$$

Time  $\uparrow$  Delay

$$H(t, F) = \sum_i A_i(t) \exp(-2j\pi F \tau_i(t))$$

Time  $\uparrow$  Frequency

At baseband,  $A_i(t)$  is complex valued

## ❑ What (may) need be modeled

- ❑ The multipath amplitudes
- ❑ The multipath angles (at Tx/Rx)
- ❑ The multipath delays
- ❑ The time dependence of these parameters

(comes from Tx/Rx mobility, or mobility of the environment)

For various environments, Tx/Rx distances, locations...

# Narrowband channels

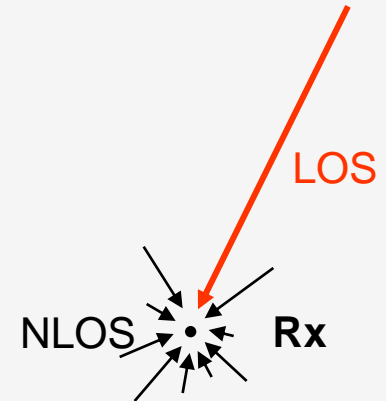


### □ Received signal:

$$r(t) = I(t)\cos(2\pi F_c t) - Q(t)\sin(2\pi F_c t)$$

$$I(t) = S_{LOS} \exp(j\varphi_{LOS}) + \sum_n S_n \exp(j\varphi_n) \Big|_t$$

$$Q(t) = S_{LOS} \exp(j\psi_{LOS}) + \sum_n S_n \exp(j\psi_n) \Big|_t$$

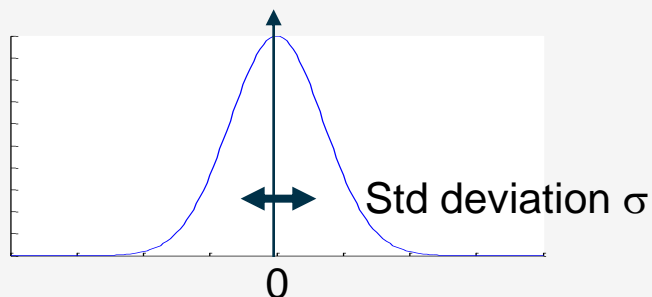


### □ Assumption:

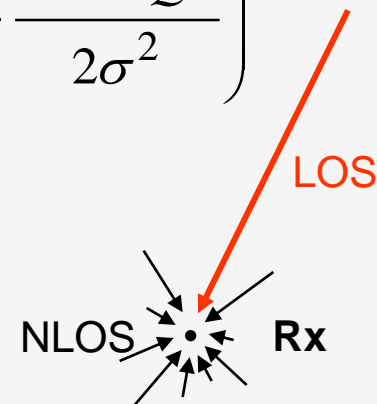
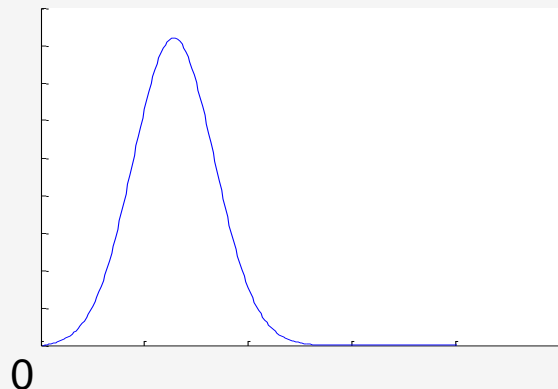
- $S_{LOS}$  behaves as a deterministic variable (DV)
- $S_n$  and  $\theta_n, \varphi_n$  behaves as random variables (RV)
- Central-limit theorem  $\Rightarrow I(t), Q(t)$  are non-centered, identically distributed Gaussian RV

## Statistics:

- Random part of  $I$ ,  $Q$ :  $PDF(I \text{ or } Q) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{I^2 \text{ or } Q^2}{2\sigma^2}\right)$



- Envelope  $|r|$



Rice distribution:

$$PDF = \frac{|r|}{\sigma^2} \exp\left(-\frac{|r|^2 + S_0^2}{2\sigma^2}\right) I_0\left(\frac{|r|S_0}{\sigma^2}\right)$$

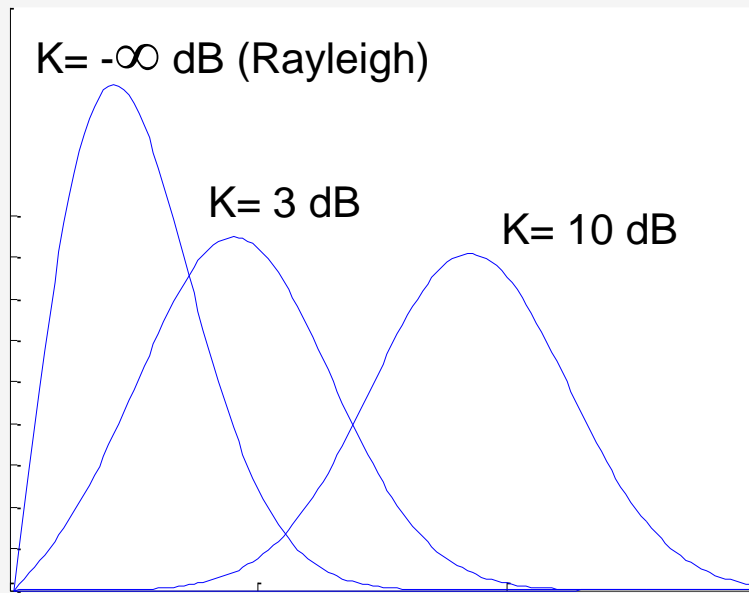
K factor: ratio of deterministic to random mean powers

$$K = \frac{S_0^2}{2\sigma^2}$$

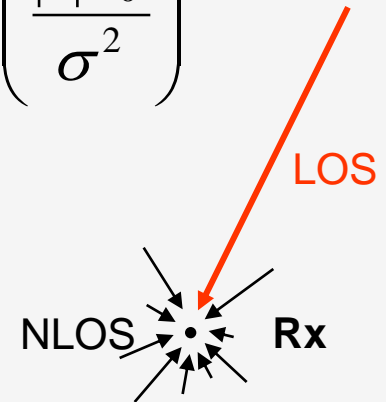


### Statistics:

□ Rice distribution:  $PDF = \frac{|r|}{\sigma^2} \exp\left(-\frac{|r|^2 + S_0^2}{2\sigma^2}\right) I_0\left(\frac{|r|S_0}{\sigma^2}\right)$



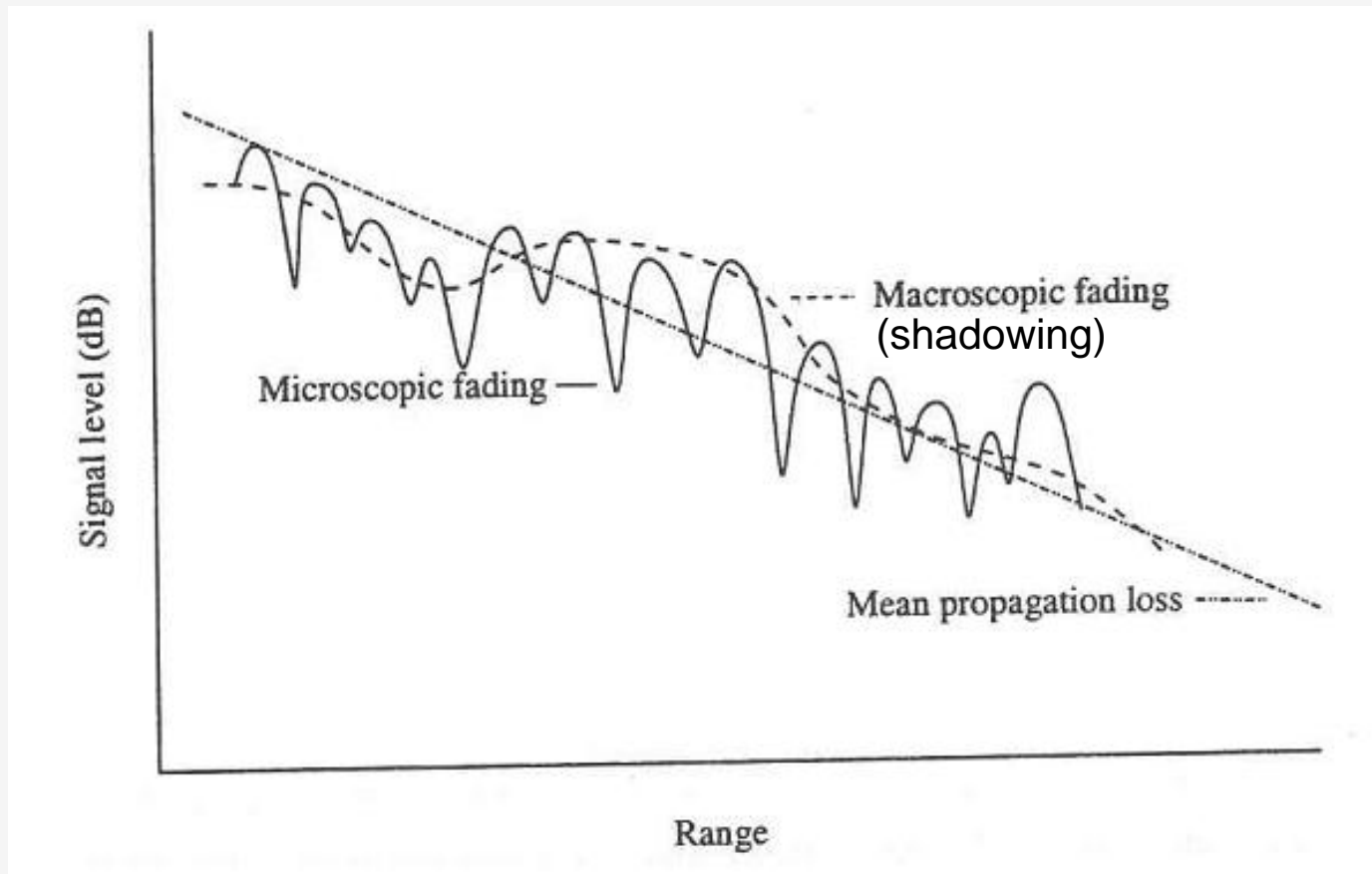
$$K = \frac{S_0^2}{2\sigma^2}$$







### □ Small distance/medium distance/long distance fading



### □ Long distance fading

□ Friis formula (free space):

$$\frac{P_r}{P_t} = G_r G_t \left( \frac{\lambda}{4\pi d} \right)^2 \propto d^{-2}$$

$$G_r, G_t = 1 \Rightarrow P_r = \frac{P_t}{L} \quad L_{dB} = 32.4 + 20 \log(d_{km}) + 20 \log(F_{MHz})$$

**Going from 1 GHz to 10 GHz  $\Rightarrow$  20 dB higher attenuation !**

□ Is this **frequency dependence** maintained in NLOS channels ?

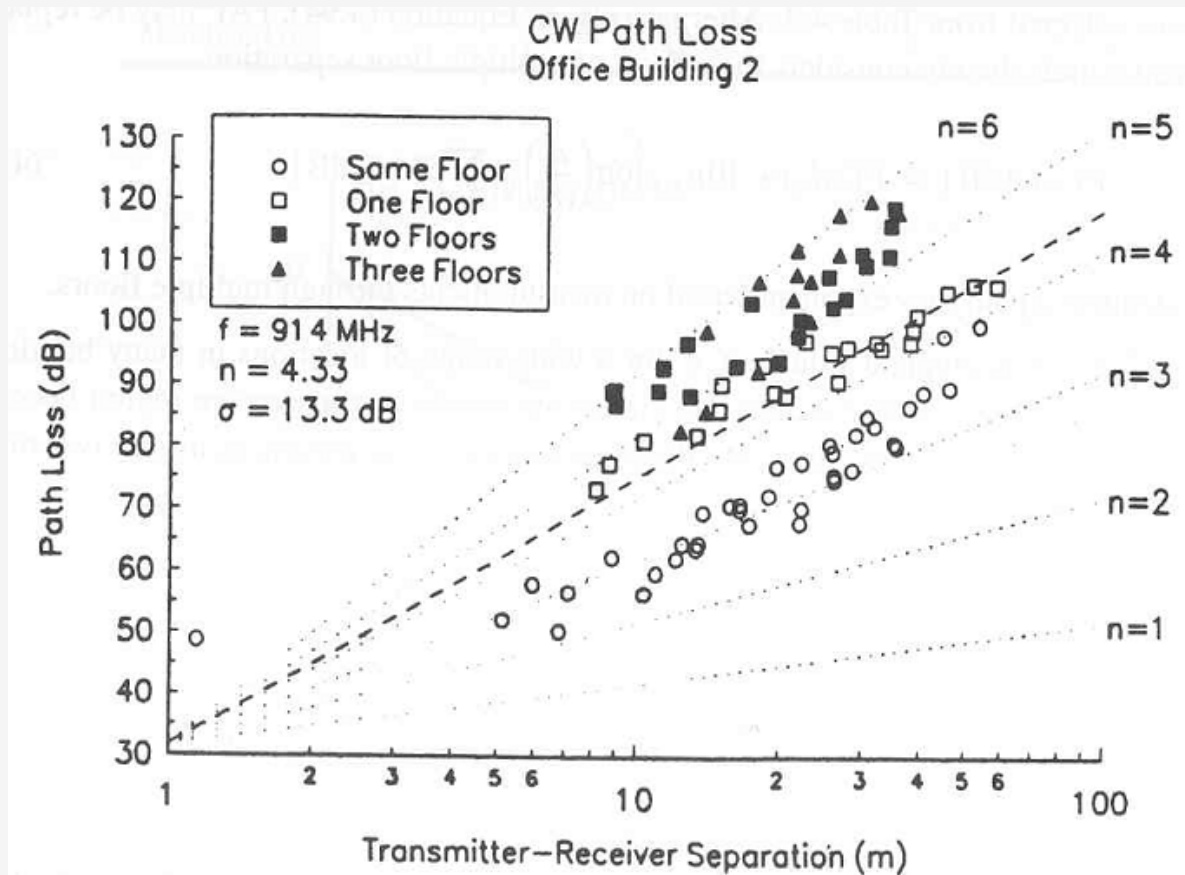
Yes ! Frequency variations *roughly speaking* obey  $F^{-2}$  in NLOS

□ Is this **distance dependence** maintained in NLOS channels ?

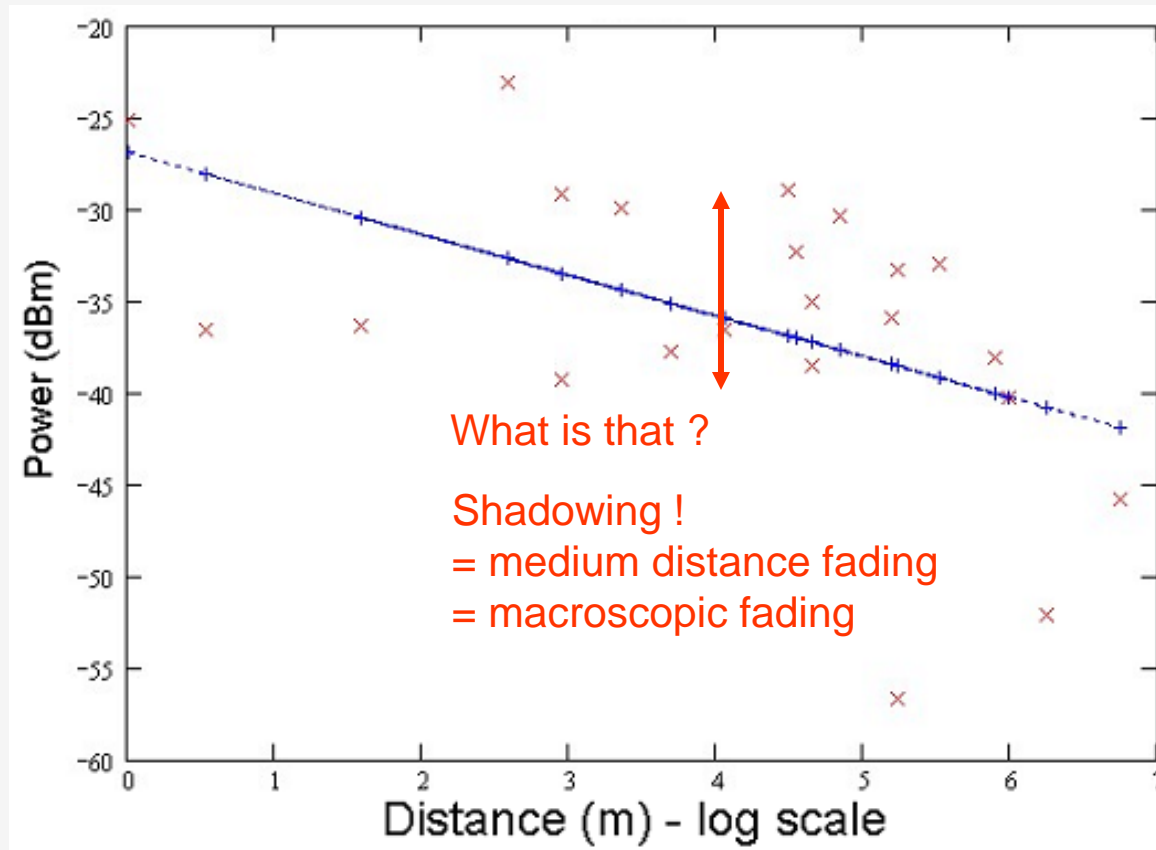
No ! The path loss exponent  $n$  often exceeds 2

$$\frac{L(d)}{L(d_0)} \propto \left( \frac{d}{d_0} \right)^n$$

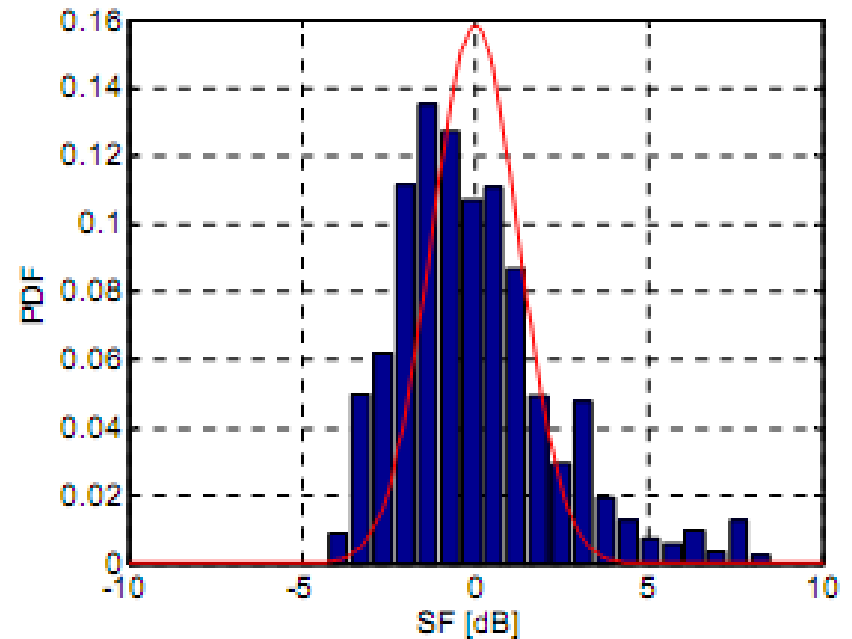
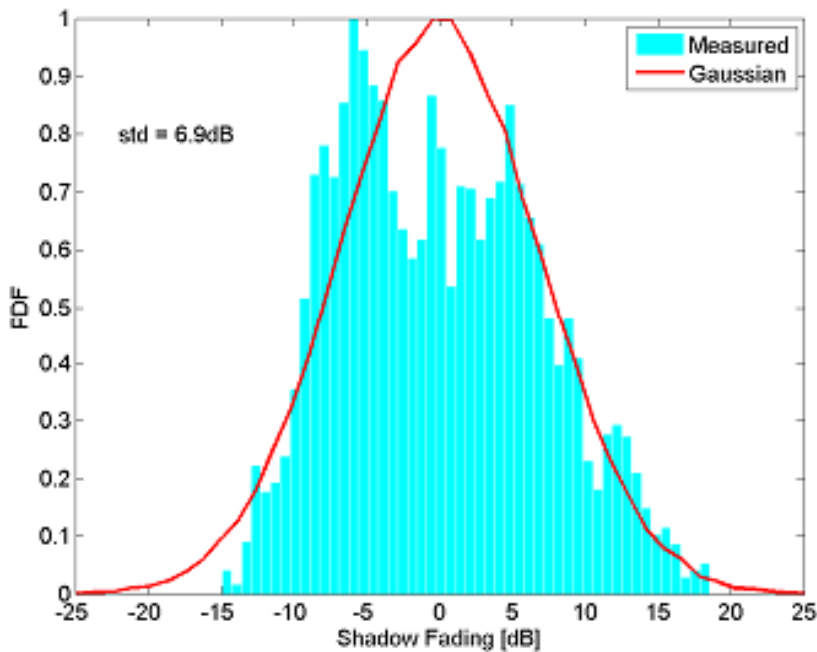
### □ Long distance fading



### □ Medium distance fading



### Medium distance fading



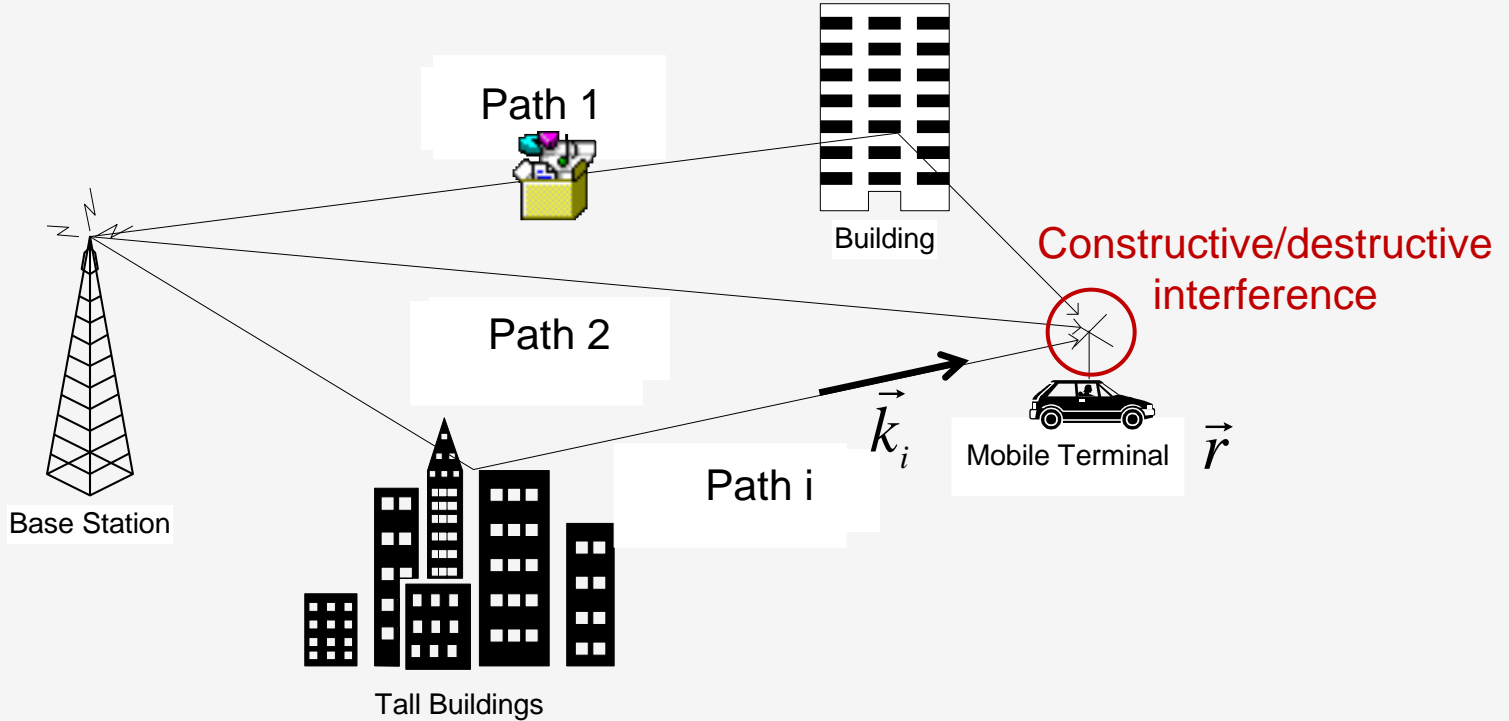
Gaussian in dB = lognormal fading

# Wideband channels

## Small scale / short term / wideband fading

Constructive/destructive interference between multipaths

$$H(t, F, \vec{r}) = \sum_i A_i(t) \exp(-2j\pi F \tau_i(t, \vec{r})) \quad \tau_i(t, \vec{r}) = \tau_i(t, \vec{0}) - \frac{\vec{k}_i \cdot \vec{r}}{2\pi F}$$

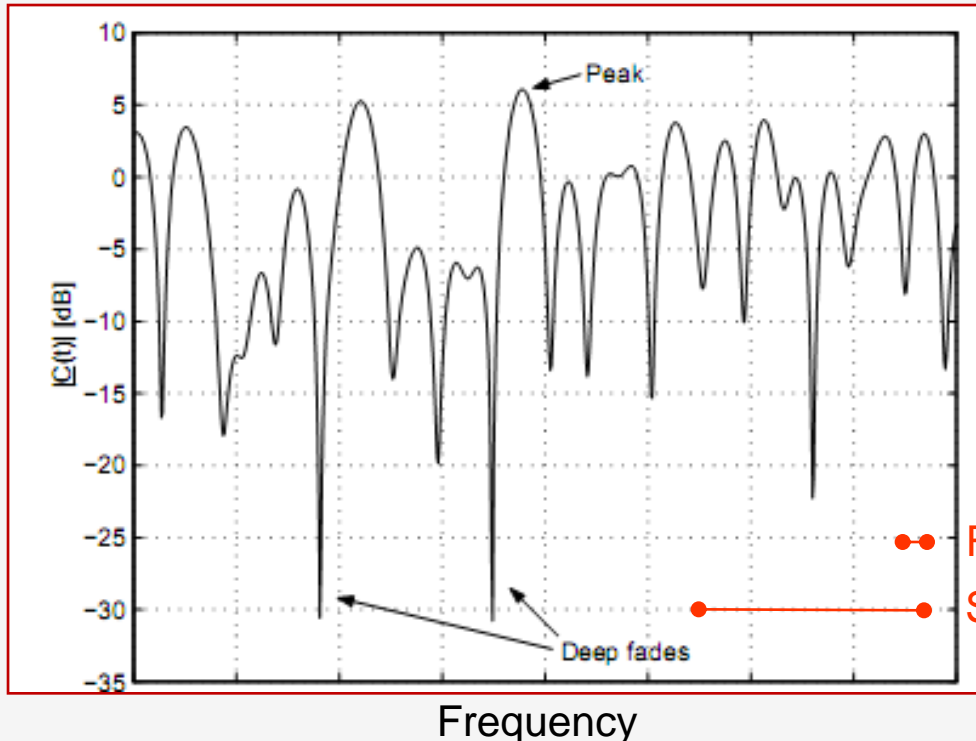


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↔ Coherence band width

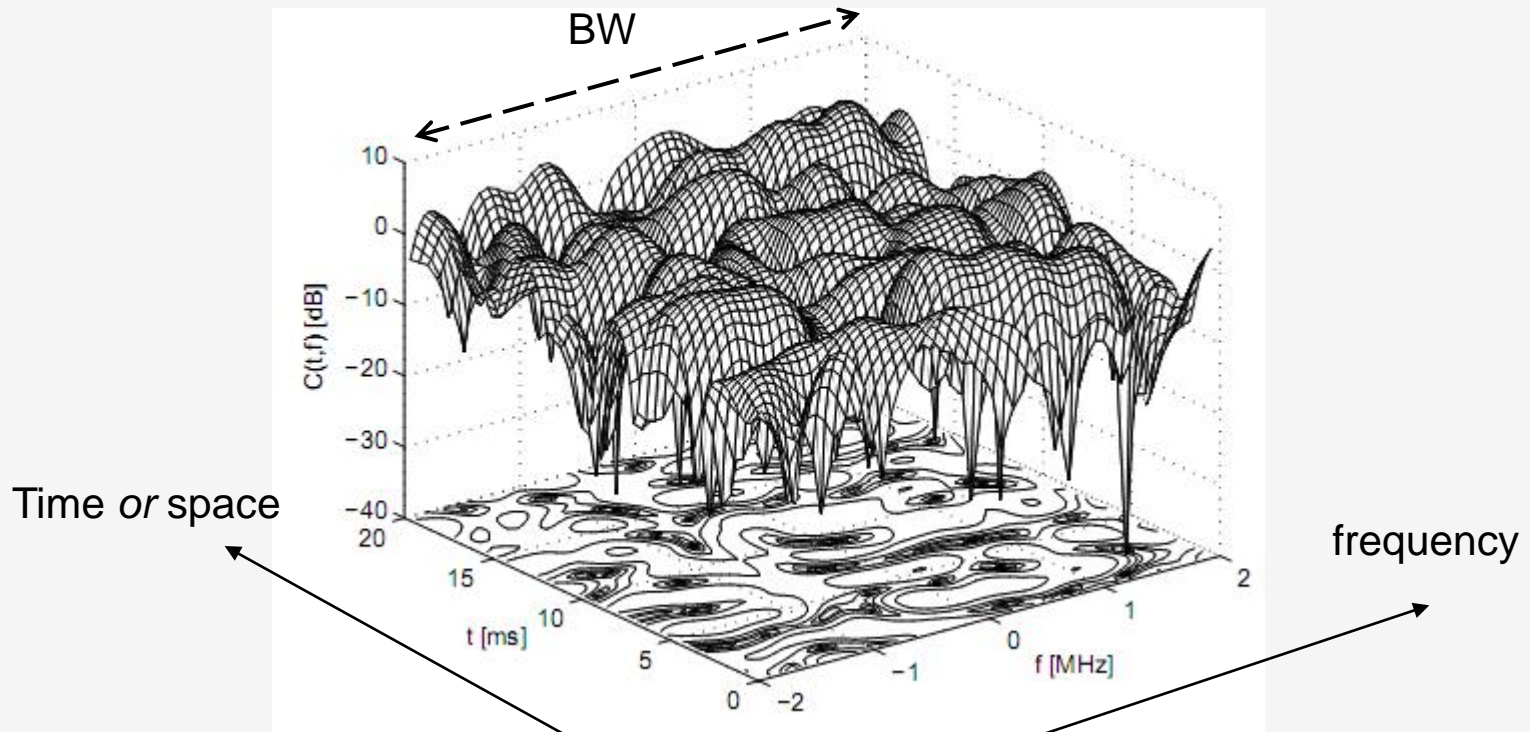




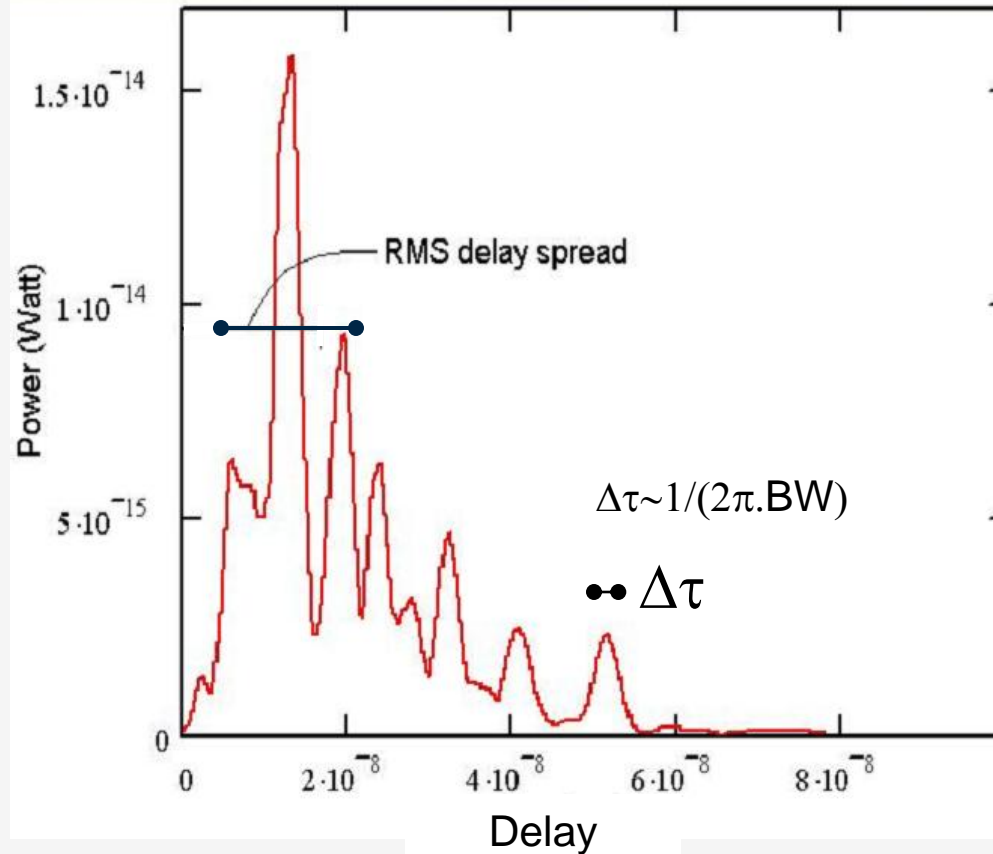
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## □ Frequency ↔ Delay (Fourier): impulse response

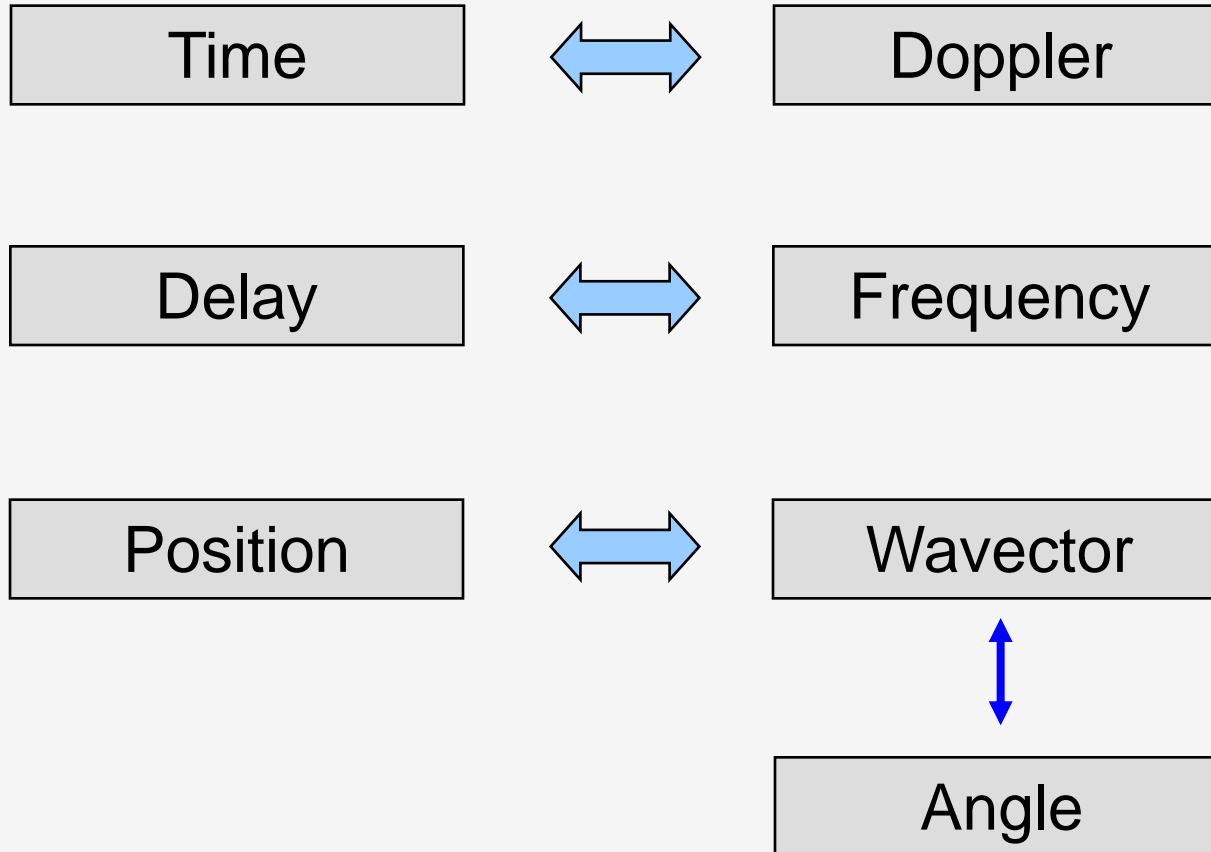


$$\bar{\tau} = \frac{\sum_k P(\tau_k) \tau_k}{\sum_k P(\tau_k)}$$

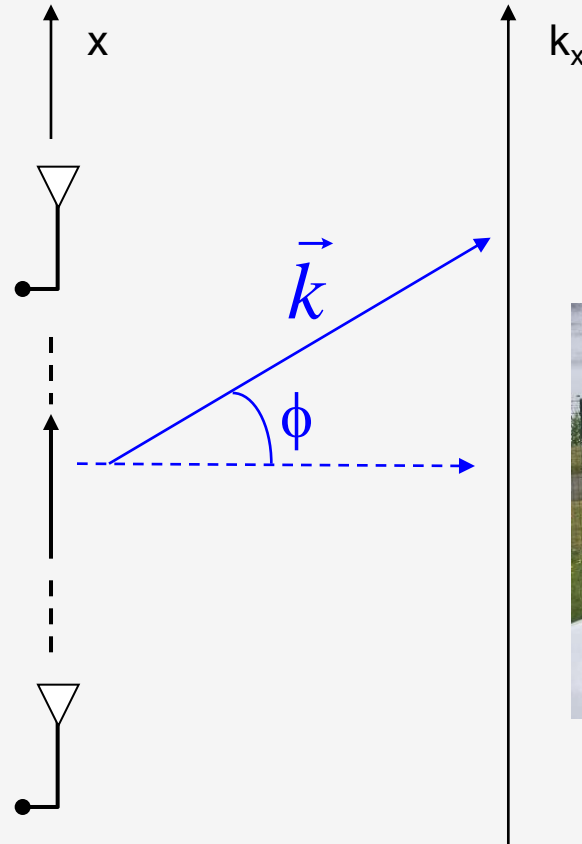
$$\tau^2 = \frac{\sum_k P(\tau_k) \tau_k^2}{\sum_k P(\tau_k)}$$

$$\tau_{\text{rms}} = \sqrt{\tau^2 - (\bar{\tau})^2}$$

## □ Fourier pairs



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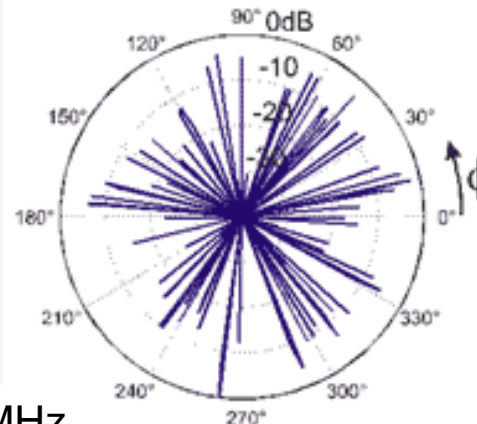


$$\exp(jk_x x) = \exp(jkx \sin(\phi))$$

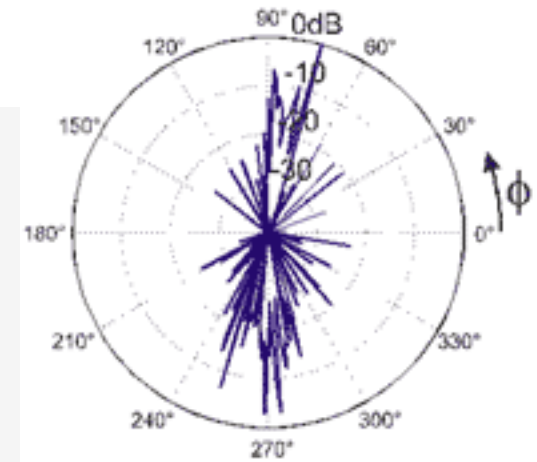
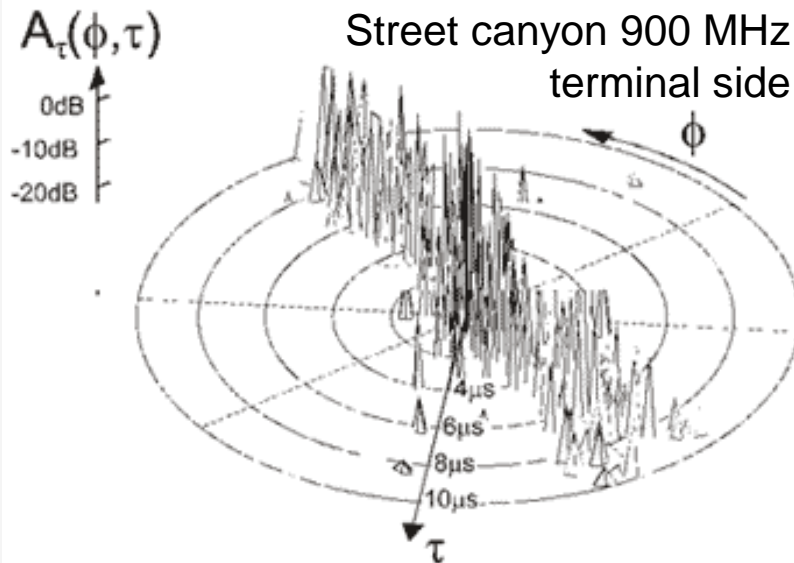


- The directional spectrum is obtained from the spatial structure of the signal

## □ Angle vs. delay



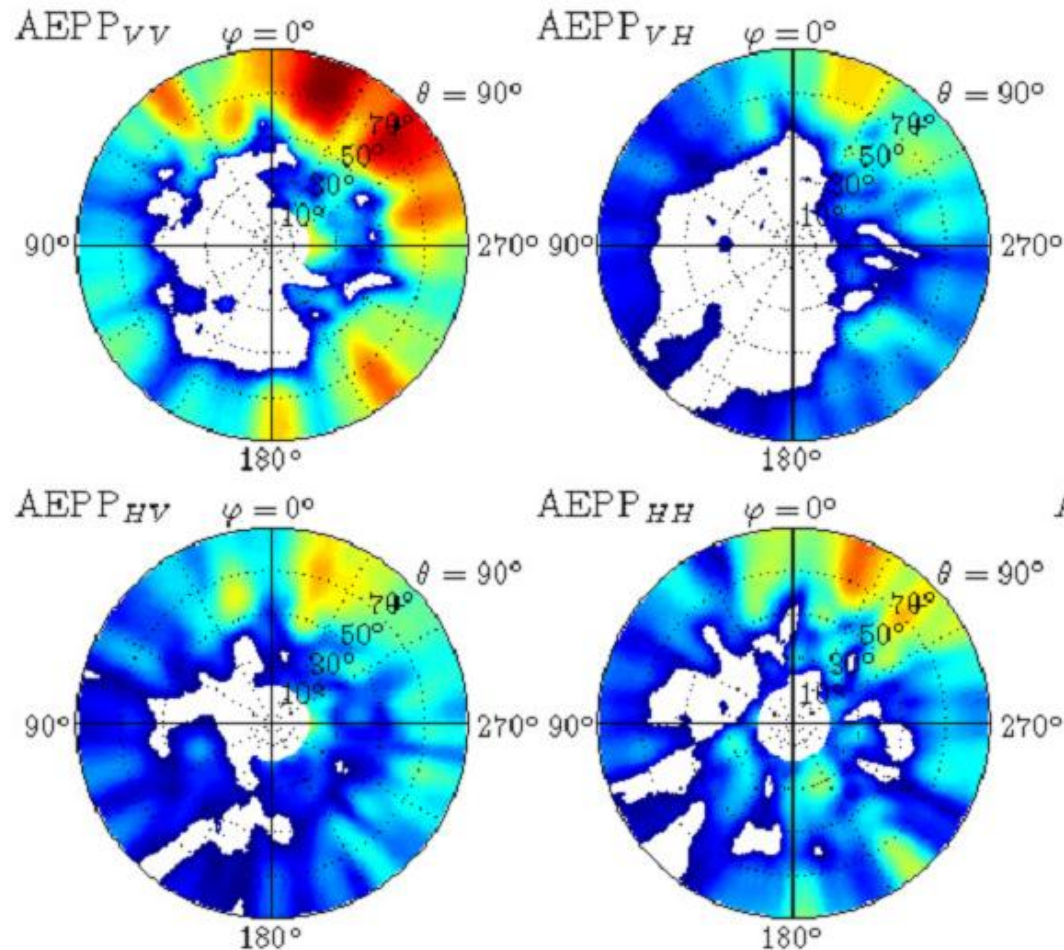
(a)  
 $\tau < 0.4 \mu\text{s}$



(b)  
 $\tau > 0.4 \mu\text{s}$

## □ Angle vs. delay

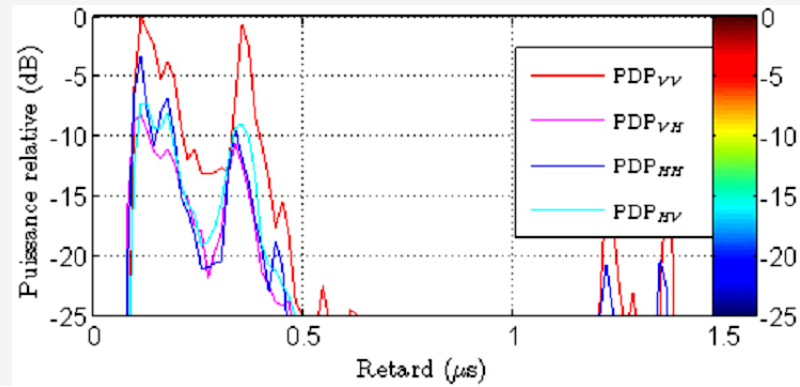
*Dunand & Conrat, 2008*





## □ Angle vs. delay

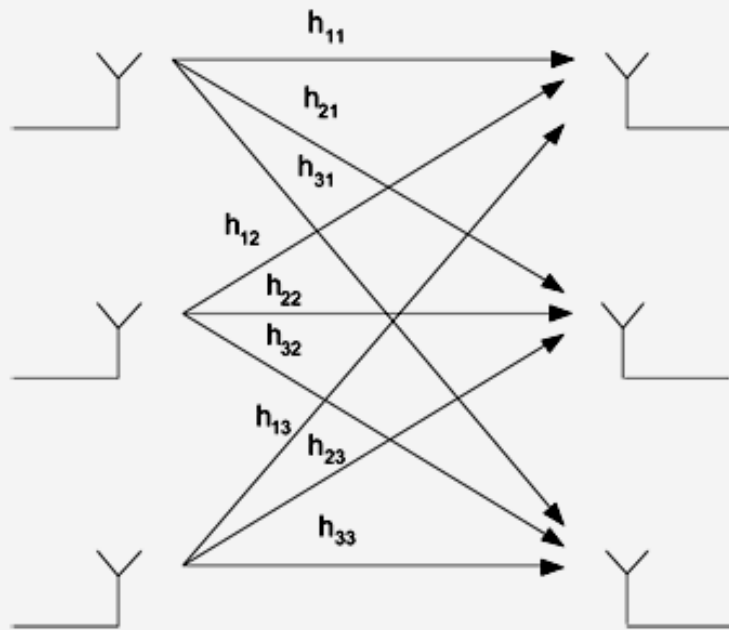
*Dunand & Conrat, 2008*



# MIMO channels



□ The impulse response becomes a matrix !



$$\mathbf{H}(\tau) = \begin{bmatrix} h_{11}(\tau) & h_{12}(\tau) & \cdots & h_{1M}(\tau) \\ h_{21}(\tau) & h_{22}(\tau) & \cdots & h_{2M}(\tau) \\ \vdots & \vdots & \ddots & \vdots \\ h_{N1}(\tau) & h_{N2}(\tau) & \cdots & h_{NM}(\tau) \end{bmatrix}$$

- The relative variation of coefficients (with position, frequency, time) dramatically impacts the diversity/spatial multiplexing performance
- The multipath structure is responsible for this variation

- **A non physical approach : based on the structure of the MIMO correlation matrix**  $\mathbf{R}_h = E\{\mathbf{h}\mathbf{h}^H\}$ , with  $\mathbf{h} = \text{vec}(\mathbf{H})$

Kronecker approximation: 
$$\mathbf{R}_h \approx \frac{1}{\sqrt{\text{tr}\{\mathbf{R}_{RX}\}}} \mathbf{R}_{RX} \otimes \mathbf{R}_{TX}^T$$

The method lends itself to easy stochastic generation in a software tool: 
$$\mathbf{H} = c \cdot \mathbf{R}_{RX}^{1/2} \mathbf{G} \mathbf{R}_{TX}^{1/2}, \text{ with } \mathbf{G} \sim \mathcal{CN}(\mathbf{0}, \mathbf{I})$$

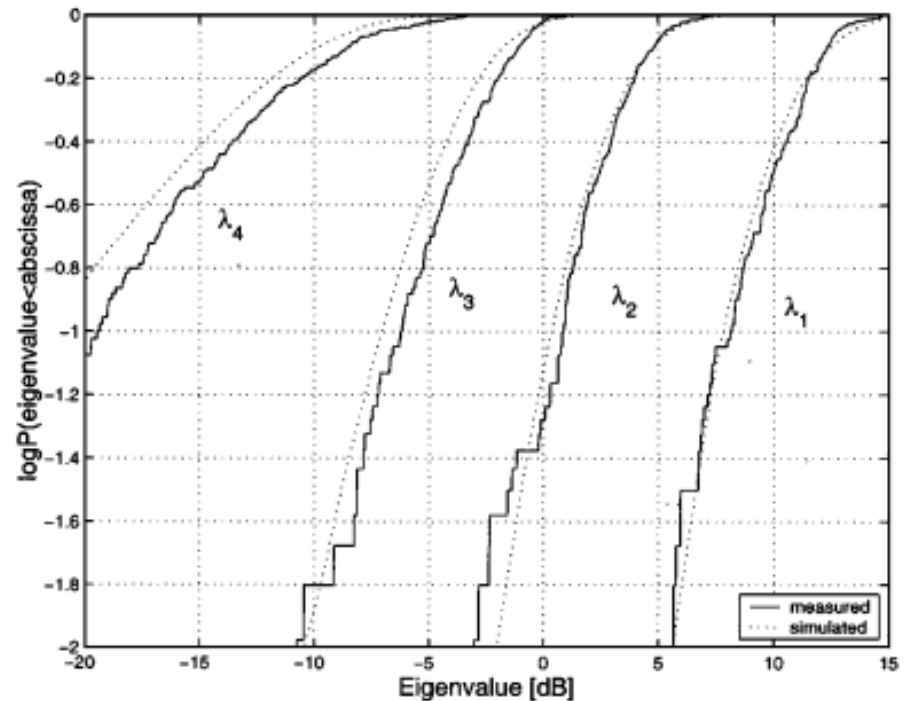
**Statistical modeling: define statistical distributions for the coefficients of the correlation matrices**

 **3GPP (LTE), IEEE 802.11n, IEEE 802.16...**

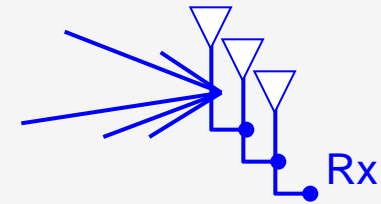
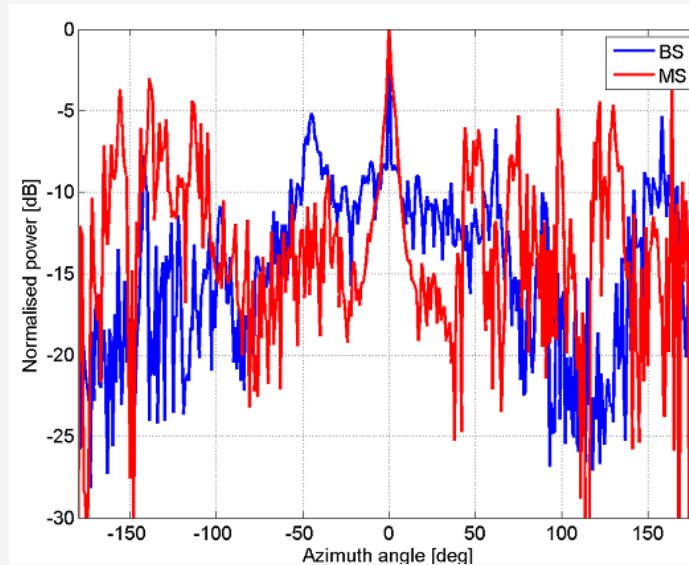
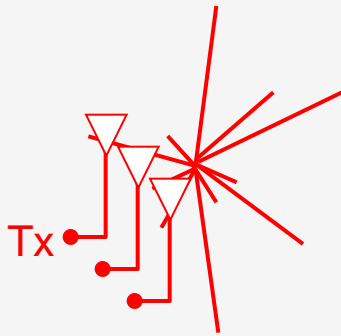
- A non physical approach : based on the structure of the MIMO correlation matrix  $\mathbf{R}_h = E\{hh^H\}$ , with  $\mathbf{h} = \text{vec}(\mathbf{H})$

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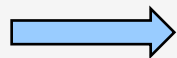
$$\begin{aligned} \mathbf{H} &= \mathbf{U}\mathbf{\Lambda}\mathbf{V}^H \\ &= \sum_{i=1}^{\min(n_R, n_T)} \lambda_i \mathbf{u}_i \mathbf{v}_i^H \end{aligned}$$



## □ Double directional channels for MIMO channel modeling

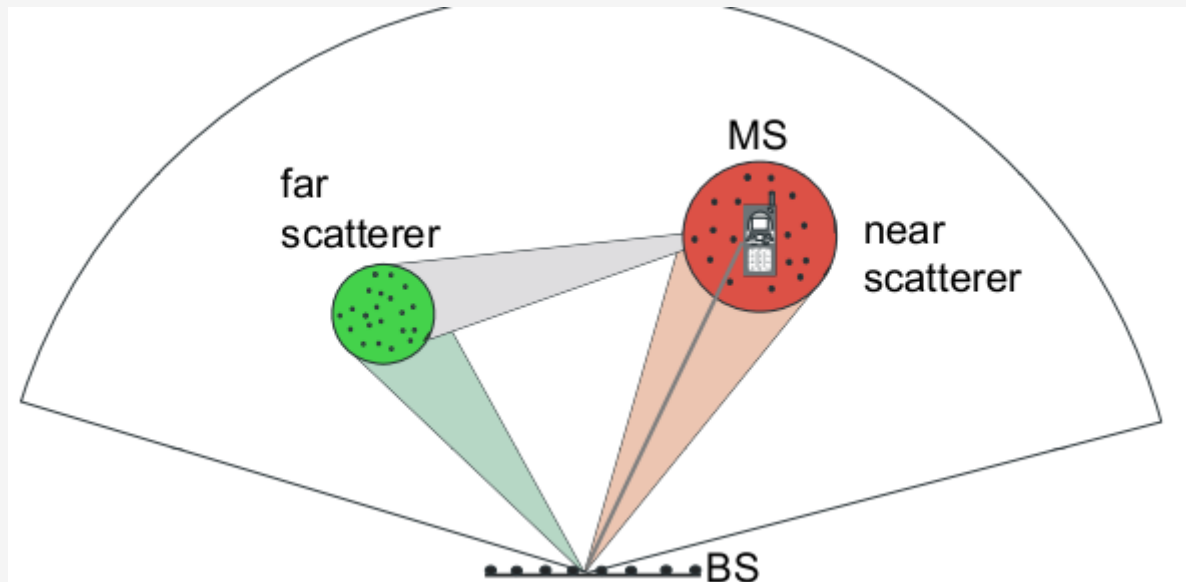


**Statistical modeling: define statistical distributions for path amplitudes, path delays, path DoA, path DoD...**



**3GPP, IEEE 802.11n, IEEE 802.16...**

- A semi-physical modeling approach : GSCM (Geometry-based Stochastic Channel Modeling)

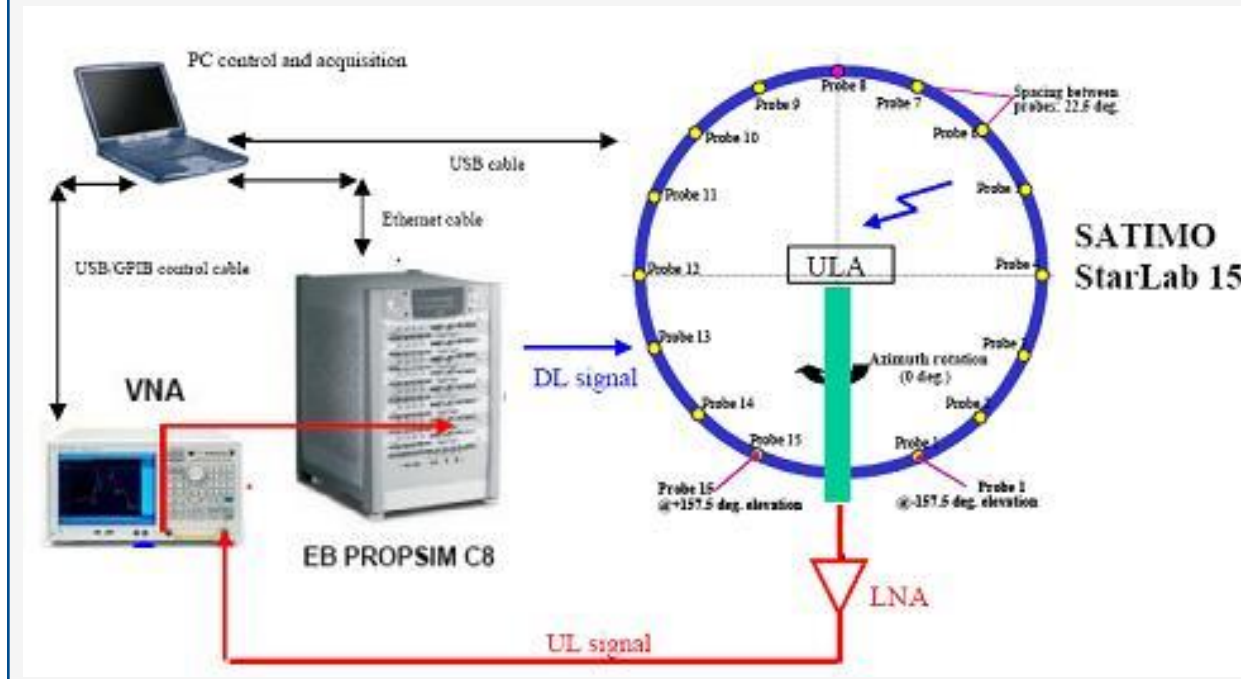
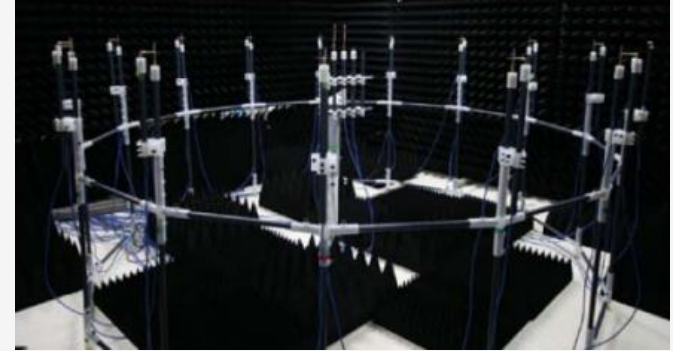


**Statistical modeling: define statistical distributions for scatterers positions, characteristics...**

**→ COST 259, 273, 2100...**

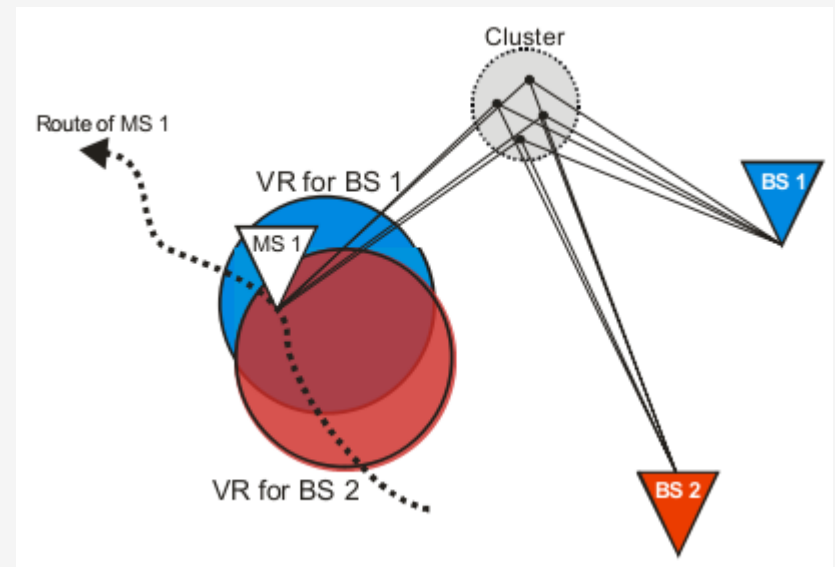
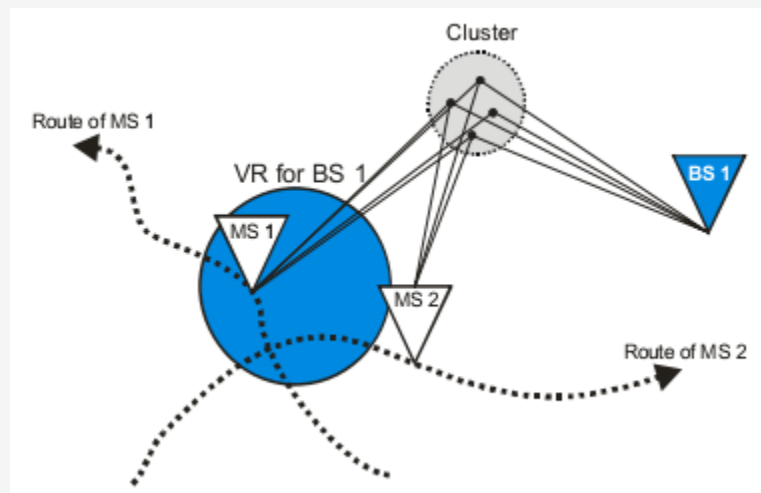
## □ What's that for ?

- Example : standardization of OTA  
(Over The Air) test methods  
for MIMO terminals



# Multi-link channels

- ❑ **Multi-link channels are encountered in future networks**
  - ❑ Where BS can simultaneously be connected to several users
  - ❑ for which terminals may simultaneously be connected to several BS

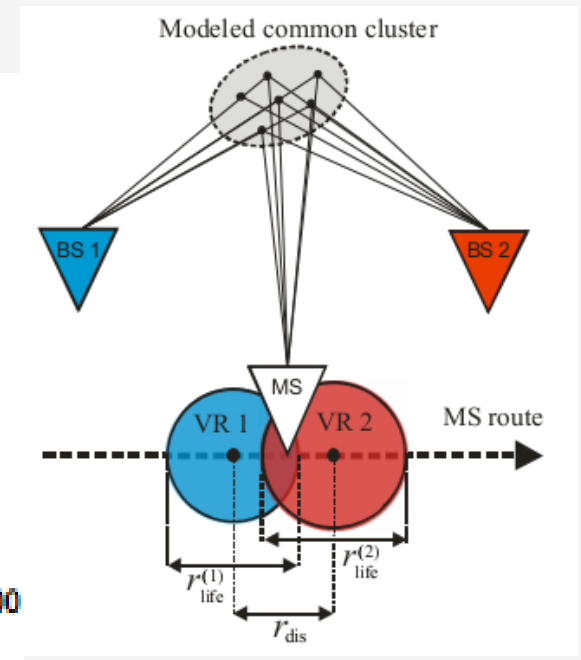
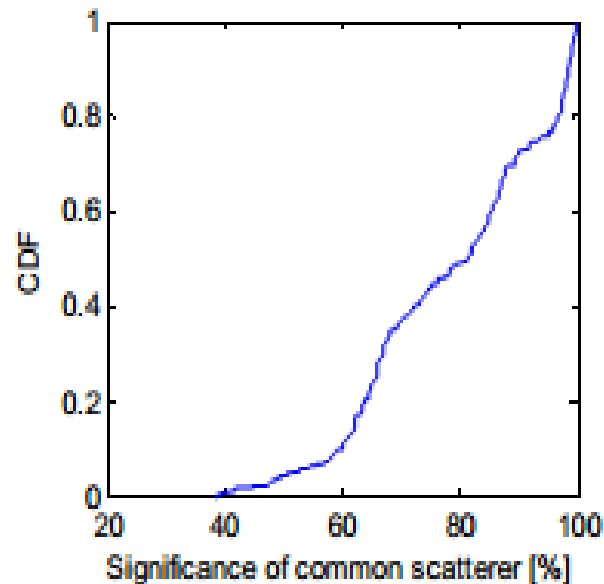
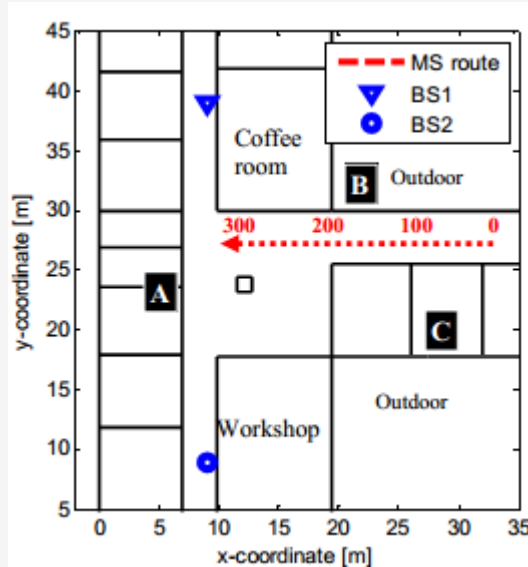




## Multi-link channels are encountered in future networks

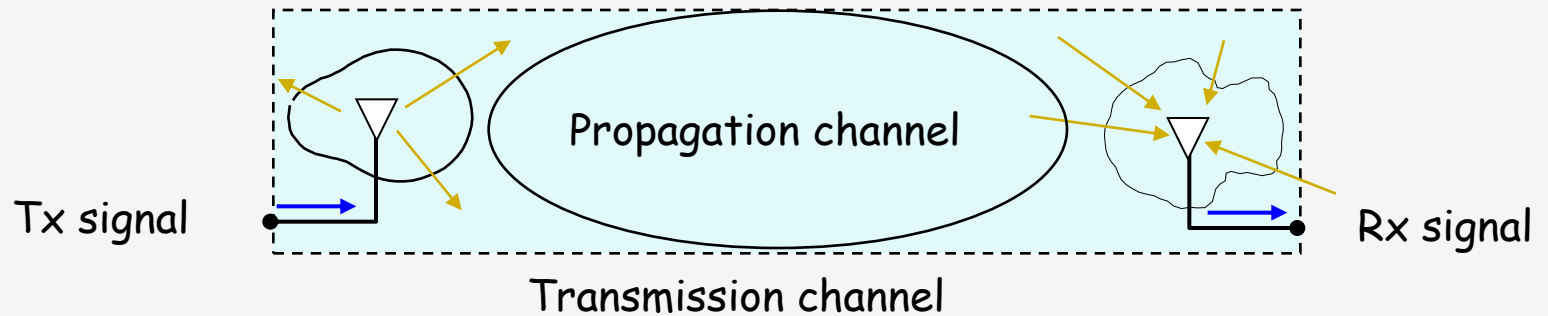
- Where BS can simultaneously be connected to several users
- for which terminals may simultaneously be connected to several BS

➡ channel modeling requires proper account of macroscopic spatial correlations



## Perspectives & conclusion

## Antennas are part of the radio channel !



An instrumentation antenna  
(for channel measurements)

#



A use case

## □ Antennas are part of the radio channel !

The super-antenna concept: antenna + user in near field



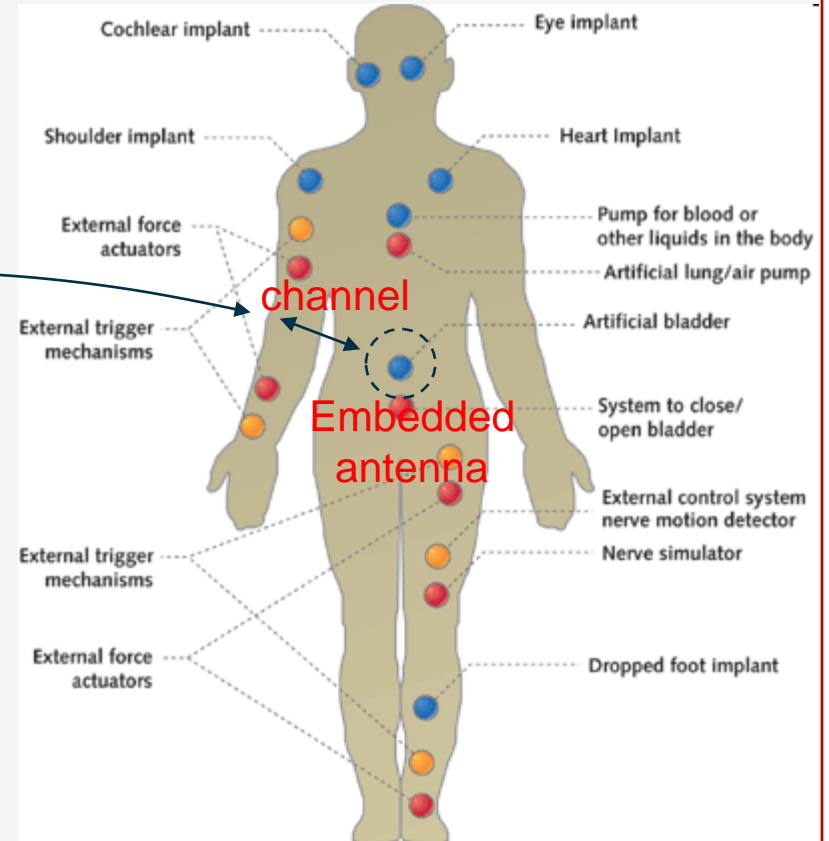
*F. Harrysson et al., COST 2100 TD 07-379, Sep. 2007*

## ❑ Antennas are part of the radio channel !

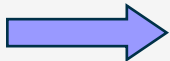
In-body antennas:  $\epsilon \sim 50$   $\sigma \sim 2$  S/m !



channel

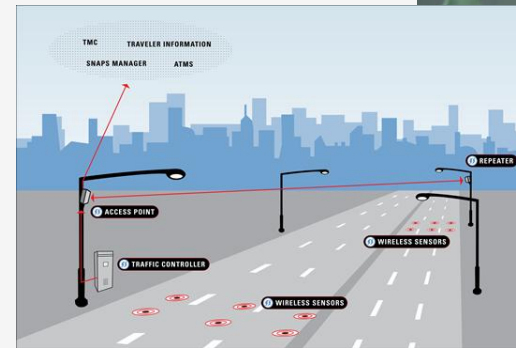
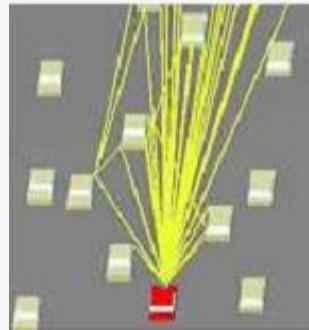
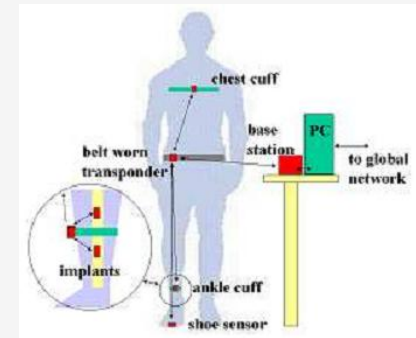
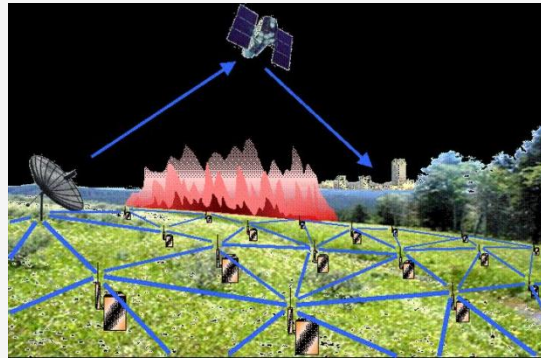
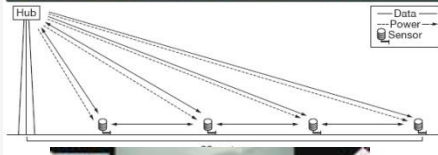
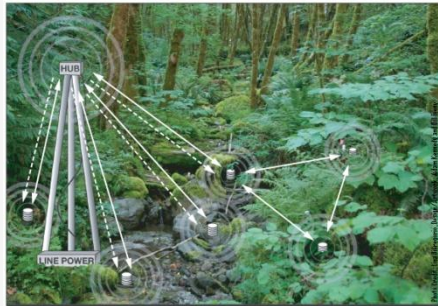


Embedded  
antenna



Composite antenna-channel problem

## □ A variety of propagation environments for new wireless use cases



- ❑ **The main message: radio channel modeling is a rich subject, combining propagation physics, data processing and a lucid view of systems/networks requirements**
  
- ❑ **The increasing sophistication of channel investigations and models stems from the complexification of wireless networks, from picocells to macrocells (even satellites) throughout**
  
- ❑ **It seems that researchers in this area are not yet jobless 😊**

